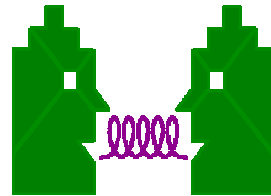




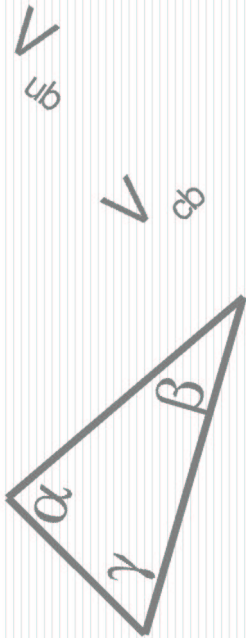
# Measurement of the CKM Matrix Element $|V_{ub}|$ with *BABAR*



ICHEP 2002 Amsterdam

Parallel Session  
CP Violation and the CKM Matrix

July 25<sup>th</sup>, 2002



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for the *BABAR* Collaboration



# Outline of the Presentation

## Part I

- Inclusive versus Exclusive Measurements
- *BABAR* Dataset

## Part II

- Inclusive Endpoint-Spectrum Analysis
- Preliminary Result

## Part III

- Exclusive  $B \rightarrow \rho e \nu$  Analysis
- New Preliminary Result



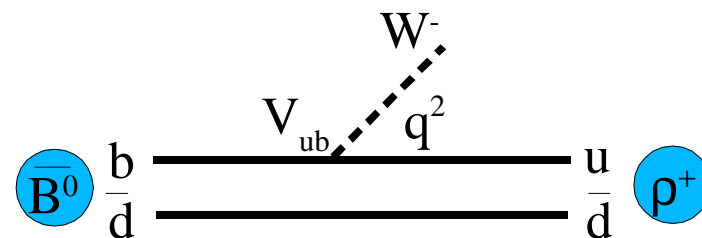
# Inclusive vs. Exclusive Measurement of $|V_{ub}|$

## ● Inclusive:

- blind to decay channel
- due to large  $b \rightarrow c e \nu$  backgrounds only sensitive in a small lepton energy region
- need to extrapolate visible rate to total rate, introducing large model dependencies
- can use inclusive photon spectrum  $b \rightarrow s \gamma$  to measure Fermi motion and reduce extrapolation uncertainty
- need Operator Product Expansion and b-quark mass to extract  $|V_{ub}|$  from the total rate.

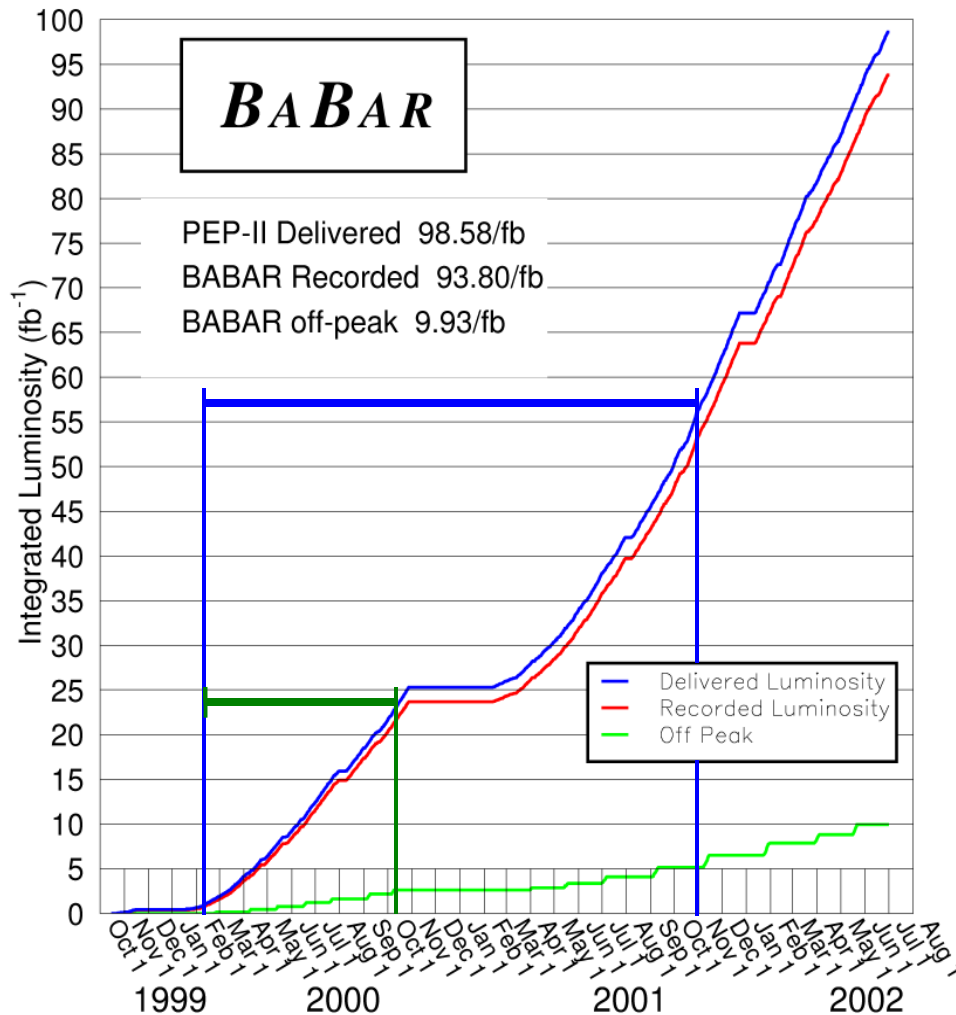
## ● Exclusive:

- reconstruct selected modes
- sensitive in larger lepton energy region, due to kinematical constraints
- need form-factors to describe the transition of the B meson to a light meson
- uncertainty of the form-factor normalization introduces large model dependency





# The *BABAR* Data Set



Data Sets used:

Inclusive Analysis:

$$L_{\text{on}} = 20.6 \text{ fb}^{-1}$$

$$L_{\text{off}} = 2.6 \text{ fb}^{-1}$$

$$N_{B\bar{B}} = 22.6 \times 10^6$$

Exclusive Analysis:

$$L_{\text{on}} = 50.5 \text{ fb}^{-1}$$

$$L_{\text{off}} = 8.7 \text{ fb}^{-1}$$

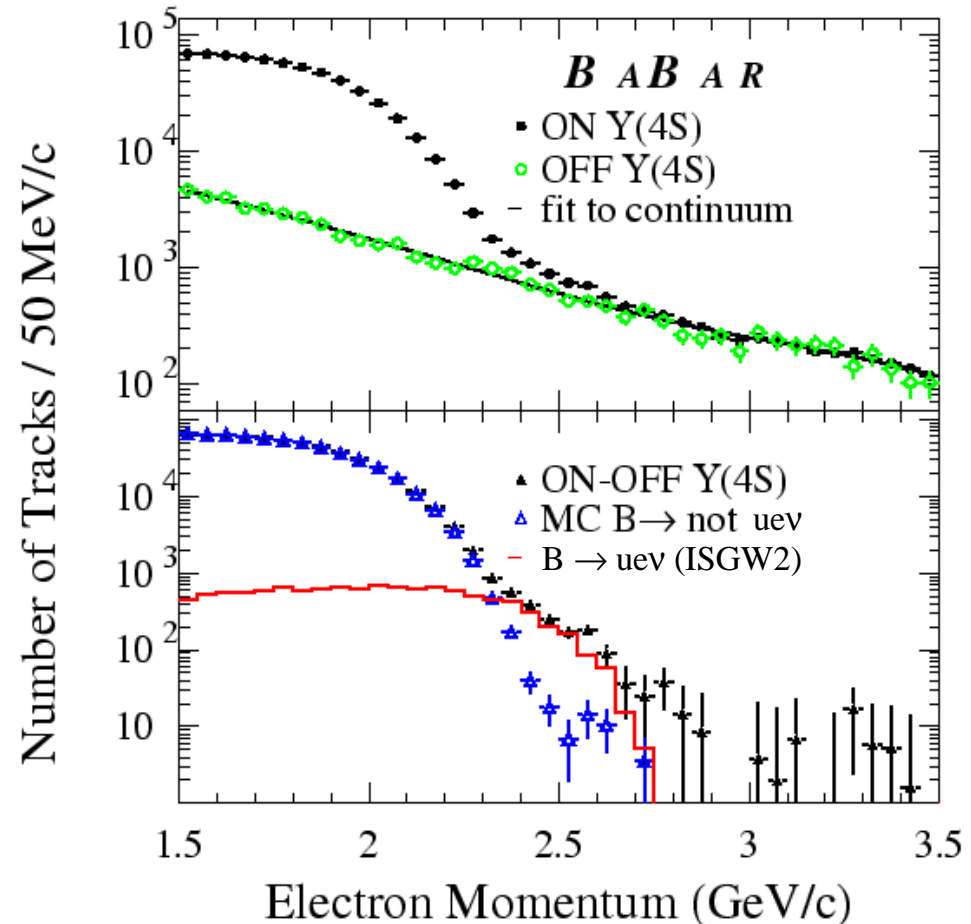
$$N_{B\bar{B}} = 55.2 \times 10^6$$



# Inclusive Analysis-Strategy $b \rightarrow u e \nu$

preliminary

- Measure  $b \rightarrow u e \nu$  rate in electron energy range 2.3 ... 2.6 GeV
- Estimate continuum background using 4<sup>th</sup> degree Chebyshev-polynomial fit to off-peak data
- Other backgrounds from MC:
  - $B \rightarrow X_c e \nu$
  - $J/\Psi \rightarrow e^+e^-$
  - $B \rightarrow X_c \rightarrow e$
  - mis-id hadrons from  $B \rightarrow X_c$
- Correct for final-state radiation and bremsstrahlung



$$\Delta B = \frac{N_{on} - N_{off} - N_{B \rightarrow ue\nu}}{2 \epsilon N_{B\bar{B}}} \cdot (1 + \delta_{rad}) = (0.152 \pm 0.014 \pm 0.014) \times 10^{-3}$$

stat                      syst



# Inclusive Estimation of $|V_{ub}|$

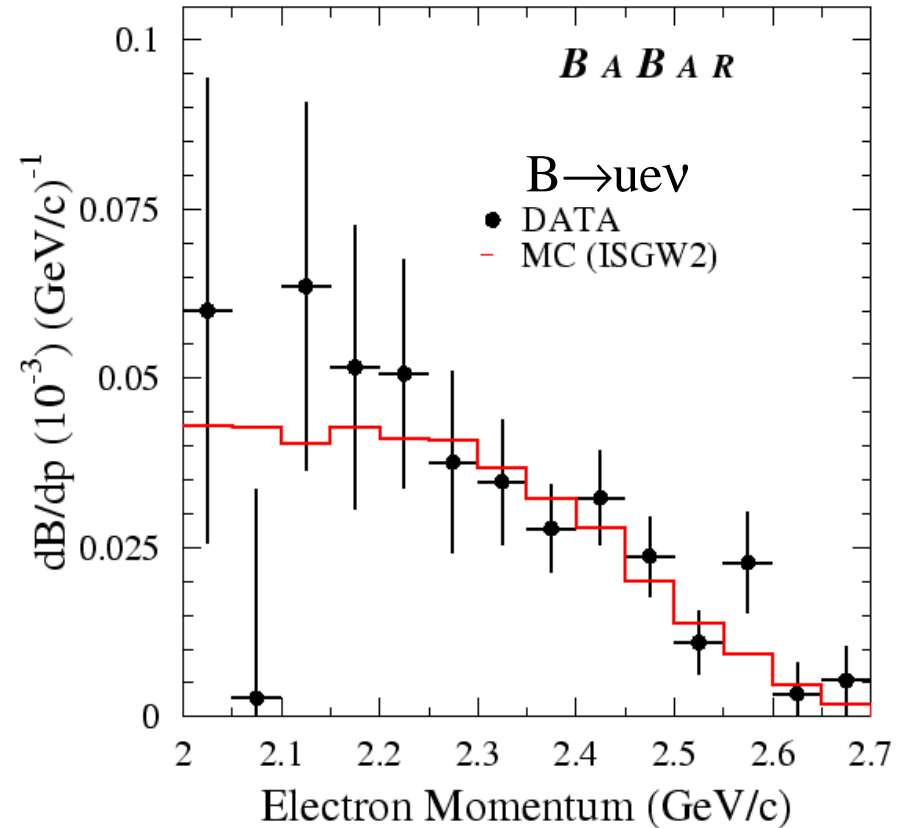
preliminary

## Systematic errors on partial rate:

- Detector simulation 5%
- Continuum subtraction 5%
- MC  $b \rightarrow c$  subtraction 3%
- Momentum spectrum of B mesons 5%

## Extrapolation to full rate:

- using input from CLEO's  $b \rightarrow s\gamma$  measurement ( $f_u = 0.074 \pm 0.014 \pm 0.009$ , fraction of events in  $2.3 < E_e < 2.6$  GeV):



$$B = (2.05 \pm 0.27_{\text{exp}} \pm 0.46_{fu}) \times 10^{-3}$$

$$|V_{ub}| = (4.43 \pm 0.29_{\text{exp}} \pm 0.25_{\text{OPE}} \pm 0.50_{fu} \pm 0.35_{sy}) \times 10^{-3}$$



## The Exclusive Analysis-Strategy $B \rightarrow \rho e \nu$

- Study 5 modes  $B \rightarrow H_u e \nu$ , where  $H_u = \rho^0, \rho^\pm, \omega, \pi^0, \pi^\pm$ , in 2 lepton-energy ranges:

**LOLEP** :  $2.0 < E_{\text{electron}} < 2.3 \text{ GeV}$  (large  $b \rightarrow c e \nu$  backgrounds)

**HILEP** :  $2.3 < E_{\text{electron}} < 2.7 \text{ GeV}$  (large continuum backgrounds)

- Binned Likelihood-Fit with 2 fit variables:

$\Delta E = E_{\text{had}} + E_{\text{lept}} + |p_\nu| - E_{\text{beam}}$ , where  $|p_\nu| \approx |p_{\text{miss}}|$ , and  $M_{\text{had}} = \pi\pi(\pi)$  mass

- Take signal and background shapes from Monte Carlo simulations, and continuum shape from off-peak data
- Extrapolate partial branching fraction to entire lepton-energy spectrum using five different form-factor calculations.

- Determine  $|V_{ub}|$  for each form-factor:

$$|V_{ub}| = \sqrt{\frac{B(B^0 \rightarrow \rho^+ e^- \nu)}{\Gamma_{\text{theo}} \tau_{B^0}}}$$



## Fitting for the $B \rightarrow \rho e \nu$ Branching Fraction

- **Extended binned maximum likelihood fit**
  - $M_{\text{had}}$  vs  $\Delta E$  (10x10 bins for  $\rho$ , 6x10 bins for  $\omega$ , 10 bins for  $\pi$ )
  - simultaneously for  $\rho^\pm, \rho^0, \omega, \pi^\pm, \pi^0$ , and in 2 lepton energy regions
  - use method by Barlow/Beeston (Comp. Phys. Com 77, 219-228) to take finite MC statistics into account
- **Make use of isospin and quark model relations:**
  - $\Gamma(B^0 \rightarrow \rho^- e^+ \nu) = 2 \Gamma(B^+ \rightarrow \rho^0 e^+ \nu)$
  - $\Gamma(B^0 \rightarrow \pi^- e^+ \nu) = 2 \Gamma(B^+ \rightarrow \pi^0 e^+ \nu)$
  - $\Gamma(B^+ \rightarrow \rho^0 e^+ \nu) = \Gamma(B^+ \rightarrow \omega e^+ \nu)$
- **9 parameter fit:**
  - **Par 1:**  $\mathcal{B}(B \rightarrow \rho / \omega e \nu)$
  - **Par 2:**  $\mathcal{B}(B \rightarrow \pi^0 / \pi^\pm e \nu)$
  - **Par 3+4:**  $b \rightarrow u$  downfeed (normalization in hilep/lolep)
  - **Par 5..9:**  $b \rightarrow c$  (normalization)





# Fit Projections for $B^0 \rightarrow \rho^- e^+ \nu$

- direct signal
- crossfeed signal
- other  $b \rightarrow ue\nu$
- $b \rightarrow ce\nu$

(isospin-constrained average of  $\rho^\pm$  and  $\rho^0$ )

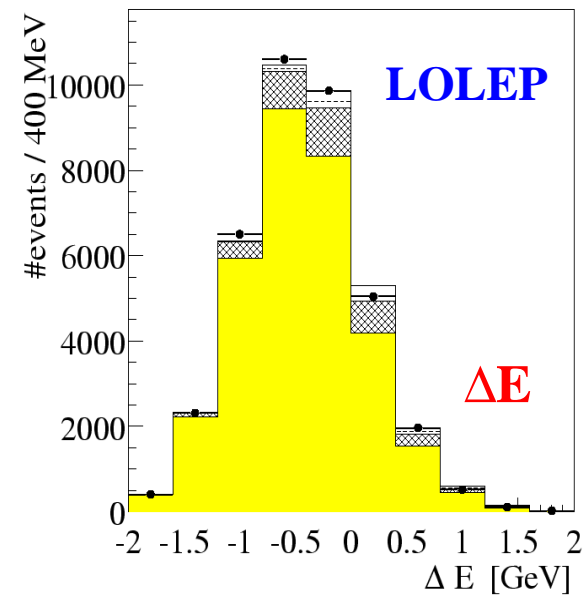
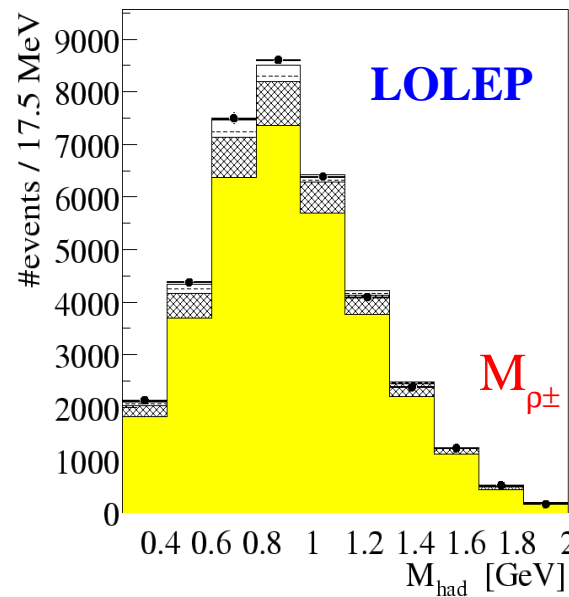
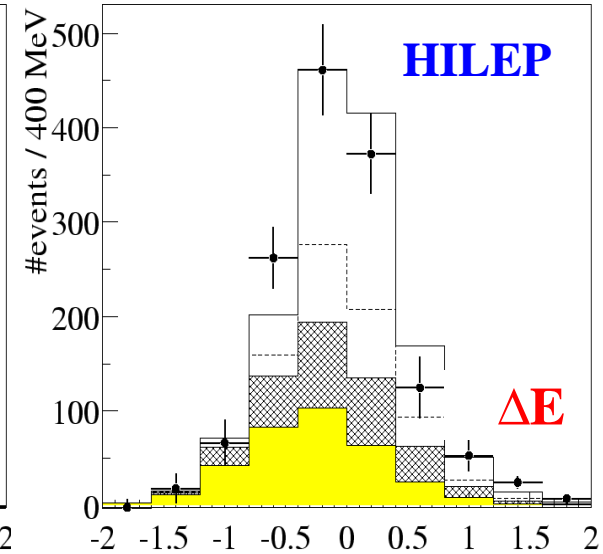
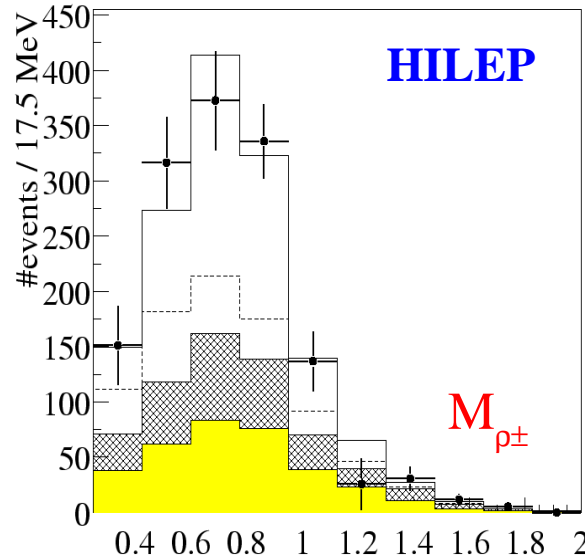
$\chi^2 = 91(93 \text{ Ndof}), P=52\%$

**Direct signal yields**

**HILEP (2.3 - 2.7 GeV):**

**$510 \pm 62$**   $B^0 \rightarrow \rho^- e^+ \nu + \text{CC}$

**$324 \pm 40$**   $B^+ \rightarrow \rho^0 e^+ \nu + \text{CC}$





## Summary of Systematic Errors on $\text{Br}(B \rightarrow \rho e \nu)$

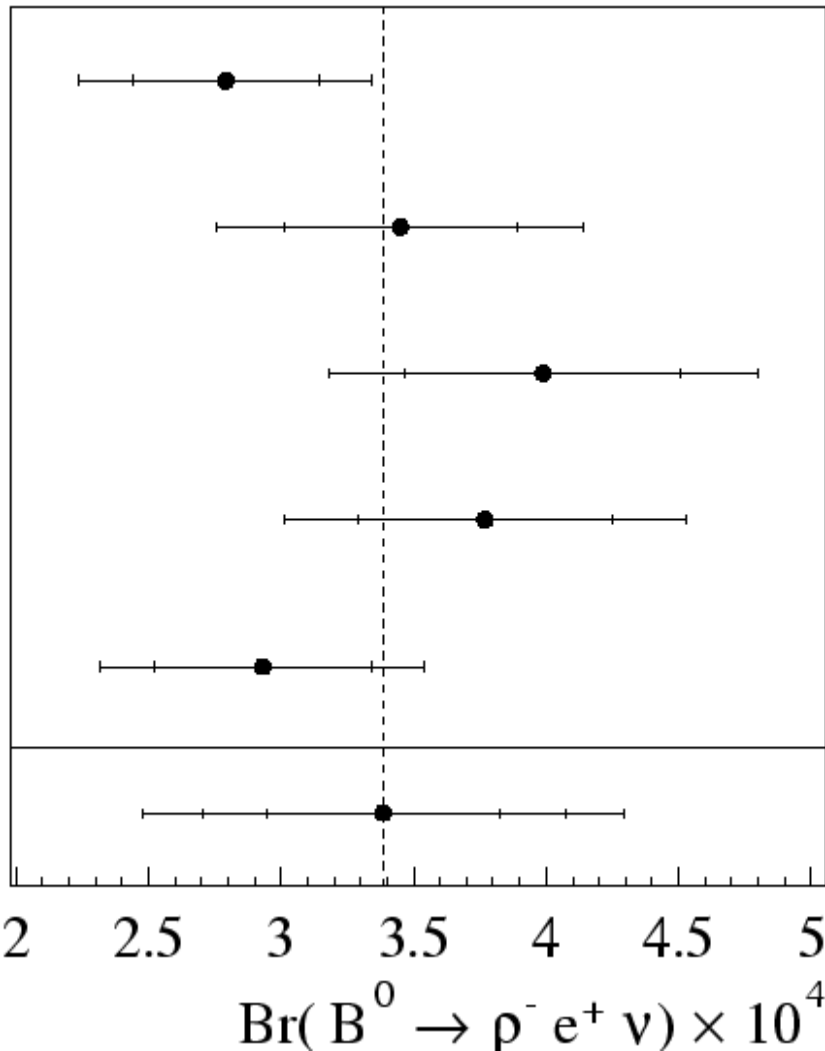
● track efficiency	$\pm 5 \%$	Detector Simulation
● track resolution / track smearing	$\pm 1 \%$	
● photon/ $\pi^0$ efficiency	$\pm 5 \%$	
● photon/ $\pi^0$ energy scale	$\pm 3 \%$	
● electron id	$\pm 2 \%$	
● fake lepton rate (electrons)	$\pm 1 \%$	
● resonant $b \rightarrow u$ downfeed composition (ISGW2)	$+6, -4 \%$	Background Modeling $+11, -10 \%$
● non-resonant $b \rightarrow u$ downfeed (Neubert & Fazio)	$\pm 9 \%$	
● $b \rightarrow c$ composition	$+1.4, -1.7 \%$	Others $\pm 9 \%$
● B counting	$\pm 1.6 \%$	
● B lifetime	$\pm 1.5 \%$	
● $f_{+}/f_{00}$	$\pm 1 \%$	
● isospin breaking	$\pm 0 \%$	
● fit method	$+4, -6 \%$	
● data selection	$\pm 6 \%$	

**TOTAL:  $\pm 15.5 \%$**



# $B^0 \rightarrow \rho^- e^+ \nu$ Branching Fraction Results

preliminary



ISGW2:  
 $2.79 \pm 0.35 \pm 0.43$

UKQCD:  
 $3.45 \pm 0.44 \pm 0.53$

LCSR:  
 $3.99 \pm 0.52 \pm 0.62$

Beyer/Melikhov:  
 $3.77 \pm 0.48 \pm 0.58$

Ligeti/Wise:  
 $2.93 \pm 0.41 \pm 0.45$

Theoretical error on the combined result:

Half of the full spread seen between the different form-factors.

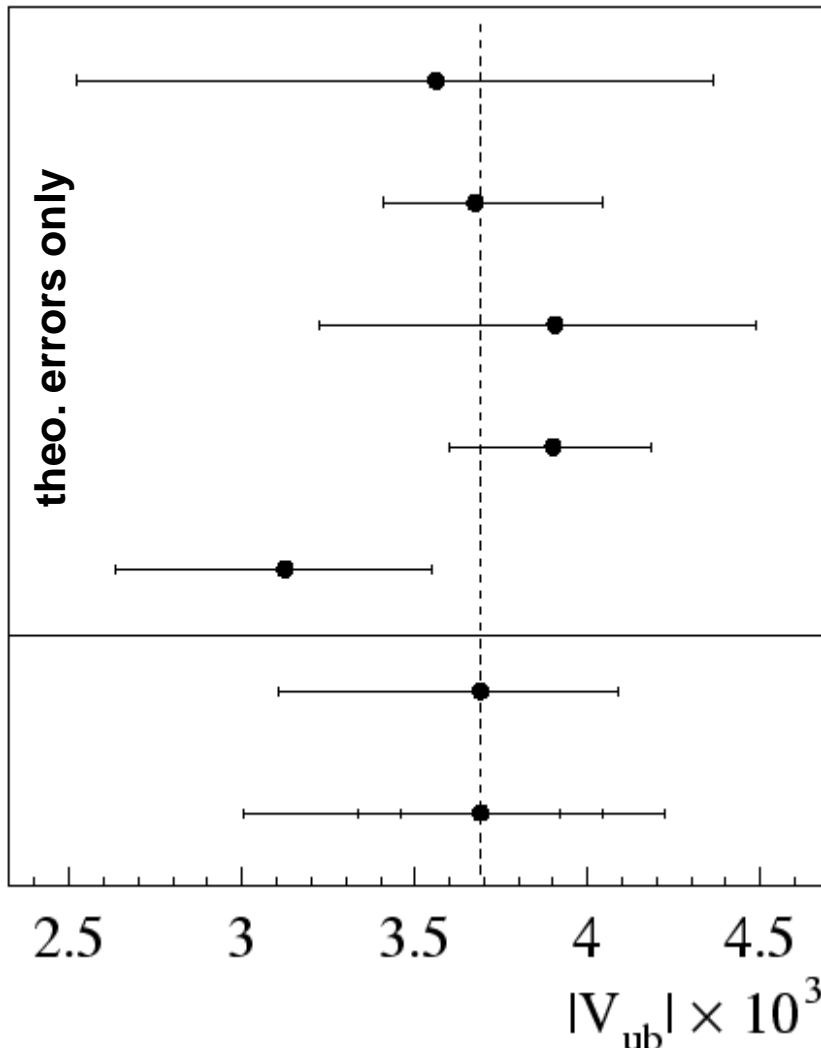
## Combined Result:

$$(3.39 \pm 0.44 \pm 0.52 \pm 0.60) \times 10^{-4}$$



# Exclusive $|V_{ub}|$ Results

preliminary



ISGW2:  
 $3.56 \pm 0.22 \pm 0.27$   $^{+0.80}_{-1.04}$

UKQCD:  
 $3.68 \pm 0.23 \pm 0.27$   $^{+0.37}_{-0.27}$

LCSR:  
 $3.91 \pm 0.25 \pm 0.29$   $^{+0.58}_{-0.68}$

Beyer/Melikhov:  
 $3.90 \pm 0.24 \pm 0.29$   $^{+0.28}_{-0.30}$

Ligeti/Wise:  
 $3.12 \pm 0.21 \pm 0.23$   $^{+0.42}_{-0.49}$

Combined

$$|V_{ub}| = \sqrt{\frac{B(B^0 \rightarrow \rho^+ e^- \nu)}{\Gamma_{theo} \tau_{B^0}}}$$

Quoted errors on  $\Gamma_{theo}$  vary from 15% to 50%.

Combined result:  
**weighted average of 5 form-factor results**

Theoretical error on the combined result:  
**Half of the full spread seen between the FFs (including theoretical errors)**

**Combined Result:**

$$|V_{ub}| = (3.69 \pm 0.23 \pm 0.27^{+0.40}_{-0.59}) \times 10^{-3}$$



## Conclusions & Outlook

*BABAR* measurements of the **inclusive  $b \rightarrow u e \nu$  rate** and the **branching fraction  $B \rightarrow \rho e \nu$**  were presented. The matrix element  $|V_{ub}|$  can be derived from both measurements.

There is room for improvement in the future, both on the experimental and theoretical side, e.g.:

### Inclusive Analysis:

- Perform *BABAR* combined measurement of  $b \rightarrow u l \nu$  and  $b \rightarrow s \gamma$ .
- Make use of fully reconstructed B-Mesons on the tagging side.

### Exclusive Analysis:

- Gain better understanding of the downfeed background.
- Improve neutrino momentum resolution, include larger fraction of the electron energy spectrum
- Hope for progress in form-factor lattice-QCD calculations



## Inclusive Event Selection

*Backup Slide*

- require more than 3 tracks
- 2<sup>nd</sup> normalized Fox Wolfram Moment  $R_2 < 0.4$
- CMS missing momentum  $> 1 \text{ GeV}/c$
- $-0.9 < \cos \theta_{\text{miss}} < 0.8$ , where  $\theta$  = polar angle of missing momentum
- $\cos \theta_{\text{l-miss}} < 0$ , where  $\theta_{\text{l-miss}}$  = angle between electron and missing momentum
- Electron Selection:
  - select electron of highest momentum
  - cut based selector using information from drift chamber, calorimeter and chrenkov detector.
  - determine efficiency and fake rate from pure data control samples
  - veto electrons from  $J/\Psi$ -mesons:  $M_{ee} < 3.05$  or  $M_{ee} > 3.15$
- Selection Efficiency for  $2.3 < p_{\text{CMS}} < 2.6 \text{ GeV}$  : 27.7 %



# Comparison with Other Measurements *Backup Slide*

## Inclusive Results:

Experiment	$ V_{ub}  \times 10^3$	$b \rightarrow u$ rate $\times 10^3$
<b>BABAR</b>	$4.43 \pm 0.29 \pm 0.25 \pm 0.50 \pm 0.35$ Stat. OPE, $f_u$ $s\gamma$ Syst. b-mass	$2.05 \pm 0.27 \pm 0.46$ Stat. $f_u$ Syst.
<b>CLEO</b>	$4.08 \pm 0.34 \pm 0.44 \pm 0.28$ Stat. OPE, $f_u$ Syst. b-mass	$1.77 \pm 0.29 \pm 0.38$ Stat. $f_u$ Syst.
<b>LEP average</b>	$4.09^{+0.36}_{-0.39} \pm 0.42 \pm 0.24 \pm 0.21$ Stat. b $\rightarrow$ c b $\rightarrow$ u HQE Syst.	$1.71 \pm 0.31 \pm 0.37 \pm 0.21$ Stat. b $\rightarrow$ c b $\rightarrow$ u Syst.

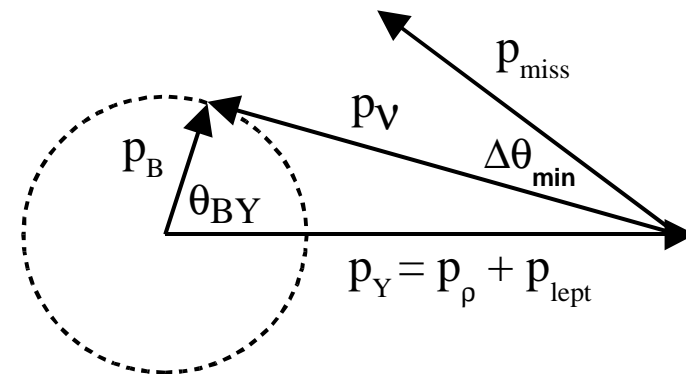


- **Multihadron selection**
  - Normalized Fox Wolfram Moment  $R_2 < 0.9$
  - $N_{\text{tracks}} > 4 \parallel ( N_{\text{tracks}} > 3 \ \&\& \ N_{\text{clusters}} > 5 )$
- **Electron ID**
  - likelihood based electron selector using information from calorimeter, driftchamber, and cherenkov detector.
  - input: well reconstructed tracks within calorimeter acceptance
- **Suppression of other backgrounds**
  - lepton must not be compatible with a  **$J/\psi$  decay**:  
 $3 < M_{J/\psi} < 3.14 \text{ GeV}$   
MC: Rejects 76% of all selected electrons from true  $J/\psi$ s.
  - electrons must not be compatible with a photon conversion.  
MC: Rejects 38% of all selected electrons from true conversions.





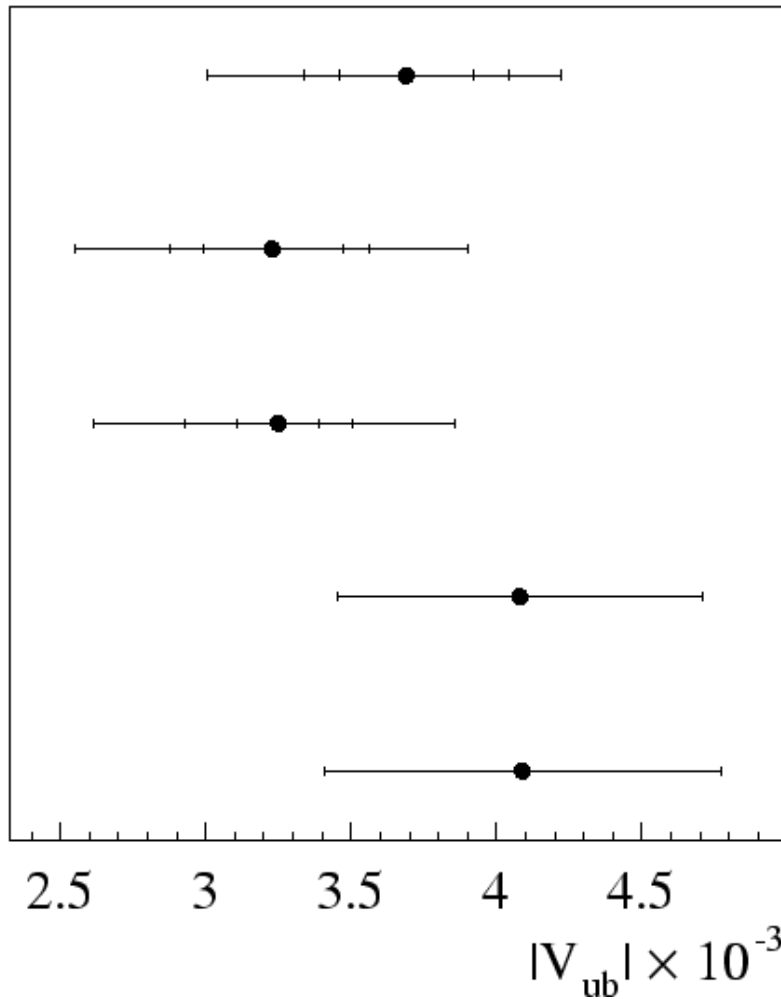
- **Hadron reconstruction**
  - Input: well reconstructed tracks
  - reject track identified as kaon
  - $\pi^0$  candidates:  $120 < m_{\pi^0} < 145$  MeV
  - $\max(p_{\pi_1}, p_{\pi_2}) > 400$  MeV, other  $p_{\pi} > 200$  MeV
- **Consistency requirement**
  - $|\cos \theta_{BY}| < 1.1$ , rejects 60% of bad combinations without losing signal
  - $\cos \Delta\theta_{\min} > 0.8$
- **Continuum suppression**
  - $R_2 < 0.4$  ( $R_2$  with tracks and clusters)
  - $|\cos(\theta_{\text{miss}})| < 0.9$
  - neural network with 14 input variables



$$\cos \Theta_{BY} = \frac{2E_B E_Y - m_B^2 - m_Y^2}{2|p_B| \cdot |p_Y|}$$



# Comparison with Other Measurements *Backup Slide*



BABAR exclusive:  
 $3.69 \pm 0.23 \pm 0.27$   $^{+0.40}_{-0.59}$   
preliminary

CLEO exclusive I  
 $3.23 \pm 0.24$   $^{+0.23}_{-0.26} \pm 0.58$

CLEO exclusive II  
 $3.25 \pm 0.14$   $^{+0.21}_{-0.29} \pm 0.55$

CLEO inclusive:  
 $4.08 \pm 0.63$  (stat+syst+theo)

LEP inclusive:  
 $4.09 \pm 0.68$  (stat+syst+theo)

**Similar analysis  
strategy, sensitive  
to  $\rho$  channels**

**average of 2 CLEO  
measurements**



# Form Factor Models Overview

*Backup Slide*

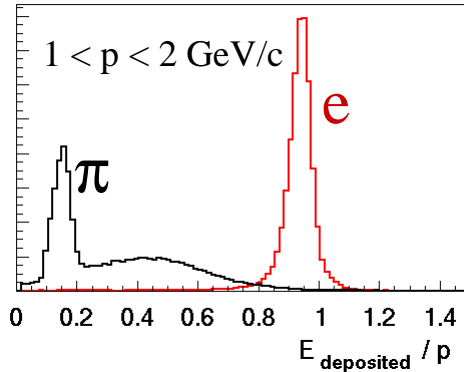
<b>ISGW2</b>	Isgur, Scora, Grinstein, Wise normalized at $q^2=q_{\max}^2$	<b>constituent quark model</b>
<b>UKQCD</b>	UKQCD group 24 <sup>3</sup> x48 lattice, quenched calculations at $q^2=q_{\max}^2$ use of HQS and LCSRs to cover entire $q^2$ range	<b>lattice QCD calculation</b>
<b>LCSR</b>	Ball, Braun normalized at small $q^2$ , complementary to UKQCD, use of LCSRs	<b>light cone sum rules</b>
<b>B/M</b>	Beyer, Melikhov fully relativistic UKQCD results used for normalization at $q_{\max}^2$	<b>constituent quark model</b>
<b>L/W</b>	Ligeti, Wise relates semileptonic B and D decays uses input for $D \rightarrow K^* l \nu$ from E791 measurements	<b>SU(3) flavour symmetry, SU(4) HQ spin-flavour symmetry</b>



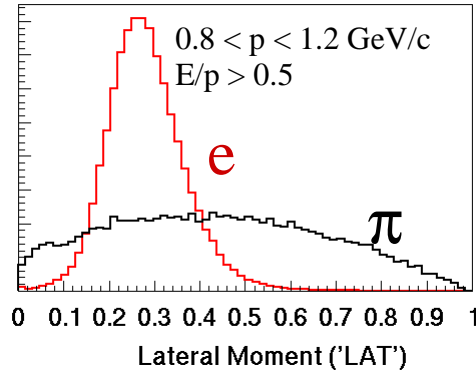
# The BABAR Detector

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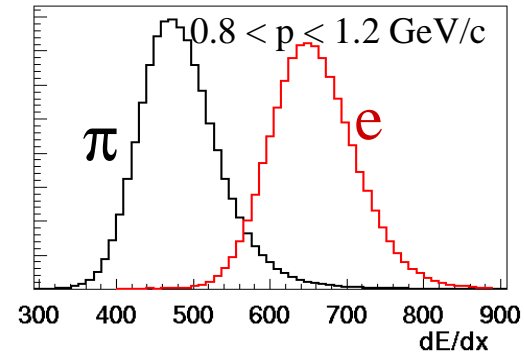
## $E/p$ E.M. calorimeter



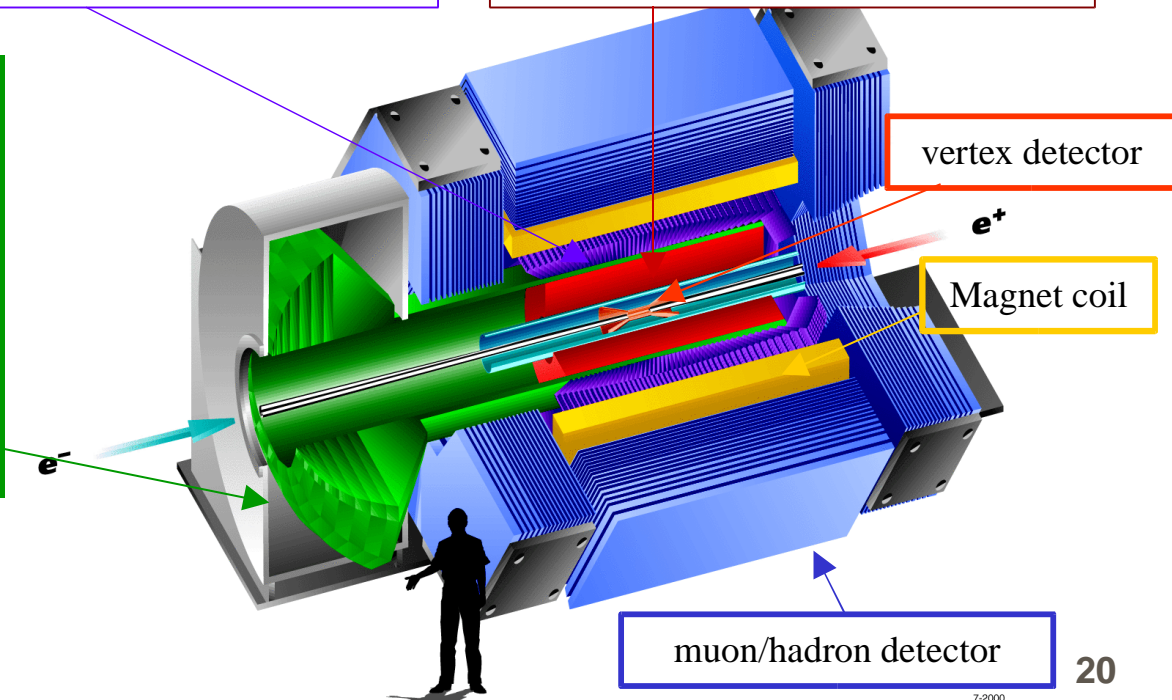
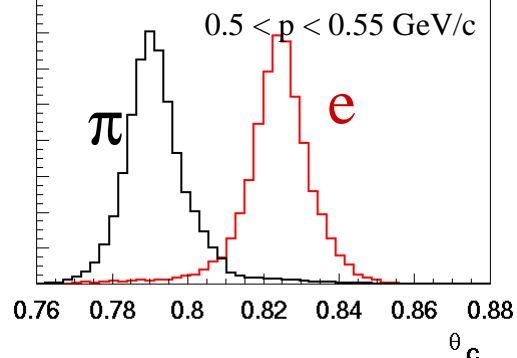
## shower shape



## $DE/dx$ driftchamber



## $\theta_c$ Cherenkov detector



## Electron Identification

07/19/02

7-2000  
8558A1