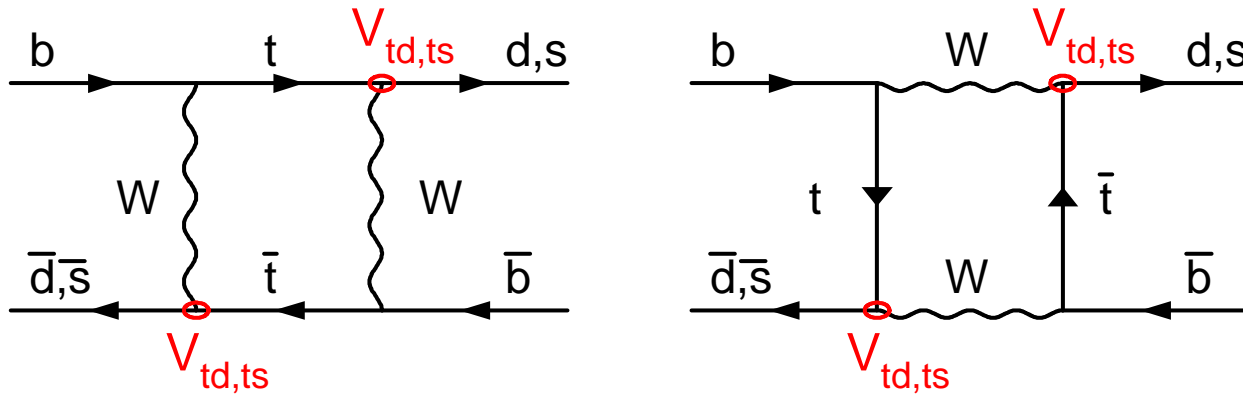


B_s Oscillation Results



Abstracts: 242 (OPAL), 250 (ALEPH), 478 (SLD), 587 (DELPHI)
new new new

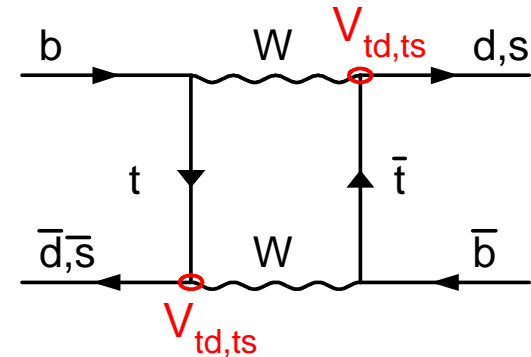
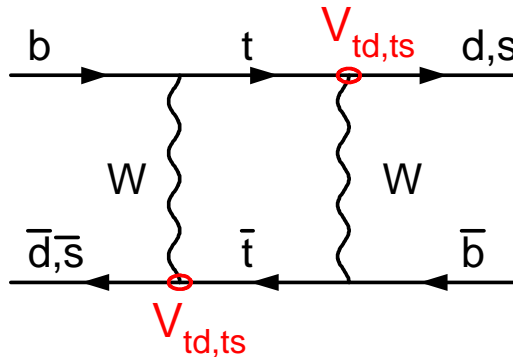
Stéphane Willocq
University of Massachusetts, Amherst

31st International Conference on High Energy Physics
Amsterdam
24-31 July 2002

Special thanks to D.Abbaneo, F.Parodi, O.Schneider, A.Stocchi

B⁰ – B̄⁰ System (I)

- B⁰ ↔ B̄⁰ transitions occur via second order weak interactions



- B_d⁰ mixing frequency:

$$\Delta m_d = \frac{G_F^2}{6\pi^2} m_{B_d} m_t^2 F\left(\frac{m_t^2}{m_W^2}\right) B_{B_d} f_{B_d}^2 \eta_{QCD} |V_{tb}^* V_{td}|^2 = 0.503 \pm 0.006 \text{ ps}^{-1}$$

World average July 2002

But extraction of |V_{td}| from Δm_d is affected by a 15 to 20% uncertainty

mostly due to theoretical uncertainty in $\sqrt{B_{B_d} f_{B_d}}$

→ reduced theoretical uncertainties and **most precise determination of |V_{td}|**

obtained by measuring Δm_s / Δm_d

$$\frac{\Delta m_s}{\Delta m_d} = \frac{m_{B_s} f_{B_s}^2 B_{B_s}}{m_{B_d} f_{B_d}^2 B_{B_d}} \cdot \left| \frac{V_{ts}}{V_{td}} \right|^2 = \frac{m_{B_s}}{m_{B_d}} \cdot (1.16 \pm 0.05)^2 \cdot \left| \frac{V_{ts}}{V_{td}} \right|^2 = (1.32 \pm 0.10)^2$$

S.Aoki BCP4

A.Kronfeld & S.Ryan

$B^0 - \bar{B}^0$ System (II)

Wolfenstein parameterization of the CKM weak quark mixing matrix

$$\begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} = \begin{pmatrix} 1 - \frac{1}{2}\lambda^2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \frac{1}{2}\lambda^2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} + O(\lambda^4)$$

Measurements of the oscillations frequencies impose significant constraints on (ρ, η) = apex of unitarity triangle

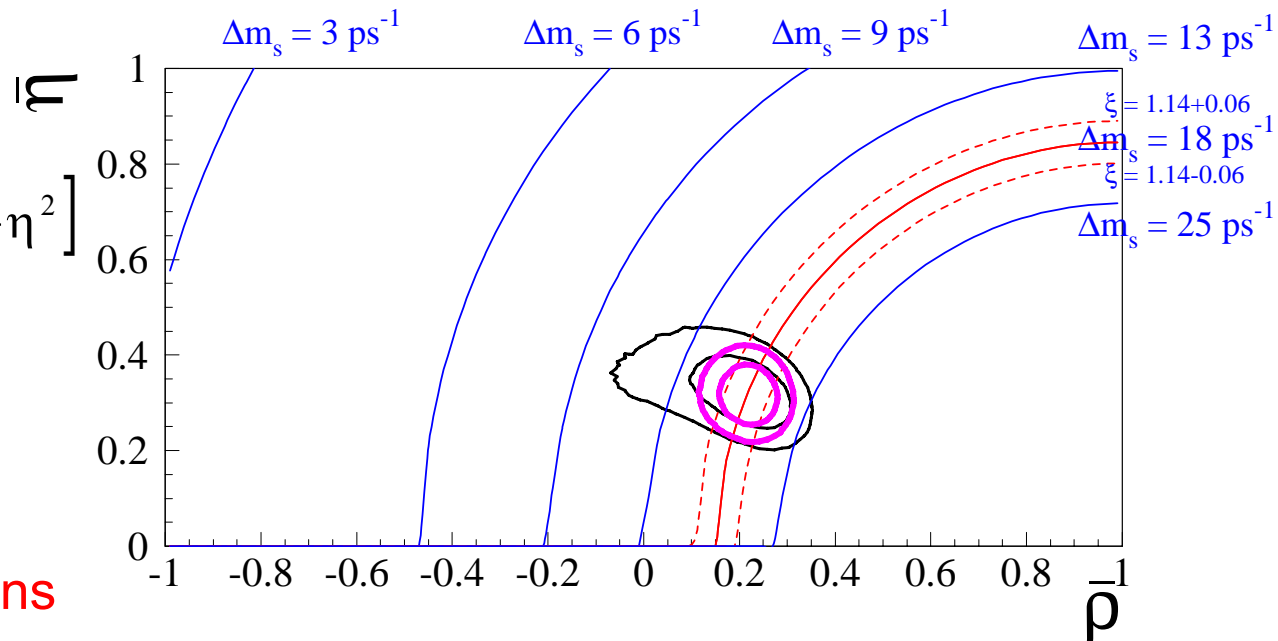
Lower limit on $\Delta m_s \rightarrow$ upper limit on $|V_{td}|$

$$\Delta m_s \propto |V_{ts}|^2 = A^2 \lambda^4$$

$$\Delta m_d \propto |V_{td}|^2 = A^2 \lambda^6 \left[(1 - \rho)^2 + \eta^2 \right]$$

$$\Rightarrow \frac{\Delta m_s}{\Delta m_d} \approx O\left(\frac{1}{\lambda^2}\right) = 20$$

\rightarrow fast B_s oscillations



Mixing Ingredients (I)

1. Reconstruct B decay vtx & proper time
2. Tag B⁰ or B⁰ flavor at production
3. Tag B⁰ or B⁰ flavor at decay

Significance of B_s mixing signal:

$$S = \sqrt{\frac{N}{2}} f_{B_s} (1 - 2w) e^{-\frac{1}{2}(\Delta m_s \sigma_t)^2}$$

statistics B_s purity mistag resolution

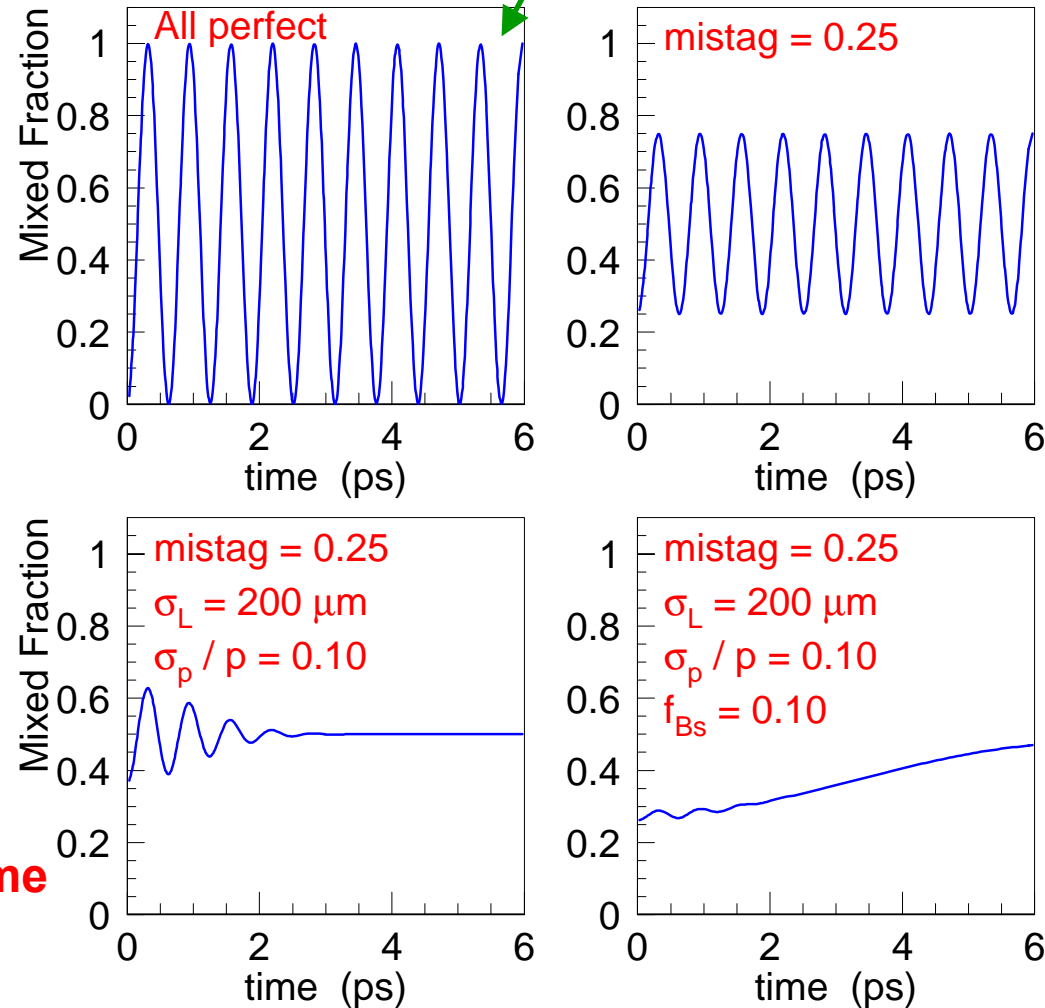
$$\sigma_t^2 = \left(\frac{\sigma_L m_B}{p} \right)^2 + \left(\frac{\sigma_p}{p} t \right)^2$$

⇒ **σ_t significantly increases with time for most analyses**

(except for exclusive reco analyses that have small enough σ_p / p)

$$\Delta m_s = 10 \text{ ps}^{-1}$$

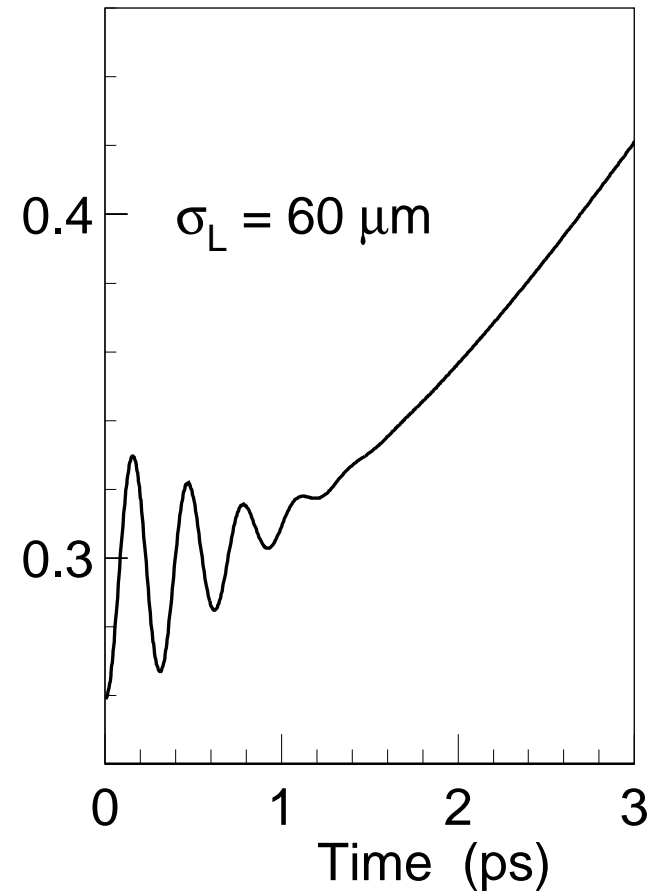
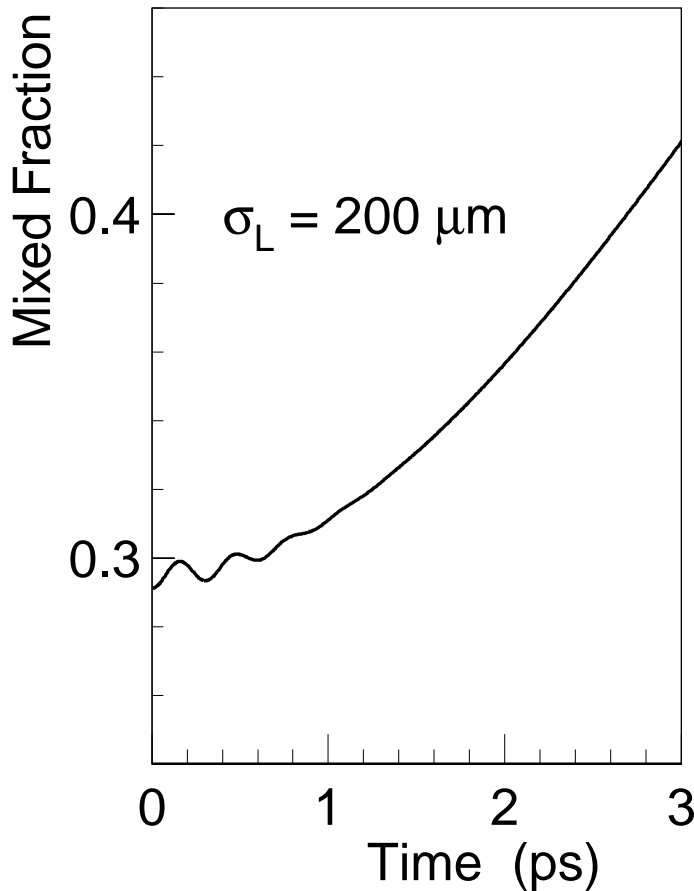
Mixed Fraction = N_{mixed} / (N_{mixed} + N_{unmixed})



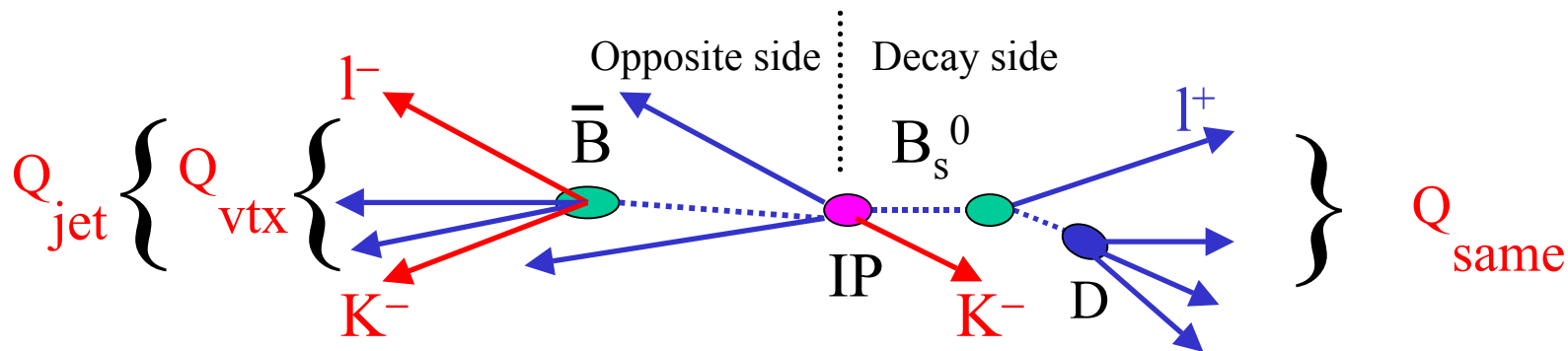
Mixing Ingredients (II)

Need excellent decay length resolution to detect high-frequency oscillations

Example: B_s mixing with $\Delta m_s = 20 \text{ ps}^{-1}$, $w = 0.25$, $\sigma_p / p = 0.10$, $f_{B_s} = 0.18$



Initial State (Production) Tagging (I)



❖ Polarized Forward-Backward Asymmetry (SLD only)

Left- (right-) polarized e^- tags forward hemisphere quark as b (\bar{b})

❖ Opposite Side Tags

Lepton charge $b \rightarrow l^-$

Kaon charge $b \rightarrow c \rightarrow s$ (i.e. K^-)

Avg mistag rates $w \approx 0.28$ (LEP)

Jet Charge $\sum_{\text{tracks}} Q_i |\mathbf{p}_i \cdot \mathbf{T}|^k$

0.22 (SLD)

Secondary vtx charge Q_{vtx}

❖ Same Side Tags

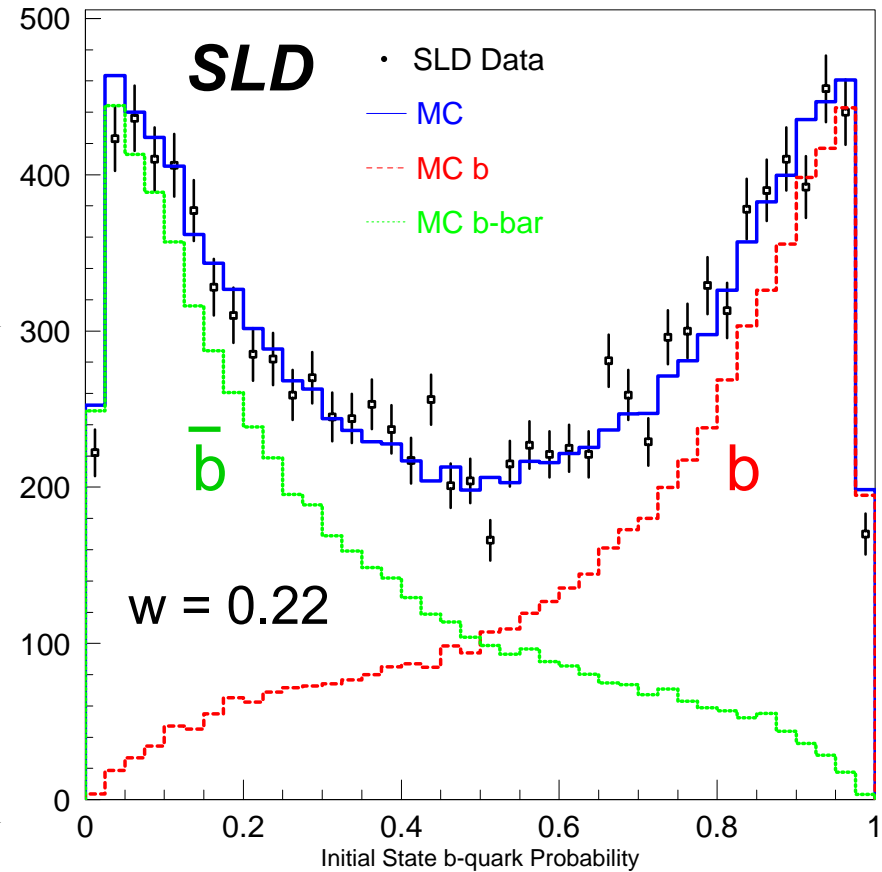
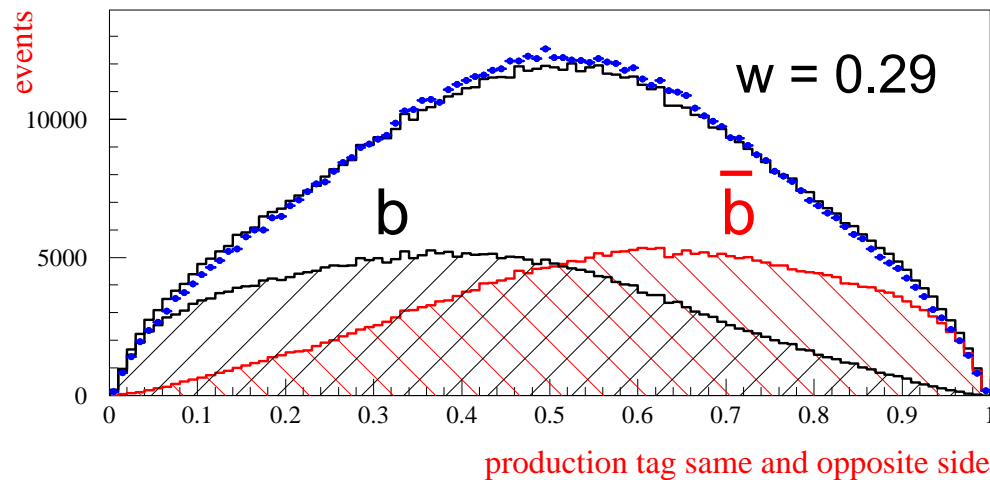
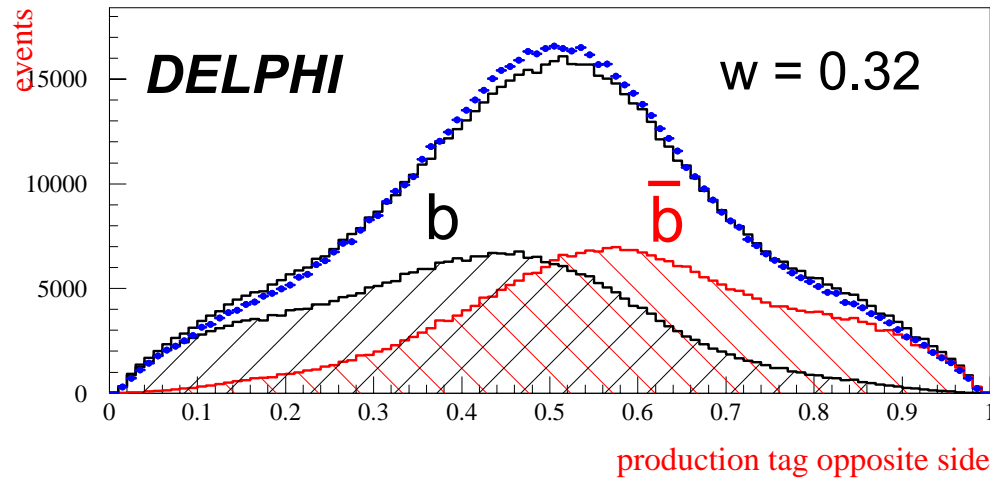
Jet Charge

Fragmentation kaon: $B_s(\bar{b} s)$ produced with accompanying $K^-(\bar{s} u)$

→ Tags combined in most analyses + event-by-event mistag probabilities

Initial State (Production) Tagging (II)

1992-2000 data



b-quark probability

Reconstruction Methods

→ Reconstruct B decay to determine proper time and B^0 / \bar{B}^0 decay flavor

Efficiency ↑

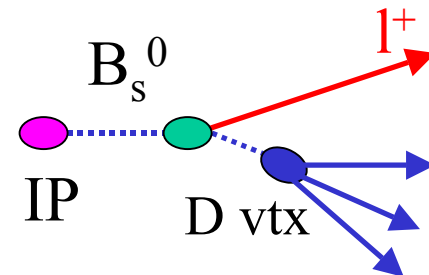
1) Inclusive

Fully inclusive: reconstruct $B_s \rightarrow D_s^- X$ cascade structure

DELPHI, SLD

Semileptonic decays: lepton + topological D vtx

ALEPH, DELPHI, OPAL, SLD

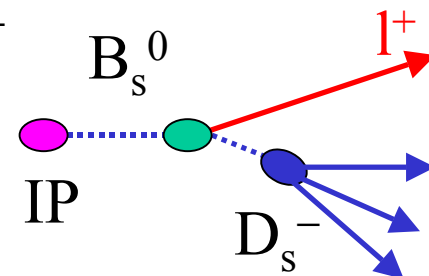


2) Semi-exclusive

Partial reconstruction: $B_s \rightarrow D_s^- l^+$ or $B_s \rightarrow D_s^- (\text{hadrons})^+$
with full or partial reconstruction of D_s decay

$D_s^- \rightarrow \phi\pi^-, K^{*0}K^-, K^0K^-, \dots$ ALEPH, DELPHI, OPAL, SLD

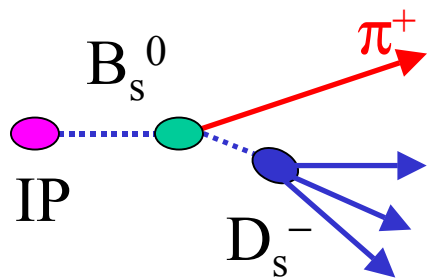
$D_s^- \rightarrow \phi h^- X$ CDF



3) Exclusive

Full reconstruction: $B_s \rightarrow D_s^- h^+, \bar{D}^0 K^- h^+$ ($h = \pi, \rho, a_1$)
with fully reconstructed D_s and \bar{D}^0 decays

ALEPH, DELPHI



Purity ↓

→ Total of 13 different analyses (8 updated since Feb. 2002)

Inclusive Methods (I)

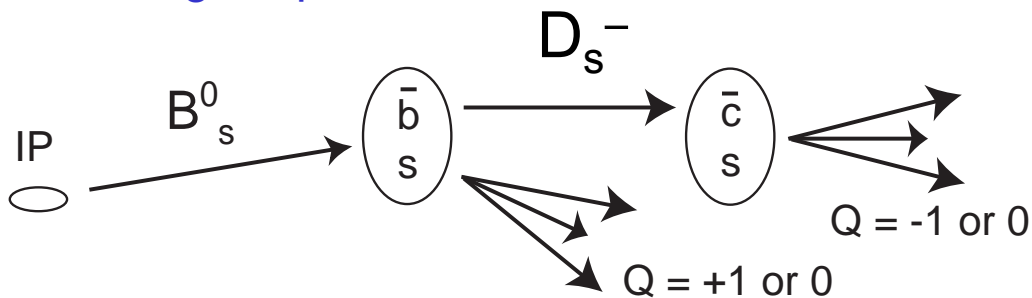
- **Fully Inclusive Analyses** DELPHI, SLD

SLD Charge Dipole (400 K Z^0)

CCD Pixel Vertex Detector

⇒ superb decay length resolution

Charge Dipole:



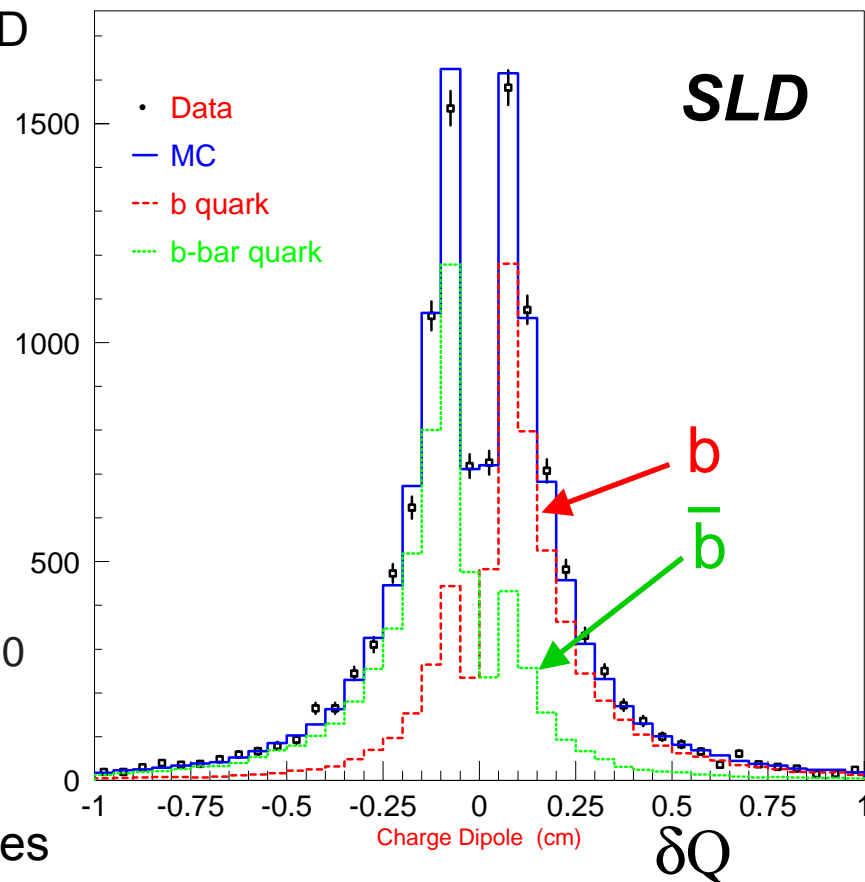
Reconstruct both secondary and tertiary vertices

Tag flavor with $\delta Q = (Q_D - Q_B) * \text{Distance}_{B \text{ to } D}$

Decay flavor mistag = 0.22 overall

= 0.10 for $B_s \rightarrow \text{single } D_s X$

= 0.46 for $B_s \rightarrow D_s D X$



11,462 selected decays

$f_{B_s} = 0.16$

$\sigma_L = 78 \mu\text{m}$ (60%) & $304 \mu\text{m}$ (40%)

Inclusive Methods (II)

DELPHI inclusive analysis (4 M Z^0)

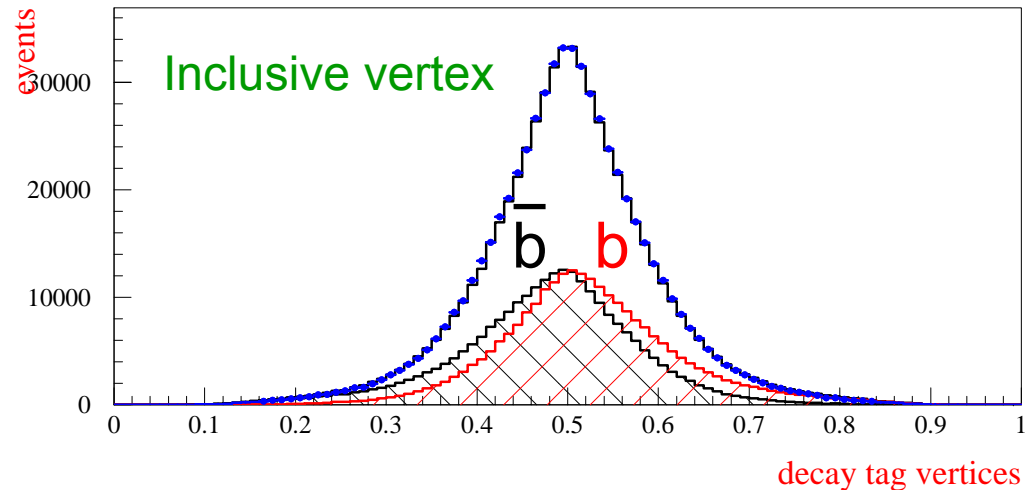
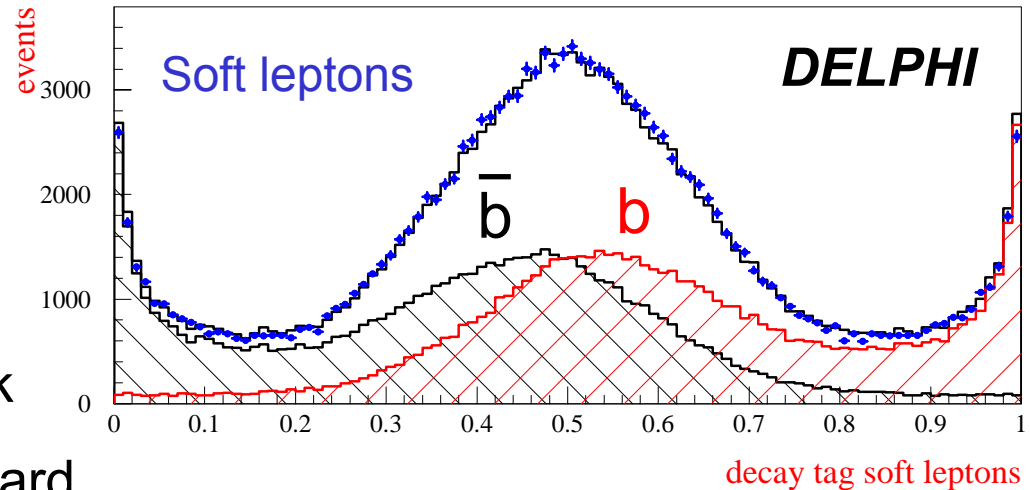
155,023 soft lepton events

Q_{lepton} for decay flavor tag with
mistag probability $w = 0.31$

614,577 inclusive vertex events

“Dipole charge” formed from track
information in forward and backward
hemispheres of the B rest frame
 \Rightarrow decay flavor tag with $w = 0.42$
(mistag increases slightly after calibration
from data)

1992-2000 data



Inclusive Methods (III)

- Inclusive Lepton Analyses ALEPH, DELPHI, OPAL, SLD

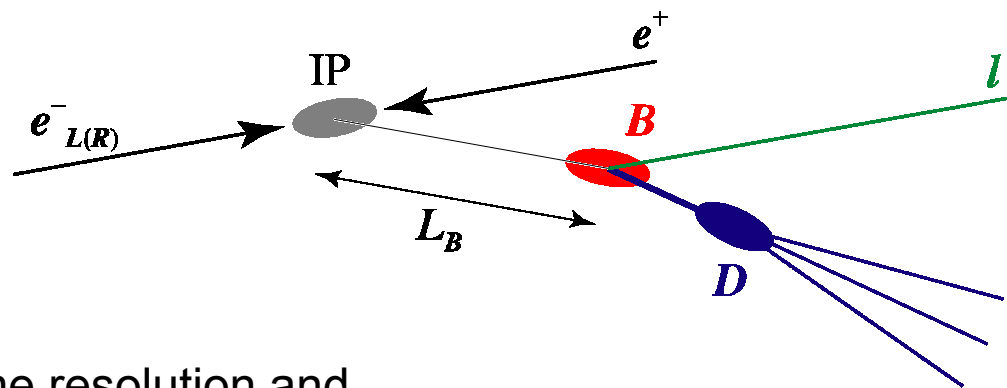
Select high- p_T lepton to suppress ($b \rightarrow c \rightarrow l^+$)

→ lepton charge tags decay flavor ($b \rightarrow l^-$) with mistag as low as $w = 0.04$ (SLD)

Reconstruct D meson inclusively (decay vertex topology & kinematical info)

→ B vtx = intersection of lepton trajectory and D vtx “track”

vertexing also includes “B track” formed with particles in jet



Pros: large statistics

Cons: worse proper time resolution and
lower B_s purity than more exclusive methods

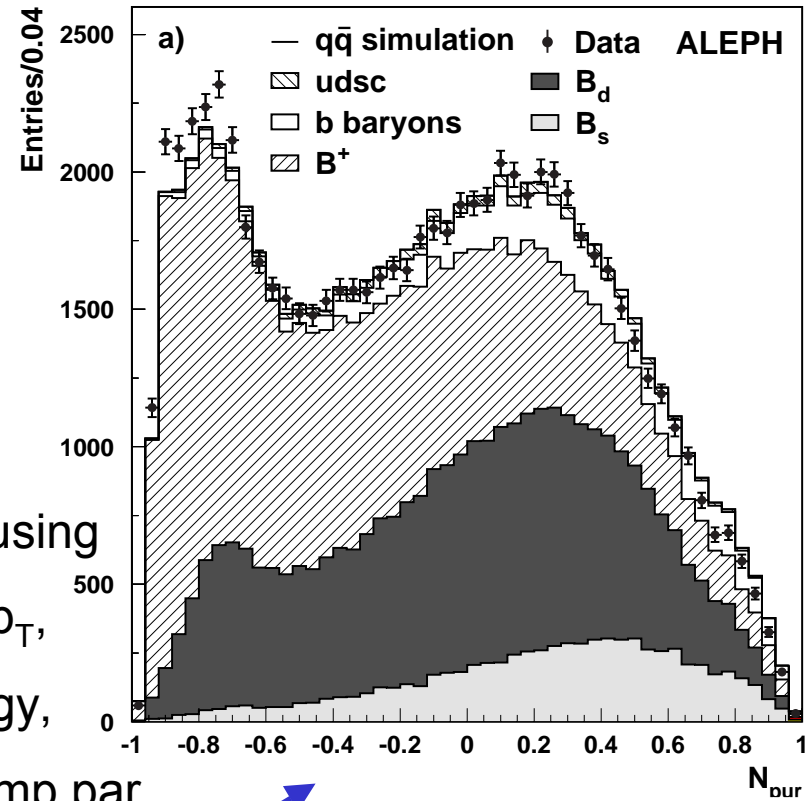
⇒ Include variables sensitive to proper time resolution, mistag probabilities
and B_s purity on an event-by-event basis

Inclusive Methods (IV)

- ALEPH Inclusive Lepton (4M Z^0)**

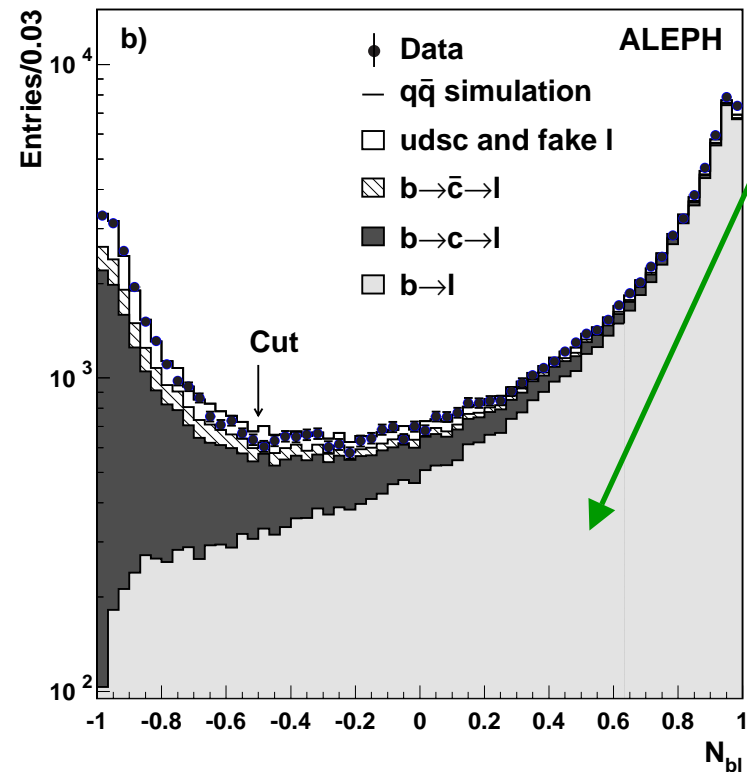
Most sensitive B_s mixing analysis: 74026 events

Avoid hard cuts and incorporate information on an evt-by-evt basis for **mistag probability**, B_s **purity** and proper time resolution



NN for $b \rightarrow l$ using lepton p and p_T , E_v , jet topology, lepton-D vtx imp.par.

B_s purity determined with NN using Q_{tot} , # D vtx trks, $\#(K^0 + K^+)$ from fragmentation and D vtx, $Q_{lepton} * Q_{kaon}$



Amplitude Fit Method

- Time-dependent mixing generates periodic signal

⇒ ideally suited for Fourier Analysis pioneered by ALEPH NIM A384, 491 (1997)

⇒ measure oscillation amplitude **A** at fixed frequency Δm_s

$$\text{Prob}(B_s^0 \rightarrow B_s^0) = \frac{1}{2} \Gamma e^{-\Gamma t} (1 + A \cos \Delta m_s t)$$

$$\text{Prob}(B_s^0 \rightarrow \bar{B}_s^0) = \frac{1}{2} \Gamma e^{-\Gamma t} (1 - A \cos \Delta m_s t)$$

MC generated with $\Delta m_s = 14 \text{ ps}^{-1}$

Expect **A = 1** for frequency = true Δm_s

A = 0 for frequency \neq true Δm_s

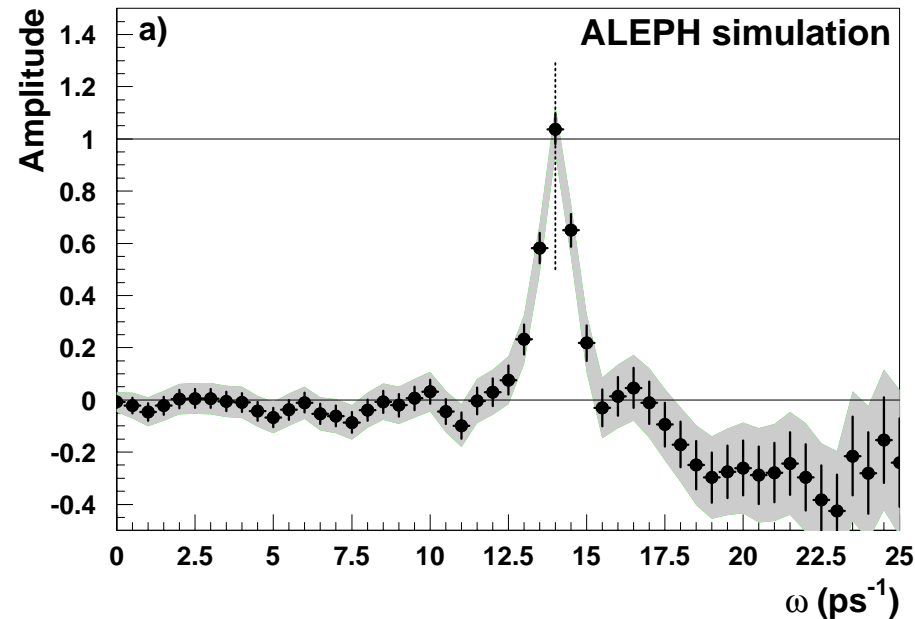
95% C.L. limit:

Δm_s values for which $A + 1.645 \sigma_A < 1$

Sensitivity:

Δm_s value for which $1.645 \sigma_A = 1$

→ σ_A increases with Δm_s due to limited proper time resolution



Inclusive Methods (V)

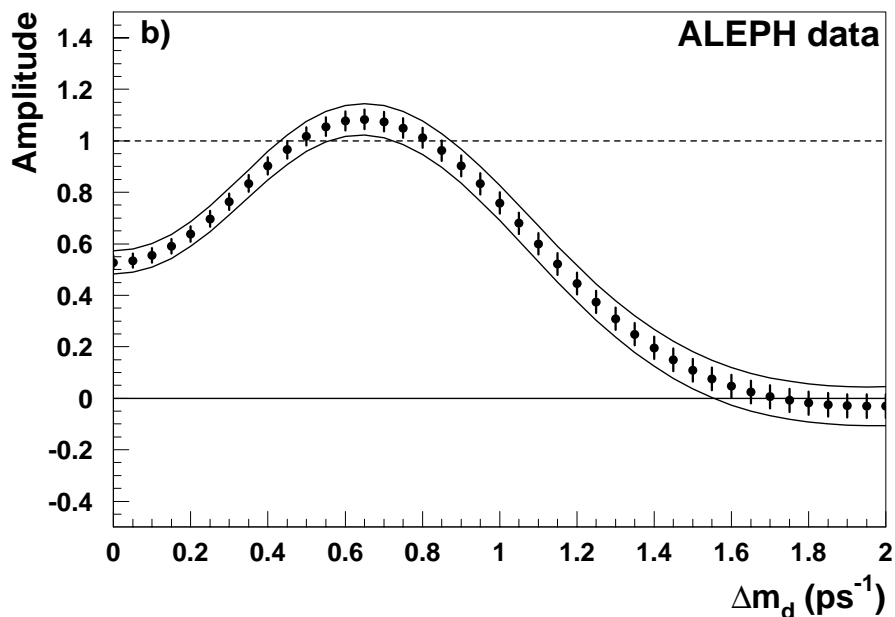
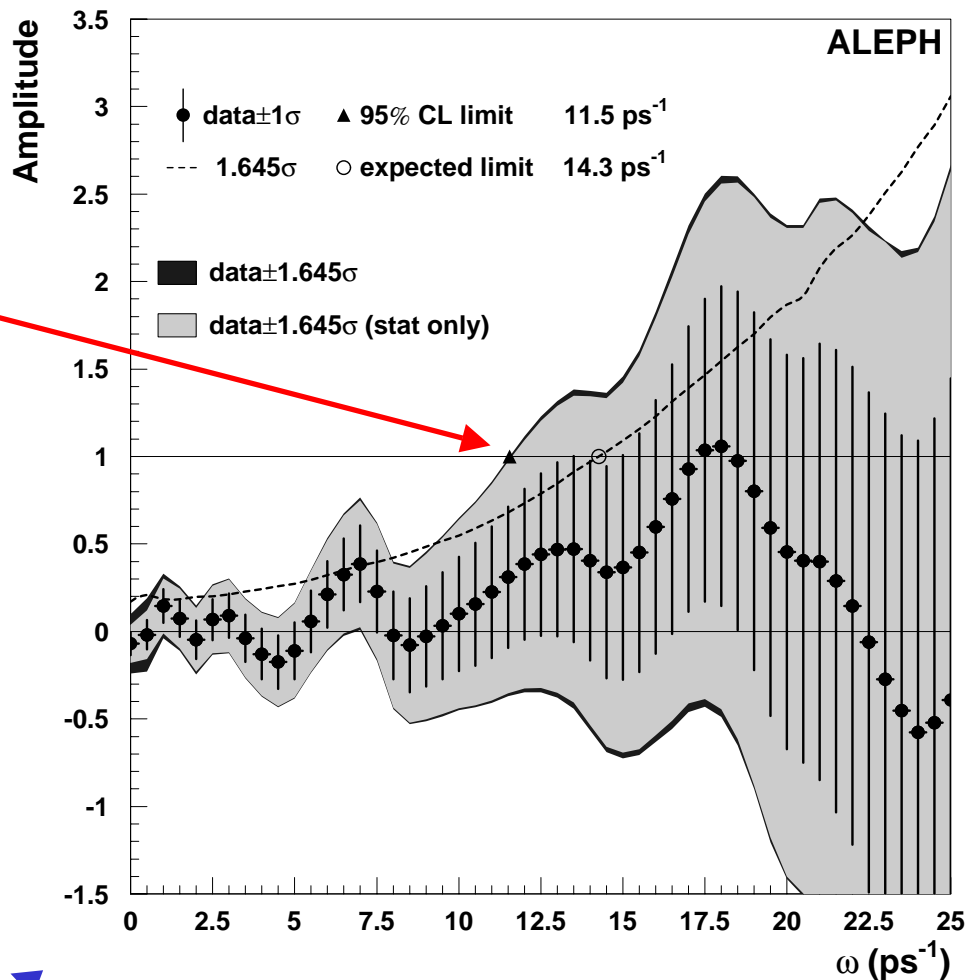
- ALEPH Inclusive Lepton**

Amplitude fit for B_s mixing

$\Delta m_s > 11.5 \text{ ps}^{-1}$ (95% C.L.)

Sensitivity = 14.3 ps^{-1}

(assuming B_s prod frac = 10.7%)



Amplitude fit for B_d mixing

$\Delta m_d = 0.55 \text{ ps}^{-1}$ ($\sigma_{\text{syst}} = 0.08 \text{ ps}^{-1}$)

Semi-exclusive Methods (I)

- Ds-Lepton Analyses** ALEPH, DELPHI, OPAL, CDF

Partial reconstruction of $B_s \rightarrow D_s^- l^+ \nu_l$

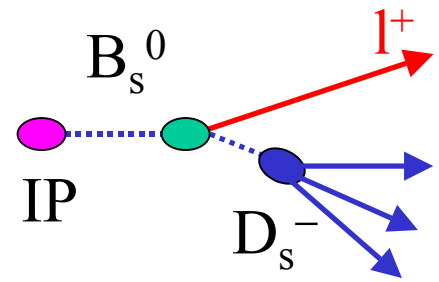
with full or partial reconstruction of D_s decay

$D_s^- \rightarrow \phi\pi^-, K^{*0}K^-, K_s^0K^-, \dots \phi h^- X$

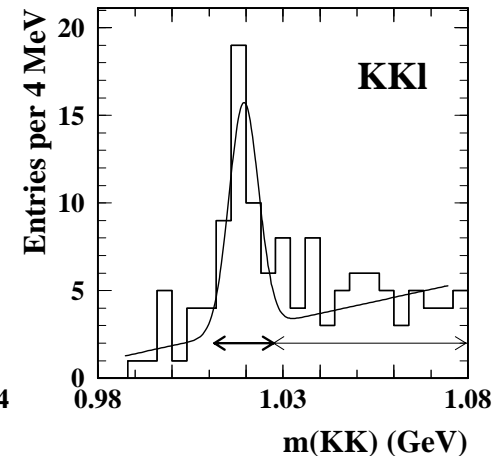
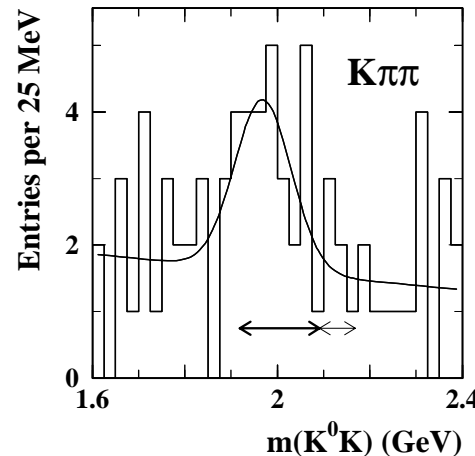
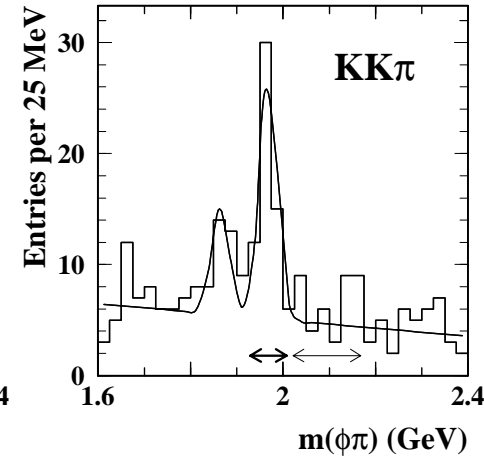
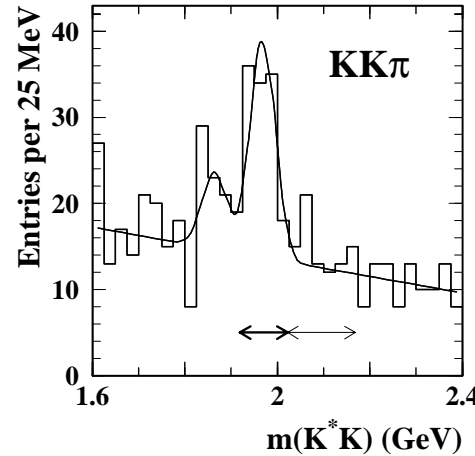
use dE/dx (and RICH @ DELPHI)

Pros: high B_s purity, good proper time resolution

Cons: low statistics



OPAL



Semi-Exclusive Methods (II)

- DELPHI Ds-Lepton** (3.5 M Z⁰)

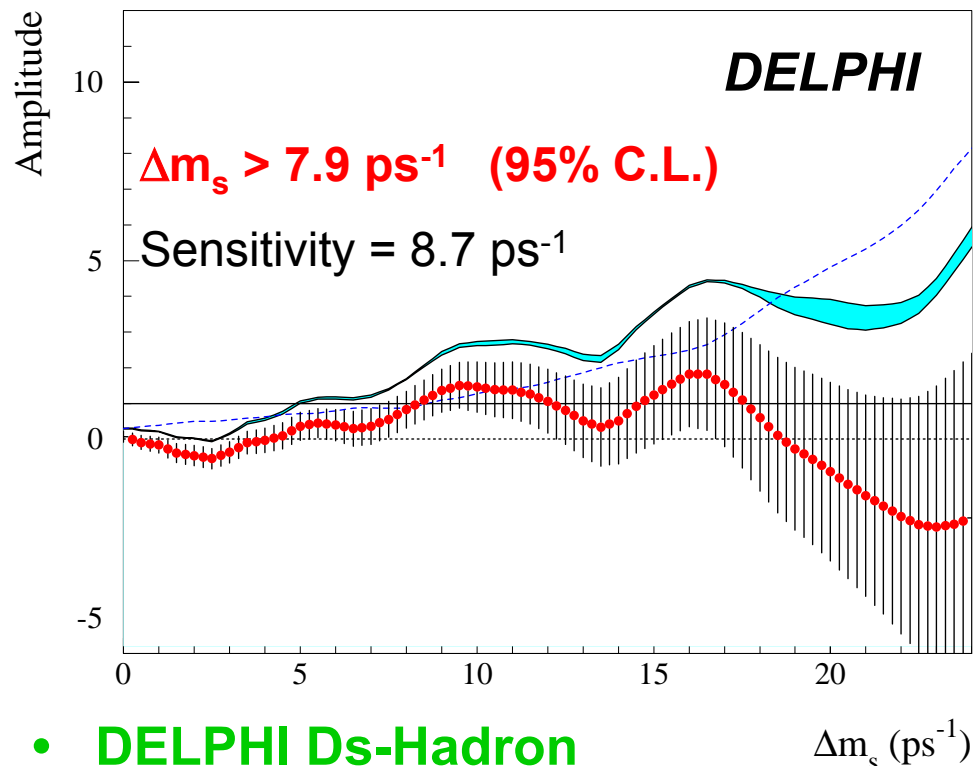
436 D_s l candidates

230 ± 18 from B_s → D_s l ν_l

σ_L = 200 μm (82%) & 740 μm (16%)

σ_p / p = 0.07 (82%) & 0.16 (16%)

now includes evt-by-evt resolution

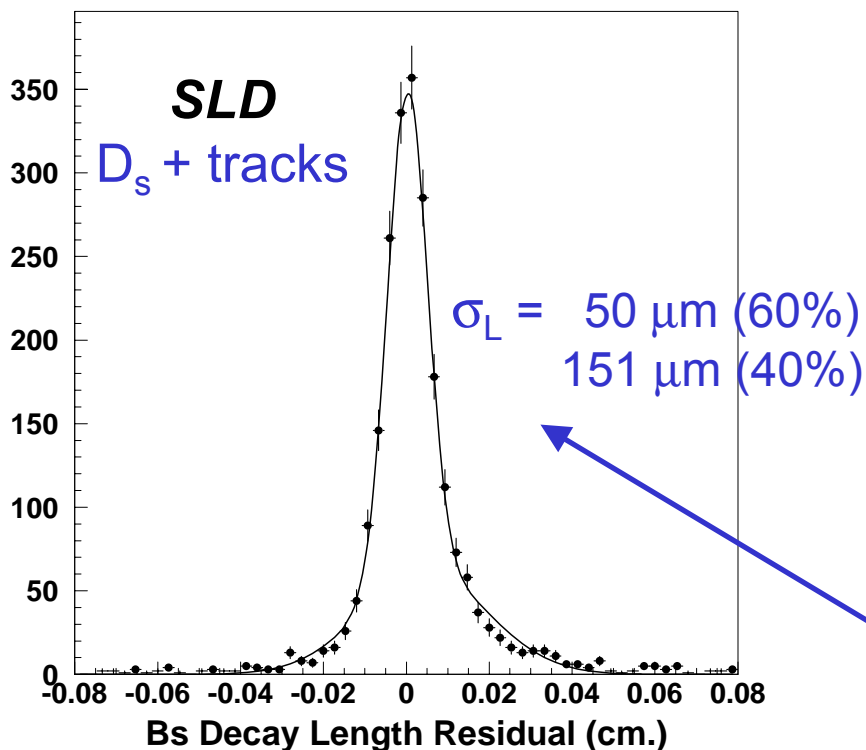


- DELPHI Ds-Hadron**

Higher efficiency but less sensitive than D_s-lepton due to worse resolution and lower B_s purity

- SLD Ds-Tracks** (lepton or hadrons)

Good B_s purity (40%) and **best resolution**



Exclusive Method

- ALEPH+DELPHI** (4.4+3.5 M Z^0)

Full reconstruction of

$$B_s \rightarrow D_s^- \pi^+, D_s^- a_1^+$$

$$\bar{D}^0 K^- \pi^+, \bar{D}^0 K^- a_1^+$$

with fully reconstructed D_s and \bar{D}^0 decays

Also sensitive to modes with

$$\text{photons: } D_s^{*-} \pi^+, D_s^{(*)-} \rho^+, D_s^{*-} a_1^+$$

→ satellite peak if missed photon(s)

B_s signal in main peak:

14 (ALEPH) + 8 (DELPHI)

B_s signal in satellite peak:

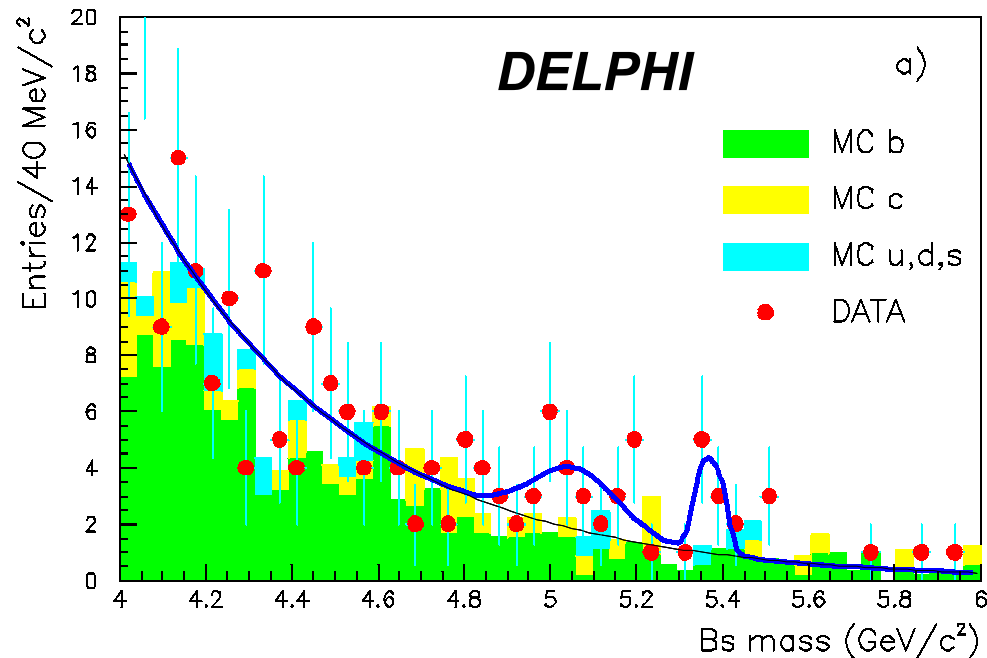
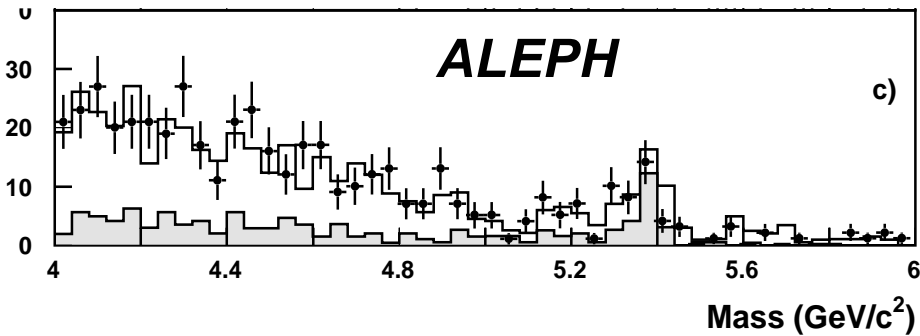
14 (ALEPH) + 15 (DELPHI)

Excellent proper time resolution

$$\langle \sigma_L \rangle = 180 \mu\text{m} \text{ (ALEPH)}$$

$$\sigma_L = 117 \mu\text{m} \text{ (58\%)} \ \& \ 216 \mu\text{m} \text{ (42\%)} \text{ (DELPHI)}$$

$$\sigma_p / p \text{ very small (0.5\% ALEPH)}$$



B_s Oscillation Amplitude: *WORLD average*

Combine measurements from ALEPH, CDF, DELPHI, OPAL and SLD

Rescale results to common set of input parameters:

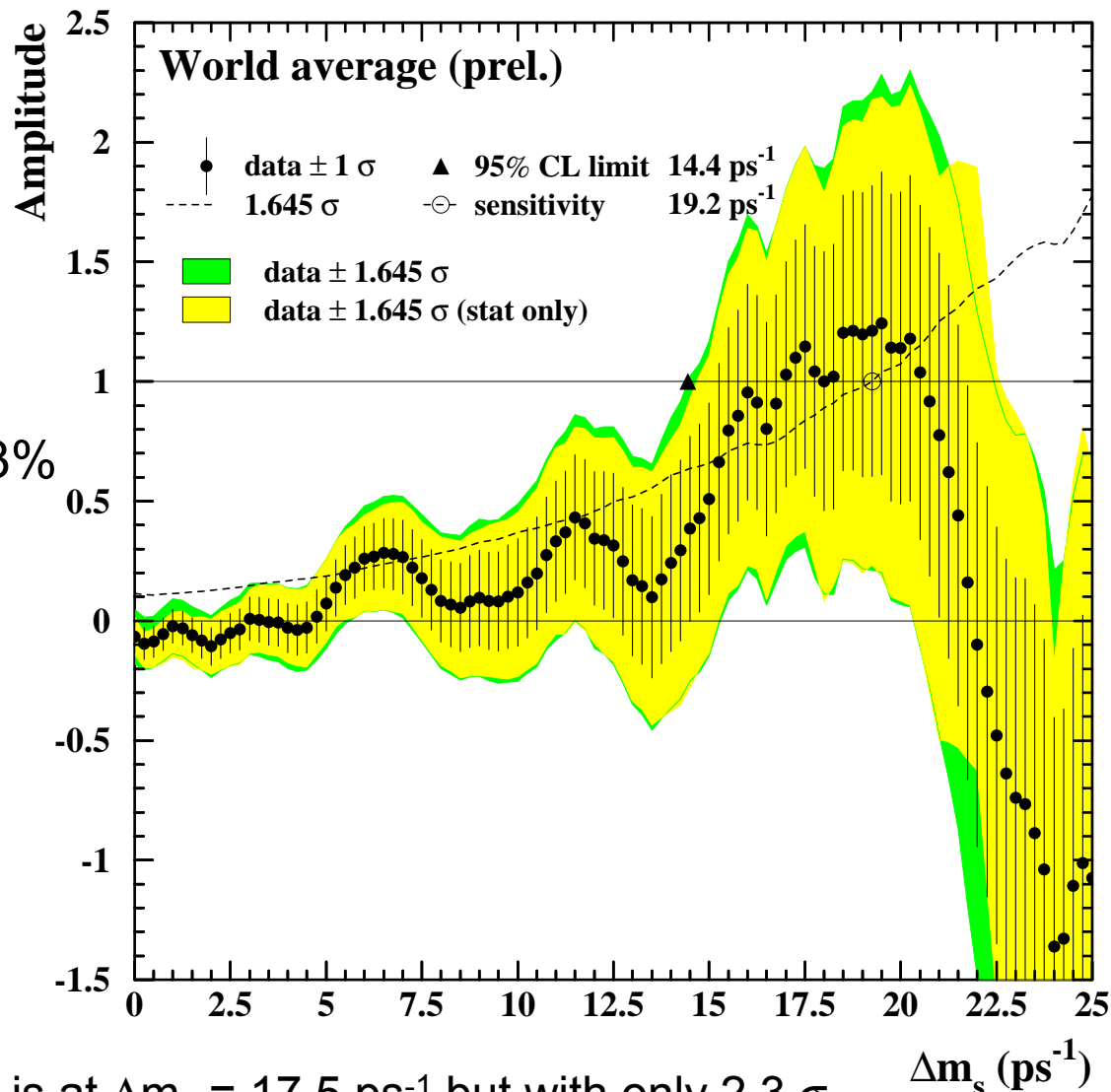
e.g., B_s production fraction = 9.3%

→ σ_A is rescaled for inclusive analyses

Sensitivity = 19.2 ps^{-1}

Lower limit at 95% C.L.:

$$\Delta m_s > 14.4 \text{ ps}^{-1}$$



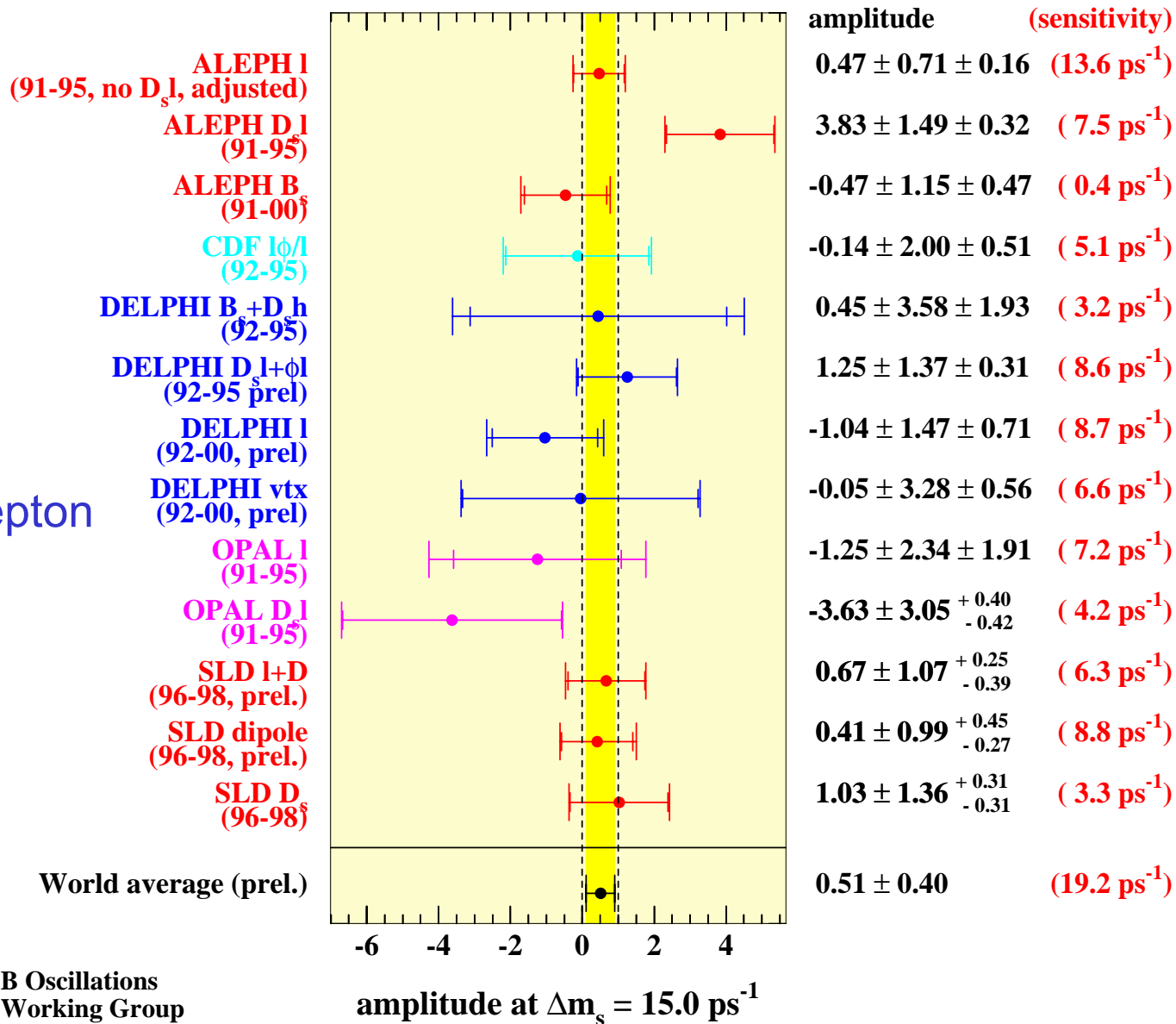
Most significant deviation from $A=0$ is at $\Delta m_s = 17.5 \text{ ps}^{-1}$ but with only 2.3σ

Individual B_s Oscillation Amplitude Measurements

Compare measured amplitudes at $\Delta m_s = 15.0 \text{ ps}^{-1}$

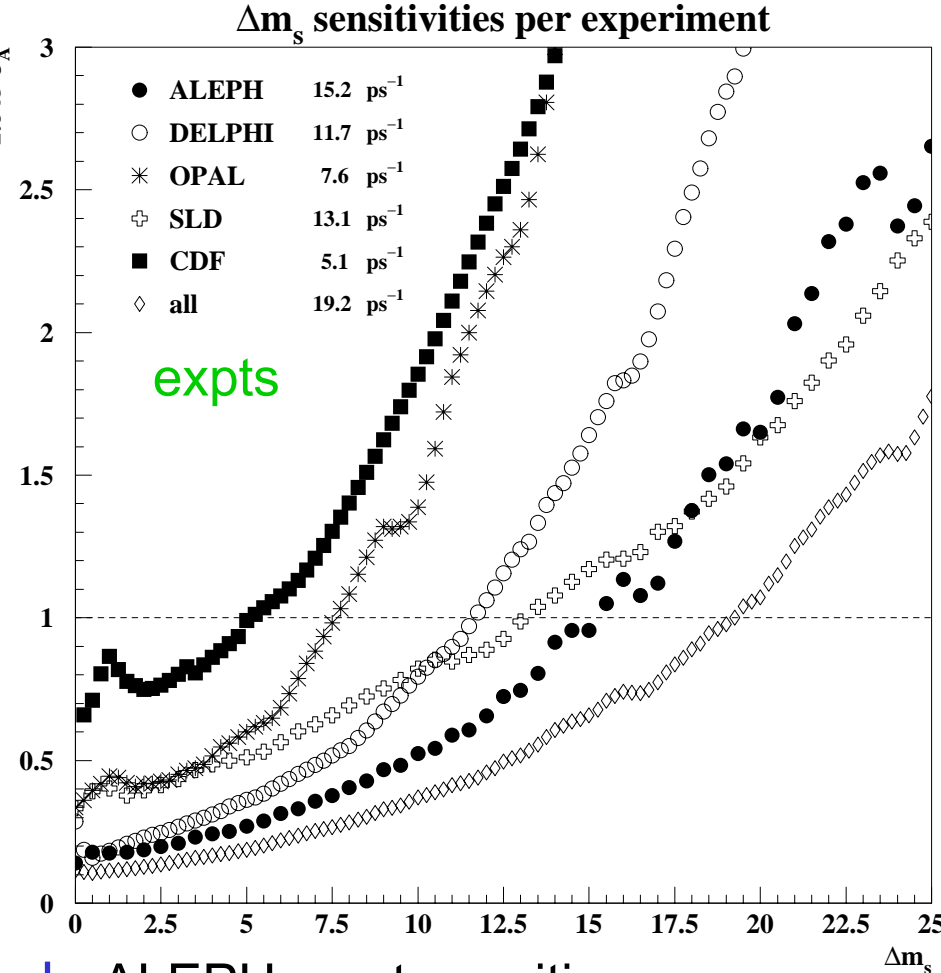
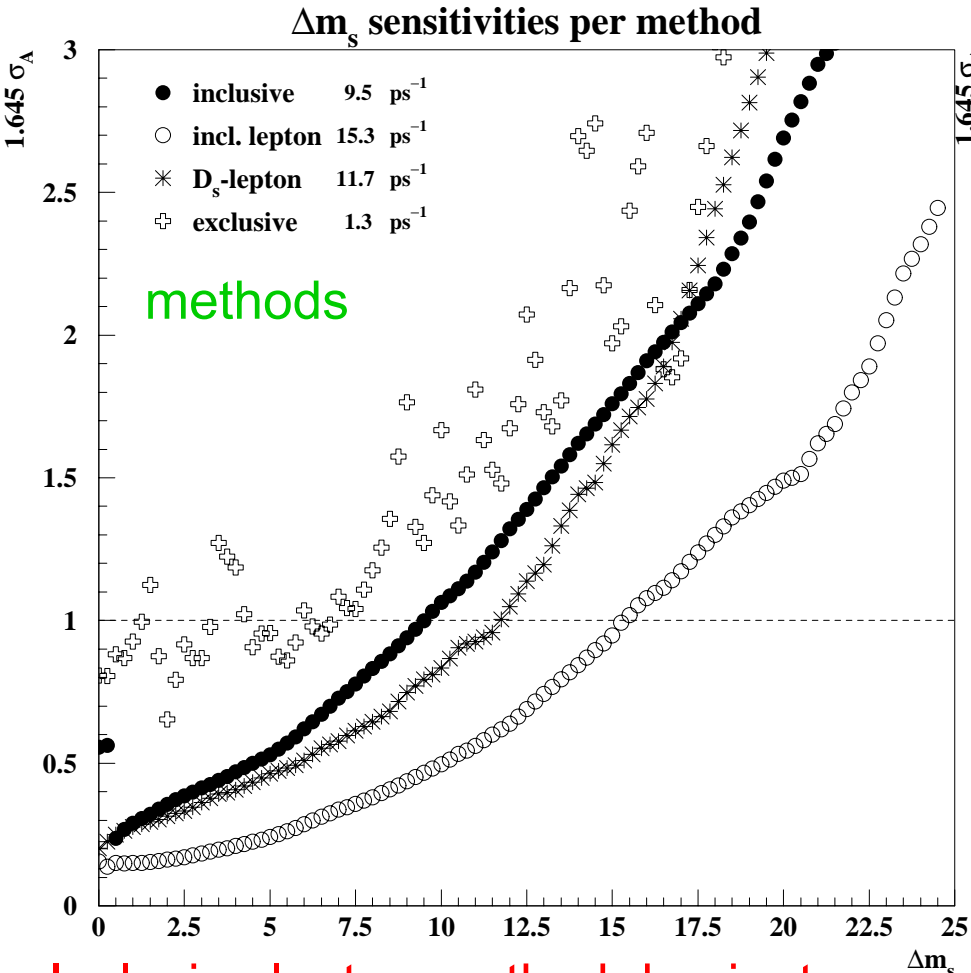
Most sensitive (smallest σ_A):

1. ALEPH inclusive lepton
2. SLD charge dipole
3. SLD lepton + D vtx



B_s Oscillation Sensitivity

Compare amplitude uncertainties ($1.645 \sigma_A$) as a function of Δm_s



Inclusive lepton method dominates

Exclusive method needs more statistics

ALEPH most sensitive

SLD hi-resolution \rightarrow smaller slope

B_s Oscillations Summary

The development of sophisticated analyses has provided steady increase in sensitivity

B_s oscillations yet to be observed

But current limit from

ALEPH+CDF+DELPHI+OPAL+SLD:

$$\Delta m_s > 14.4 \text{ ps}^{-1} \quad (95\% \text{ C.L.})$$

sets a powerful constraint on the unitarity triangle (see F. Parodi's talk)

LEP+SLD analyses nearly final

Look forward to 2nd generation expts (CDF, D0, LHCb, BTeV) to study B_s oscillations

World avg sensitivity vs.

