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A Review of the $|V_{ub}|$ and $|V_{cb}|$ Determinations

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on behalf of the V_{ub} and V_{cb} Working Groups



Introduction

Accurate $|V_{ub}|$ and $|V_{cb}|$ determination with well understood uncertainty
a key goal of heavy flavour physics programs;

Measuring upper vertex of Unitarity Triangle plays crucial role in studying origin
CP violation and answering fundamental questions which relate to it;

Theory, models and experimental techniques outline
comprehensive program based on Inclusive and Exclusive methods
where signal purities, control of backgrounds & theory uncertainties and extraction
of theory parameters directly from data are the main issues;

With present & foreseen experimental accuracies, theory uncertainties dominated
error budget making test of underlying assumptions necessary:
perform determinations with different methods and verify consistency will add truth
on each result;

Different kinematics and detector configurations at symmetric $\Upsilon(4S)$, asymmetric
 $\Upsilon(4S)$ and Z^0 and large data sets brought an healthy competition of
complementary approaches to this program.

✧ Extraction of CKM elements from inclusive decay rates based on Heavy Quark Theory implemented through **Operator Product Expansion** in the form of **HQE**;

✧ Expansion in powers of energy release in transition: $\simeq m_b$ in $b \rightarrow u$ and $m_b - m_c$ in $b \rightarrow c$ for inclusive rates and partially integrated spectra;

✧ HQE provides consistent theory framework for relating decay rates to $|V_{ub}|$ and $|V_{cb}|$:

$$\Gamma_{sl} = F_b^{quark\ decay} \times \left(1 + \frac{0}{m_b} + \frac{f(\lambda_1, \lambda_2)}{m_b^2} + \dots + \alpha_s(\dots) + \alpha_s^2(\dots) + \dots \right)$$

$$V_{ub} = 0.00445 \times \left(\frac{BR(b \rightarrow u\ell\bar{\nu})}{0.002} \frac{1.55\text{ps}}{\tau_b} \right)^{1/2} \times (1 \pm 0.020 \pm 0.052),$$

✧ OPE predictions postulate quark-hadron duality, expected to hold best for s.l. decays, prompting the need for experimental tests;

✧ must determine input parameters: m_b $[\bar{\Lambda}]$, μ_π^2 $[\lambda_1]$, (ρ_D^3, \dots) ;

✧ must understand effects of experimental cuts trimming inclusive distributions.

Extracting Parameters and Testing OPE with Data

Relations between first moments of E_ℓ , M_X and E_γ and b -quark mass and kinetic energy

Several Determinations now becoming available:

BABAR

CLEO

DELPHI

$$E_0(E_\ell), E_1(E_\ell)$$

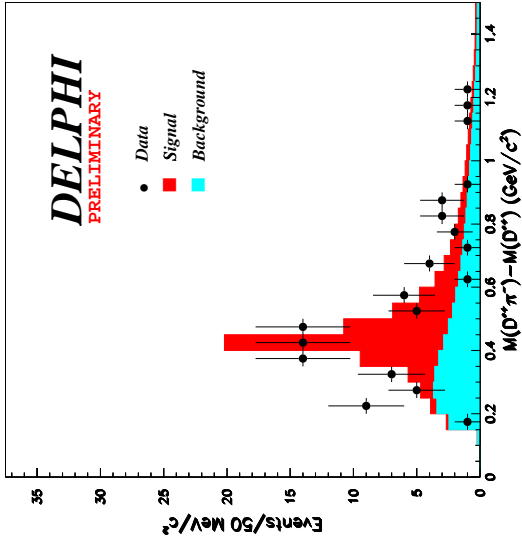
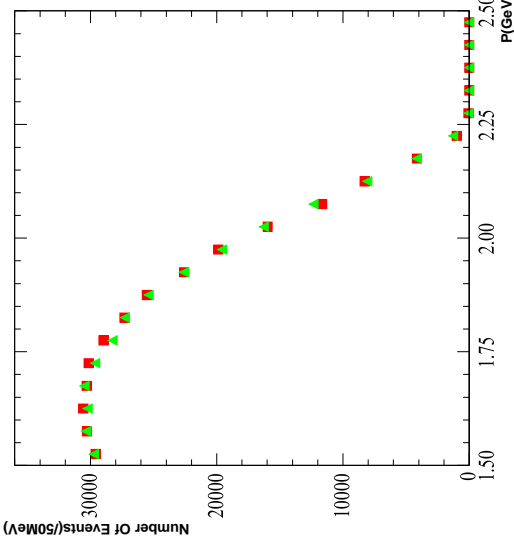
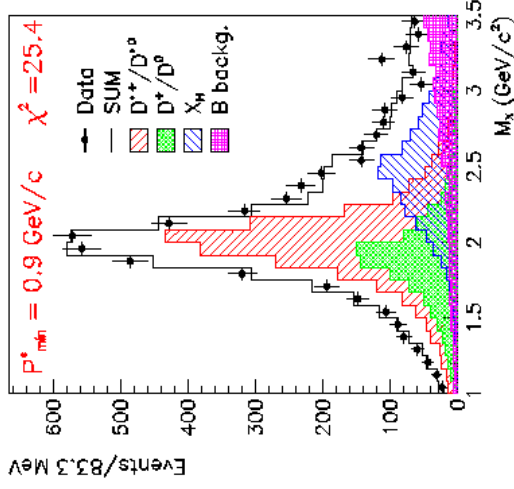
$$E_1(E_\ell), E_2(E_\ell), E_3(E_\ell)$$

$$M_1(M_X)$$

$$M_1(M_X), M_2(M_X)$$

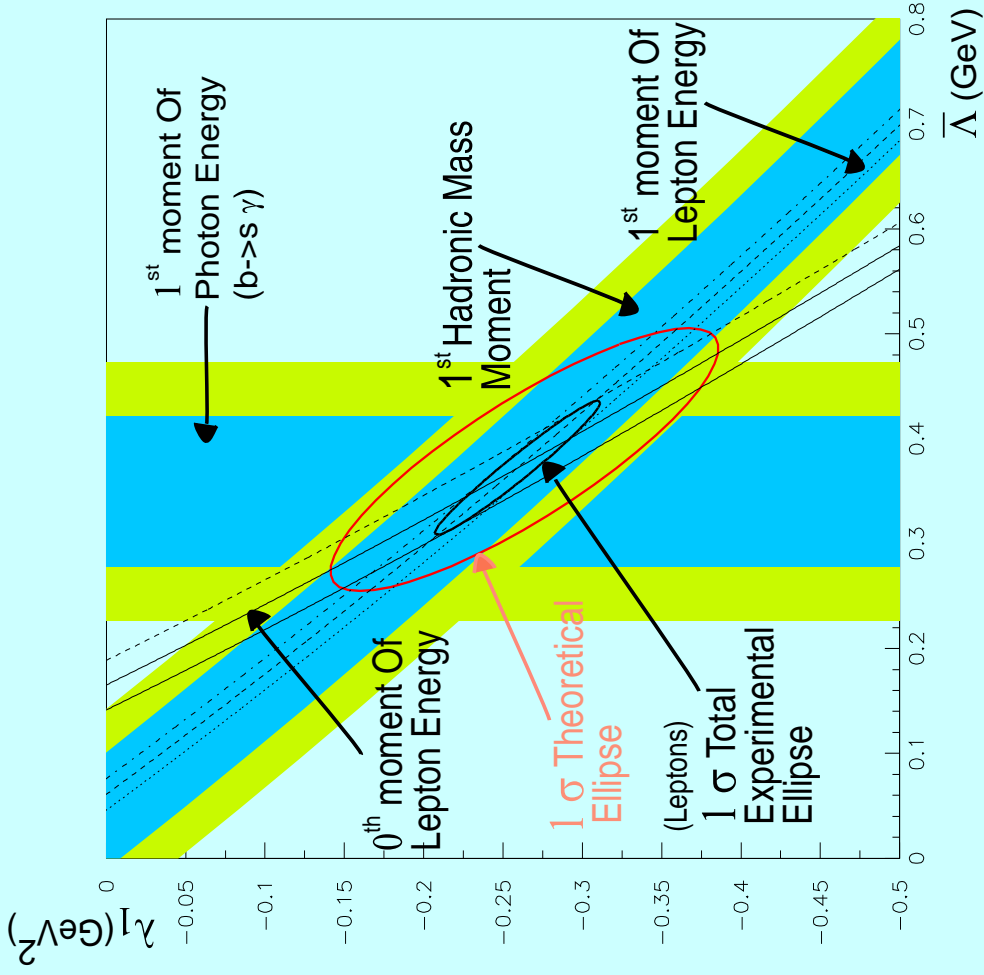
$$M_1(M_X), M_2(M_X), M_3(M_X)$$

$$M_1(E_\gamma), M_2(E_\gamma)$$

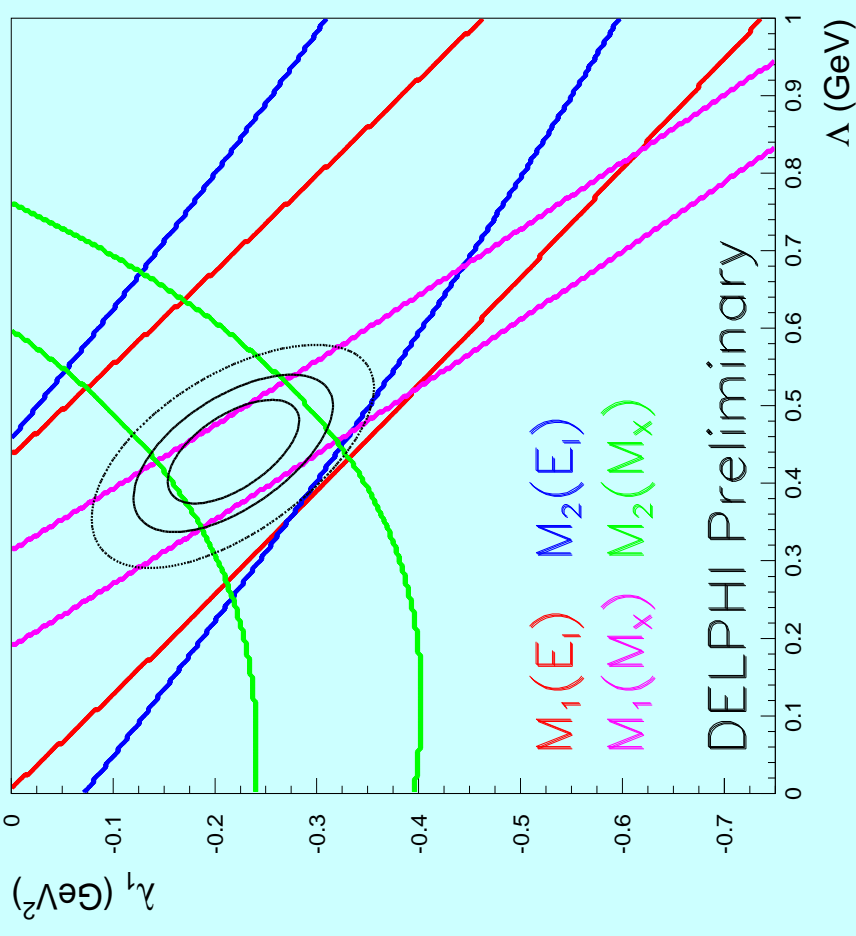


Consistency between different determinations sets constraints on possible duality violation as well as on effects from truncated OPE.

CLEO PRELIMINARY



DELPHI PRELIMINARY



Power corrections increase with E_ℓ cut \rightarrow interesting to test stability of fit results:

CLEO $E_\ell > 1.5$ GeV DELPHI $E_\ell \geq 0.5$ GeV

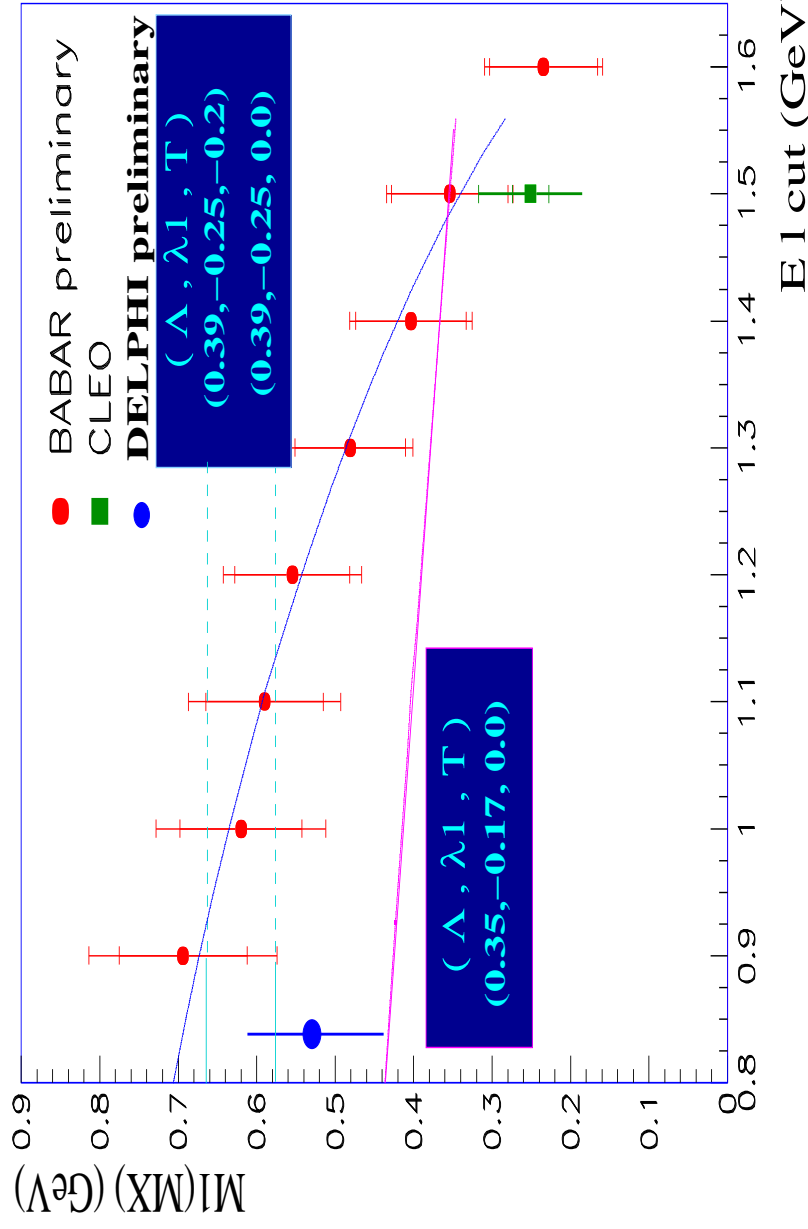
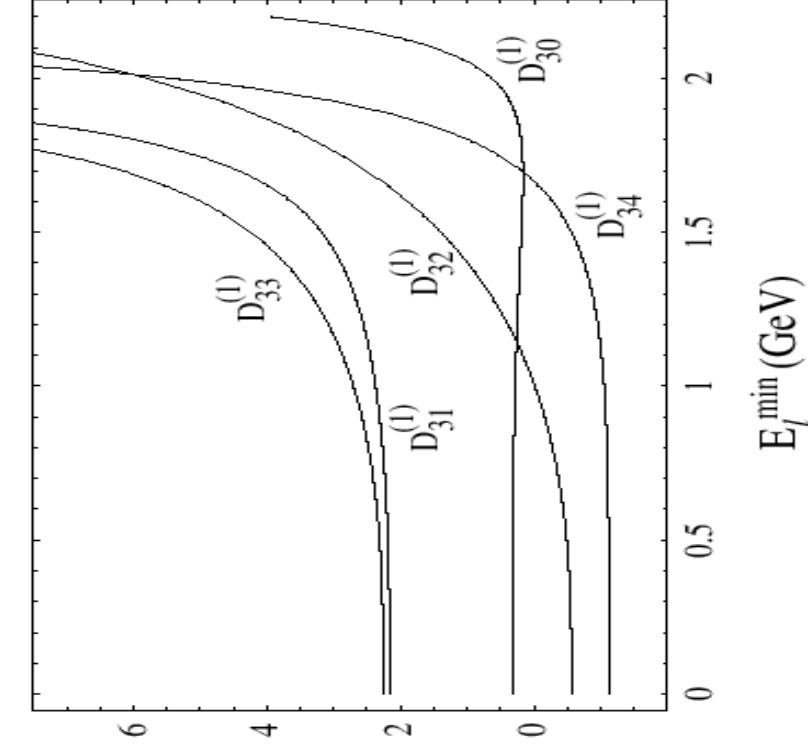
BABAR 0.8 GeV $< E_\ell < 1.6$ GeV

$1/m_b^3$ Coefficients vs. E_ℓ^{cut}

Falk and Luke

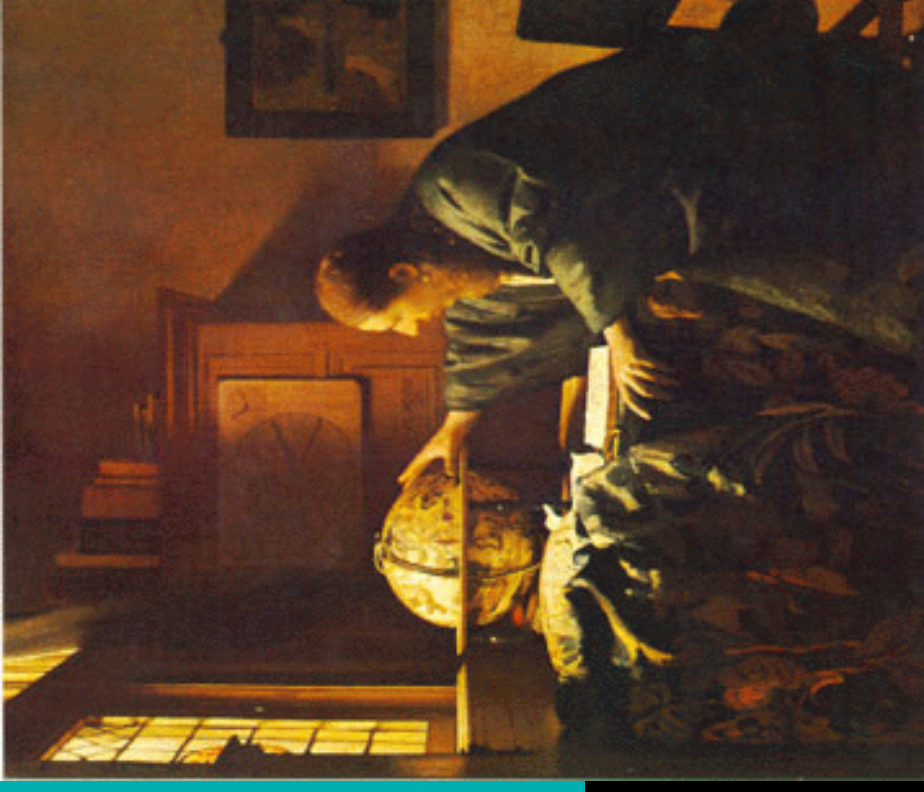
$M_1(M_X)$ vs. E_ℓ^{cut}

CLEO + BABAR + DELPHI PRELIMINARY



\diamond Slope tells of non-resonant states or rather about $1/m_b^3$ parameters ?

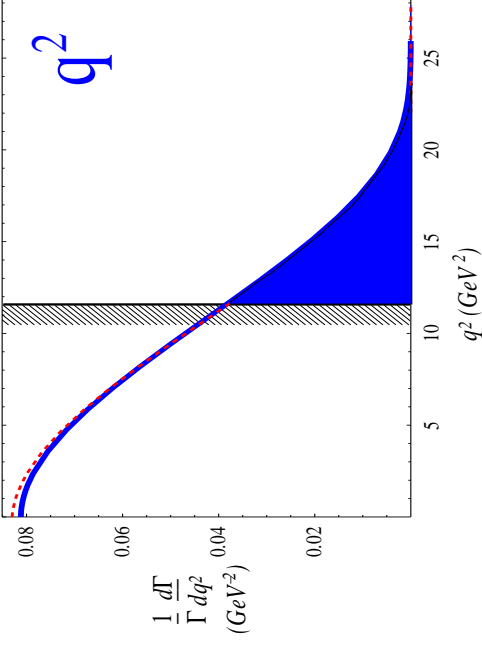
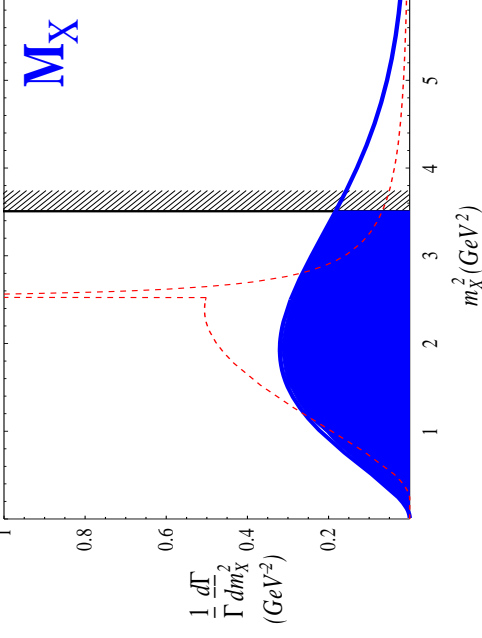
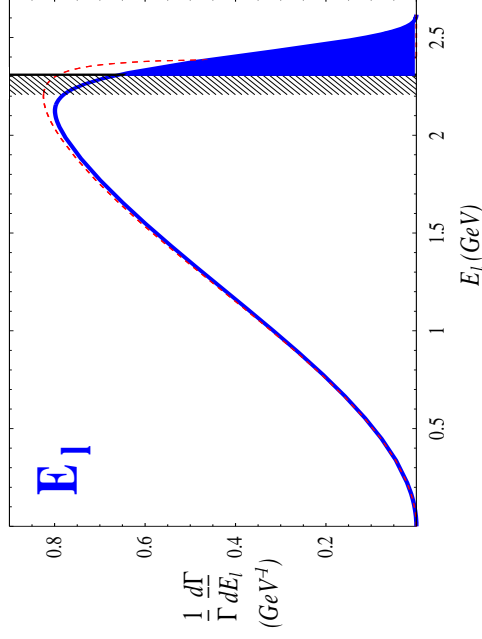
Vub



$$|V_{ub}|$$

Inclusive Determinations

Main issue $b \rightarrow u$ signal extraction from $\simeq 75\times$ larger $b \rightarrow c$: need to know and control differential rates in regions of phase space where $b \rightarrow c$ suppressed;



$$E_\ell > \frac{M_B^2 - M_D^2}{2M_B}$$

$$M_{uq} < M_{cq}$$

$$M_{\ell\nu}^2 = q^2 > (M_B - M_D)^2$$

	ALEPH	BABAR	CLEO	CLEO	DELPHI	L3	OPAL
E_ℓ	EPJC6(99)	PRL88(02)	PLB478(00)	PLB436(98)	EPJC21(01)		
F_u	NN	E_ℓ	E_ℓ	$M_X - q^2$	M_X	$\pi - \ell$	NN
Purity	0.06	.07	.13	0.15	0.68	0.18	0.04
$\sigma_{b \rightarrow c}$	15%	3%	7%	6%	12%	22%	15%
σ_{th}	9%	13%	13%	14%	10%	10%	10%

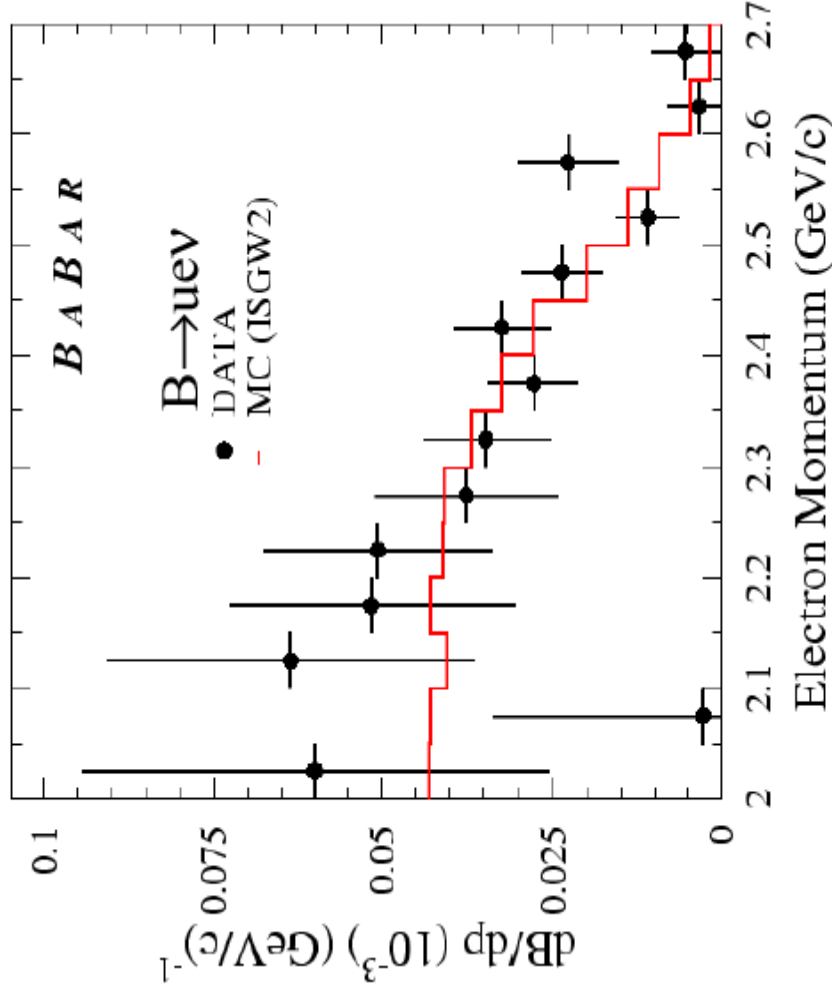
BaBar E_e Endpoint

Preliminary

Count within $2.3 \text{ GeV} < E_e < 2.6 \text{ GeV}$

compute F_u with $b \rightarrow s\gamma$

$F_u = 0.07$, $S/B = 0.26$



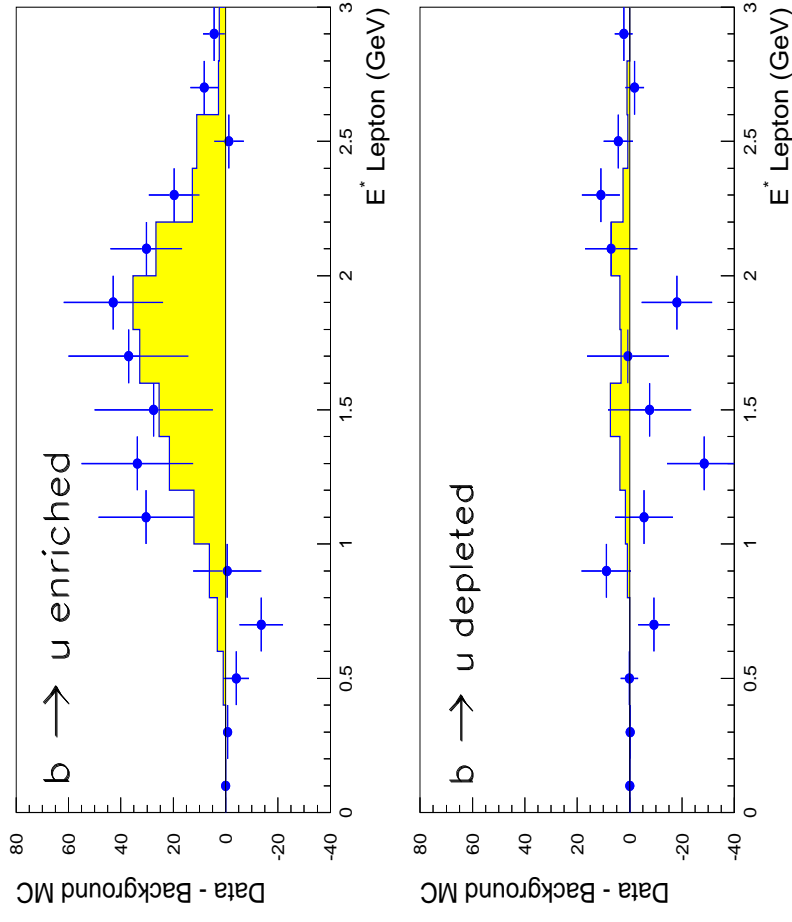
DELPHI M_X

PLB B478 (2000)

Fit E_ℓ^* for $M_X \gtrsim 1.6$

for enriched and depleted samples

$F_u = 0.68$, $S/B = 0.10$



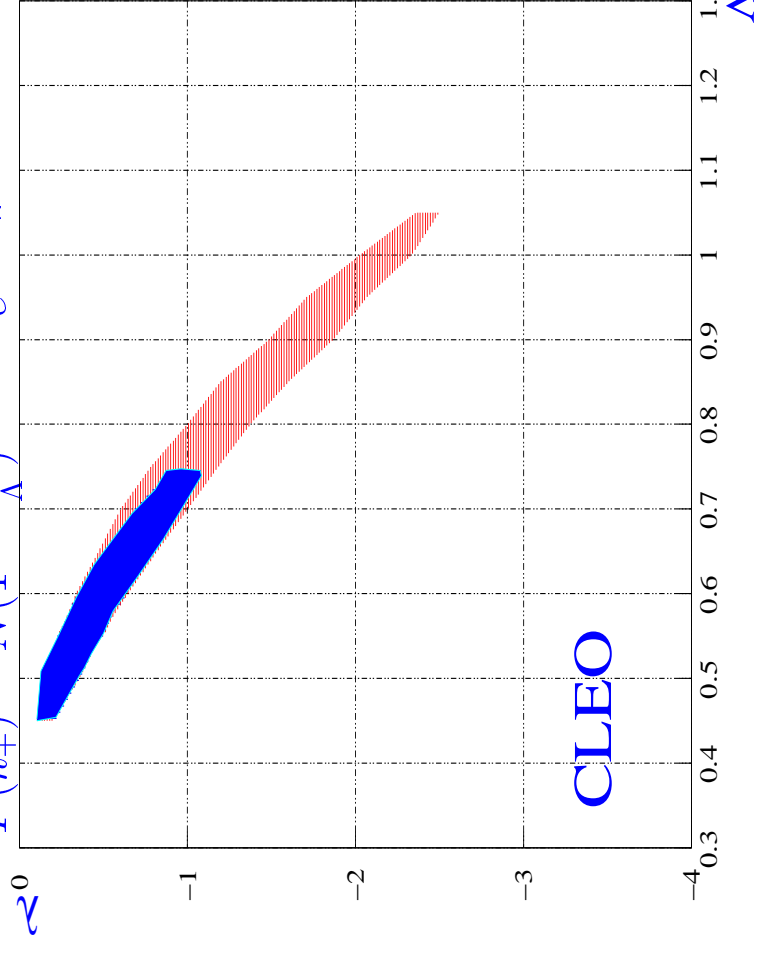
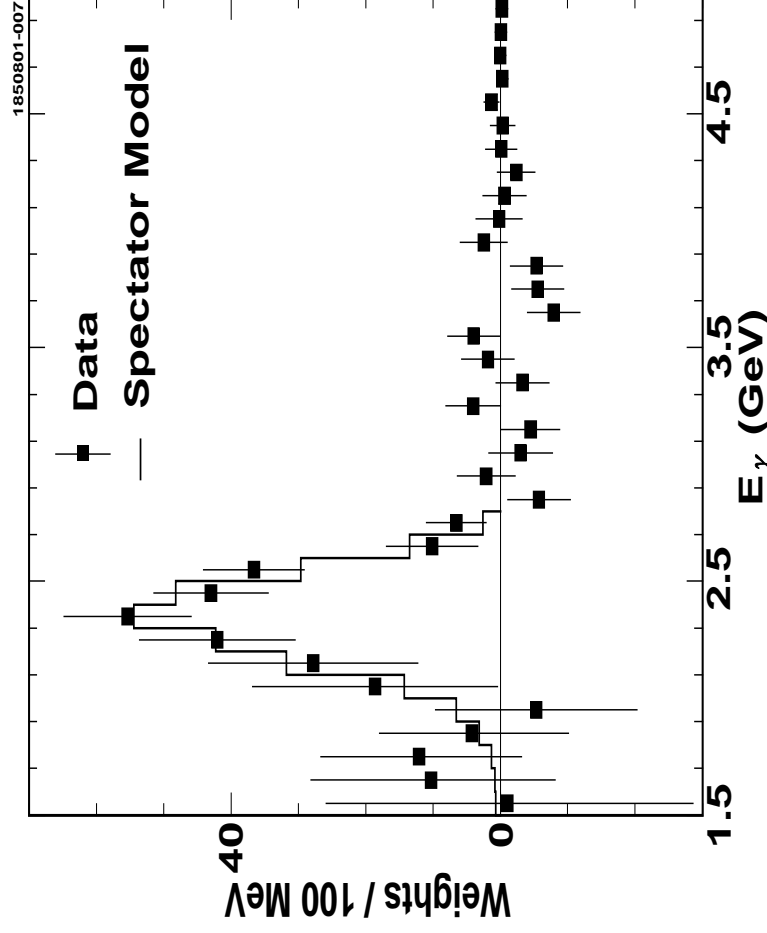
Issues in Theory Uncertainties: Shape Function Parameters

- ◆ include non-perturbative effects through shape function $F(k_+)$ and fold parton level $d\Gamma/ds'$ to derive physical distributions $d\Gamma/ds = \int dk_+ d\Gamma/ds' F(k_+)$
- ◆ relate $F(k_+)$ in $b \rightarrow X_u \ell \bar{\nu}$ and $b \rightarrow X_s \gamma$:

CLEO E_γ Spectrum

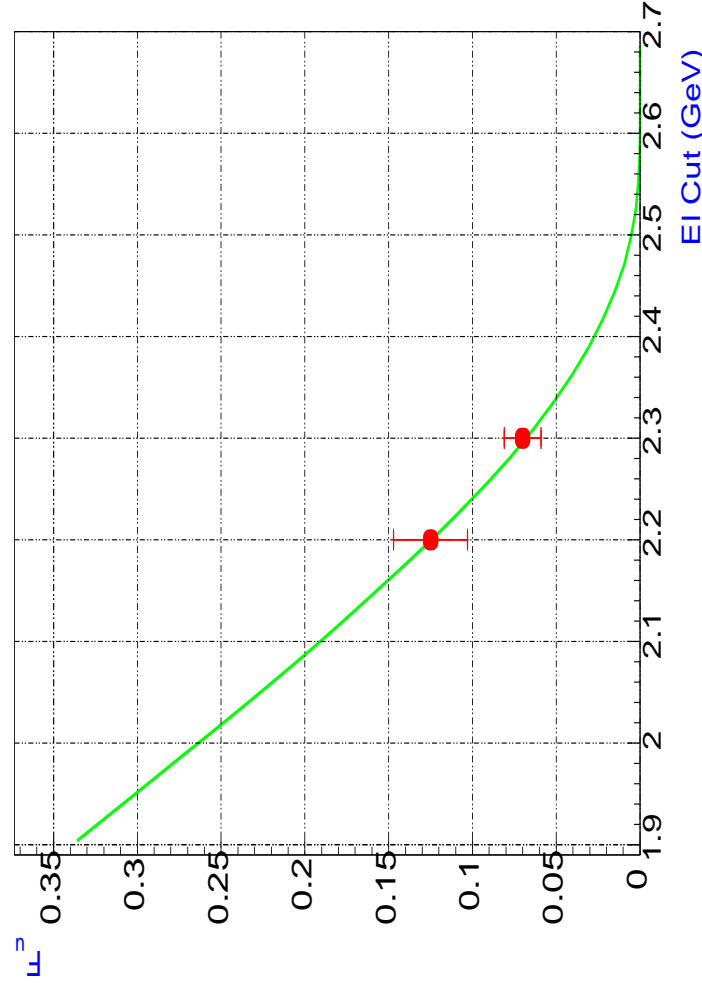
$F(k_+)$ Constraints from $b \rightarrow X_s \gamma$

$$F(k_+) = N \left(1 - \frac{k_+}{\Lambda}\right)^{-3\Lambda^2/\lambda} e^{(1 - \frac{3\Lambda^2}{\lambda})k_+/\Lambda}$$

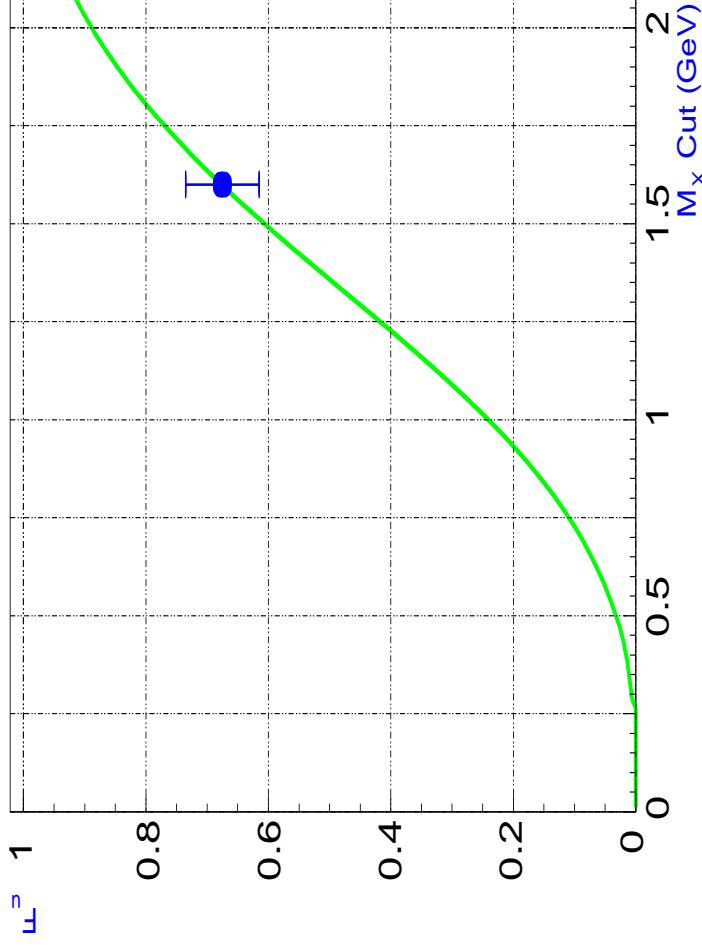


- ◆ important to probe full photon spectrum $1.5 \text{ GeV} < E_\gamma < 2.8 \text{ GeV}$

F_u with E_ℓ Cut



F_u with M_X Cut



for $E_\ell > 2.2$ GeV $\delta|V_{ub}|/|V_{ub}| = \pm 8.0\%$

for $M_X < 1.6$ GeV

$\delta|V_{ub}|/|V_{ub}| = \pm 4.4\%$

Lepton Endpoint subleading corrections suppressed by (Λ_{QCD}/m_b) factors but numerically enhanced;
 Future measurements to use $b \rightarrow s\gamma$ constraints instead simple parameter ranges

Leibovich, Ligeti, Wise PLB539, Neubert hep-ph/0207002

CLEO M_X - q^2 Preliminary

Use ν reconstruction and combine $M_X + q^2$ cuts
(after Bauer, Ligeti, Luke);

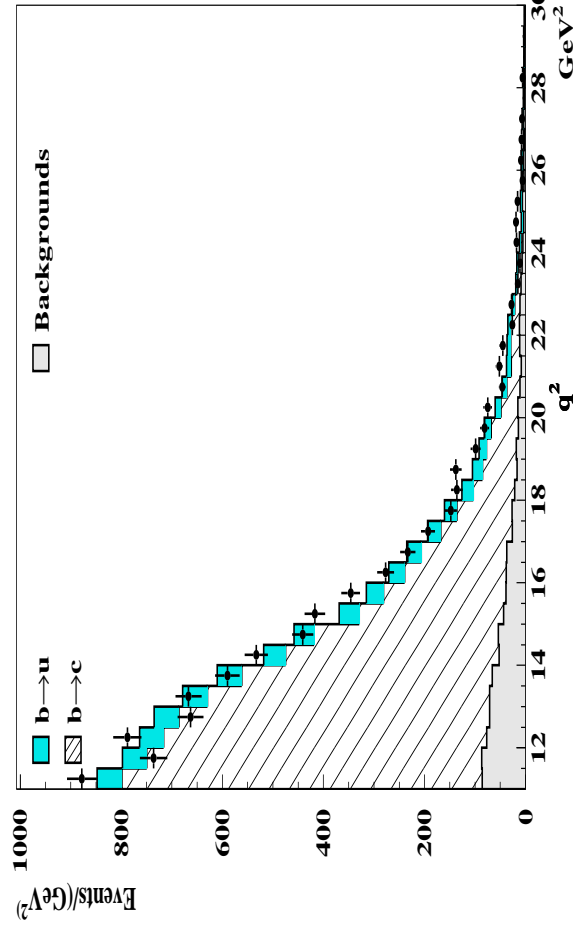
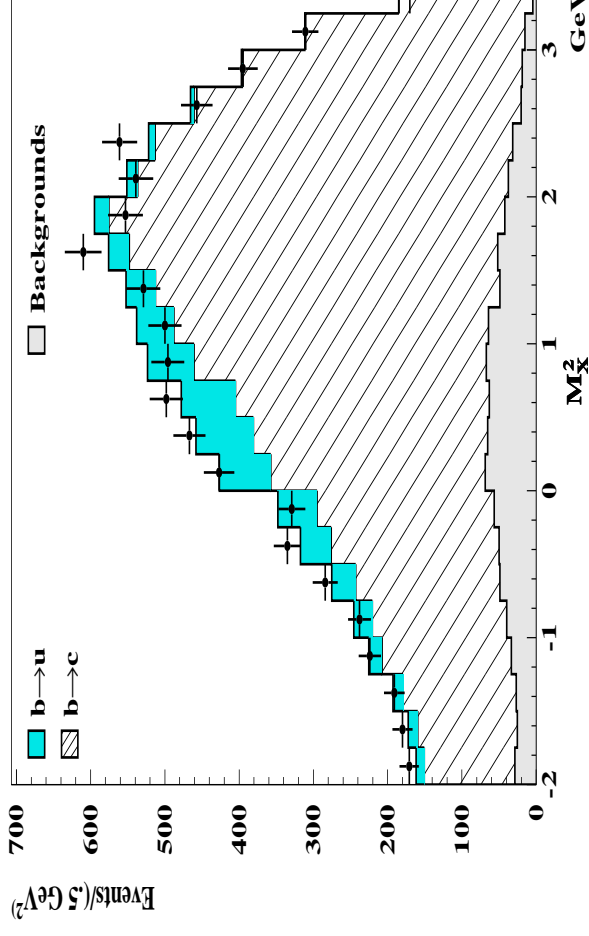
$$M_X \simeq M_B^2 + q^2 - 2E_{beam}(E_\ell + E_\nu)$$

Full fit to $q^2/(E_\ell + E_\nu)^2$, M_X , $\cos\theta_{W\ell}$

Uses models to extract sample composition and to relate regions of highest sensitivity and safe regions to extract $B \rightarrow X_u \ell \nu$

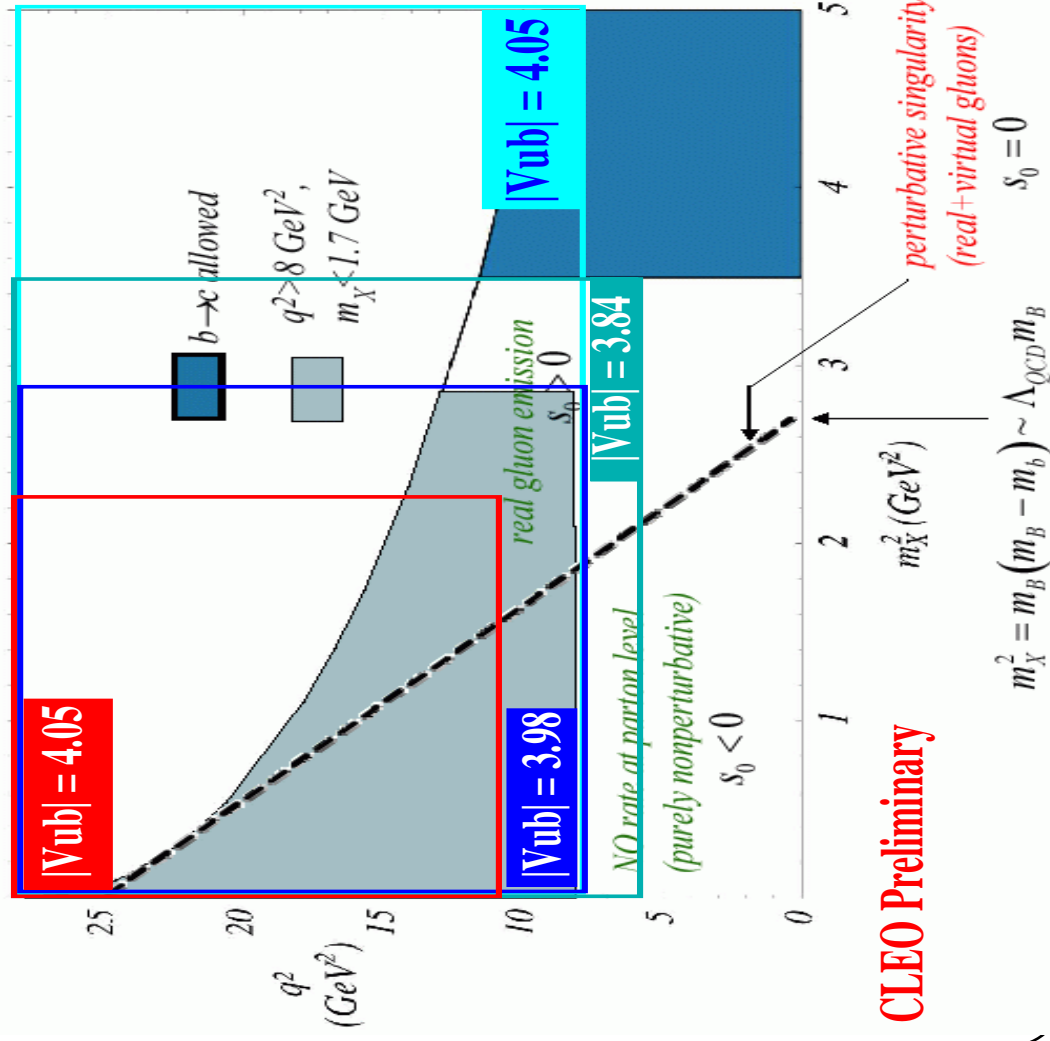
Branching fractions inferred for several regions in $M_X - q^2$ plane, HQET+OPE used to extract $|V_{ub}|$ values found to agree.

Result given for $M_X < 1.5$ GeV and $q^2 > 11$ GeV² to minimise model dependence.

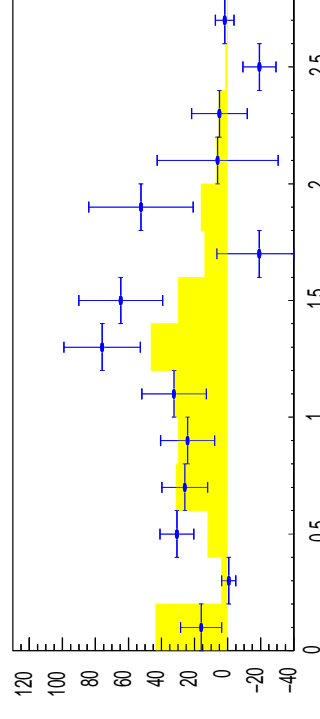
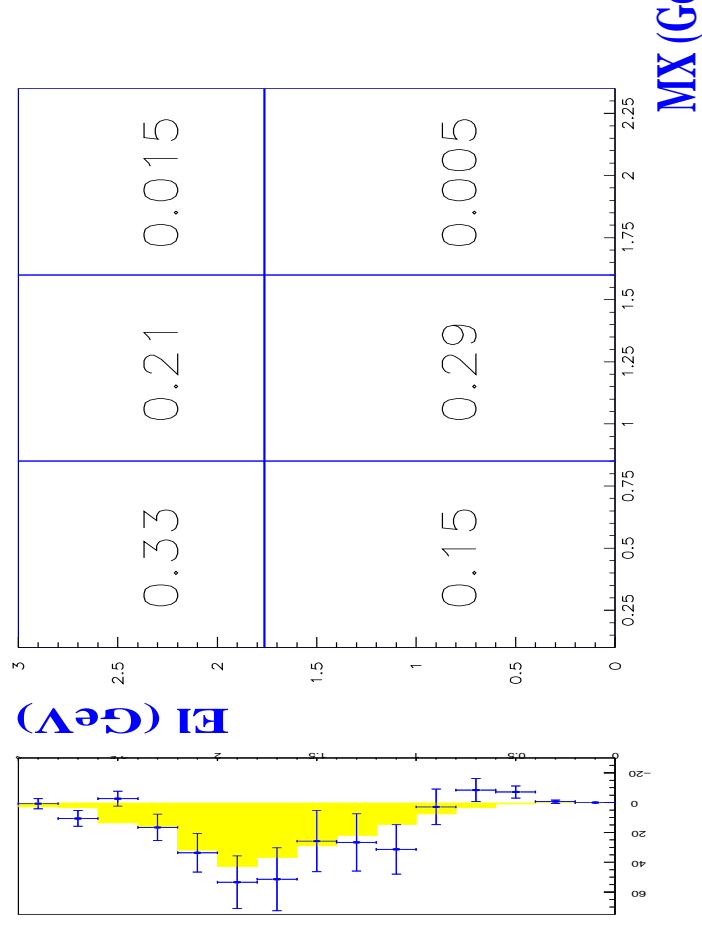


Issues in Theory Uncertainties: Decay Phase-Space Sampling

$|V_{ub}|$ FITS IN $M_X - q^2$ (CLEO)



$|V_{ub}|$ WEIGHTS IN $M_X - E_\ell$ (DELPHI)



Exclusive Determinations

$$\frac{d\Gamma(B^0 \rightarrow \pi^- \ell^+ \nu)}{dy d\cos\theta_\ell} = |V_{ub}|^2 \frac{G_F^2 p_\pi^3 M_B^2}{32\pi^3} \sin^2\theta_\ell |f_1(q^2)|^2,$$

- ✧ Exclusive $B \rightarrow X_u \ell \bar{\nu}$ decays provide with good S/B and reasonable statistics;
- ✧ main uncertainties from form factors due to three sources:
 - i) ϵ determination, ii) cross-feed subtraction and iii) normalization;
- ✧ Form Factor determinations based on a variety of techniques:
- ✦ Light-Cone Sum Rules give $\simeq 15 - 20\%$ and assume quark-hadron duality
- ✦ Quenched Lattice calculations give $\simeq 15 - 20\%$, applicability limited to large q^2

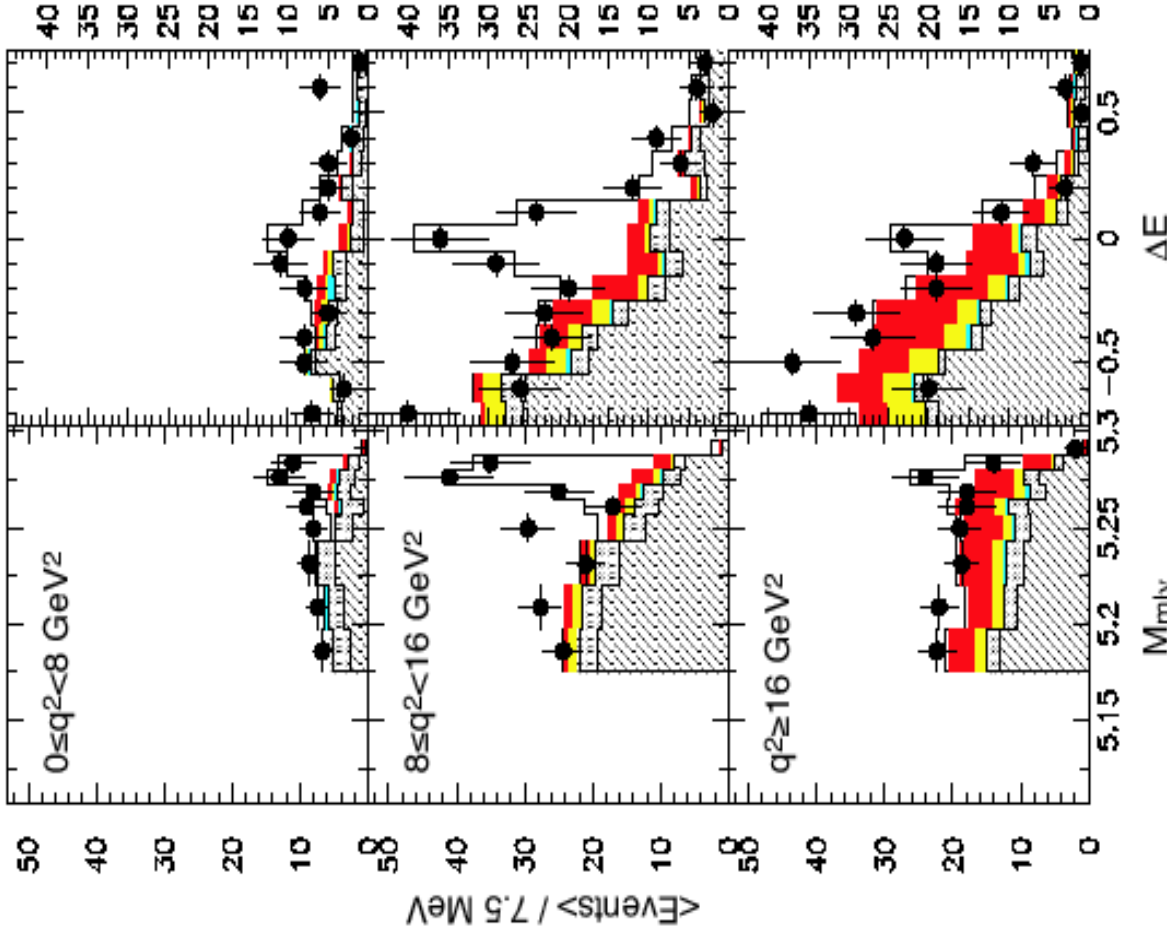
	BABAR	BELLE	CLEO	CLEO
Channel	$\rho \ell \nu$	$\pi \ell \nu$	$\pi(\rho) \ell \nu$	$\rho \ell \nu$
Purity	0.19			
$\sigma_{b \rightarrow c}$	1%		0.8%	1%
σ_{FF}	15%	19%	15%	17%

- ✦ Need to get $d\Gamma/dq^2$ from data to test models, improve accuracy;
- ✦ $\pi \ell \bar{\nu}$ possibly the golden channel here but $\rho/\omega \ell \bar{\nu}$ needed to cross-check results;

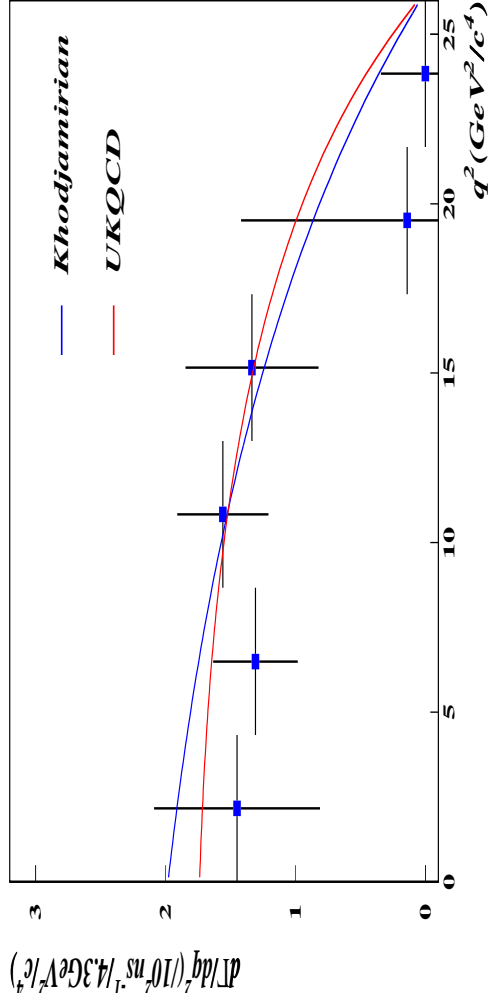
CLEO PRELIMINARY $B \rightarrow \pi \ell \bar{\nu}$

- Reduce FF dependence by extracting rates independently in q^2 bins;
- observed uncertainties in $\rho_{\ell \nu}$ from $X_u \ell \bar{\nu}$ feed-down are large;

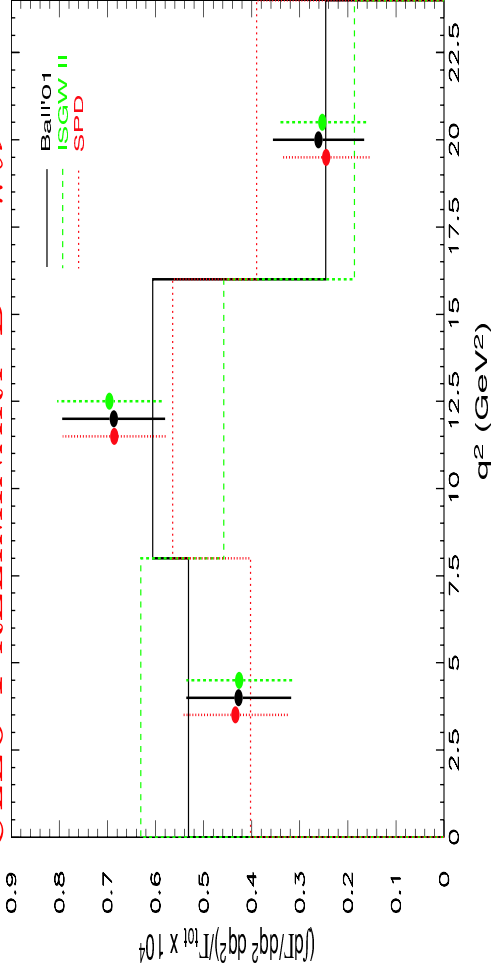
Channel	CLEO Preliminary BR (10^{-4})
$B^0 \rightarrow \pi^+ \ell^- \bar{\nu}$	$1.38 \pm 0.22 \pm 0.11$
$B^0 \rightarrow \rho^- \ell^+ \bar{\nu}$	$2.69 \pm 0.41 \pm 0.62$
$B^- \rightarrow \eta \ell^- \bar{\nu}$	$0.85 \pm 0.31 \pm 0.14$
Belle Preliminary	
$B^0 \rightarrow \pi^+ \ell^- \bar{\nu}$	$1.33 \pm 0.11 \pm 0.21$
$B^- \rightarrow \rho^0 \ell^- \bar{\nu}$	$1.44 \pm 0.18 \pm 0.23$
$B \rightarrow \omega \ell \bar{\nu}$	$0.14 \pm 0.04 \pm 0.03$
BaBar Preliminary	
$B^0 \rightarrow \rho^- e^+ \bar{\nu}$	$3.39 \pm 0.44 \pm 0.79$



BELLE PRELIMINARY $B \rightarrow \pi \ell \bar{\nu}$

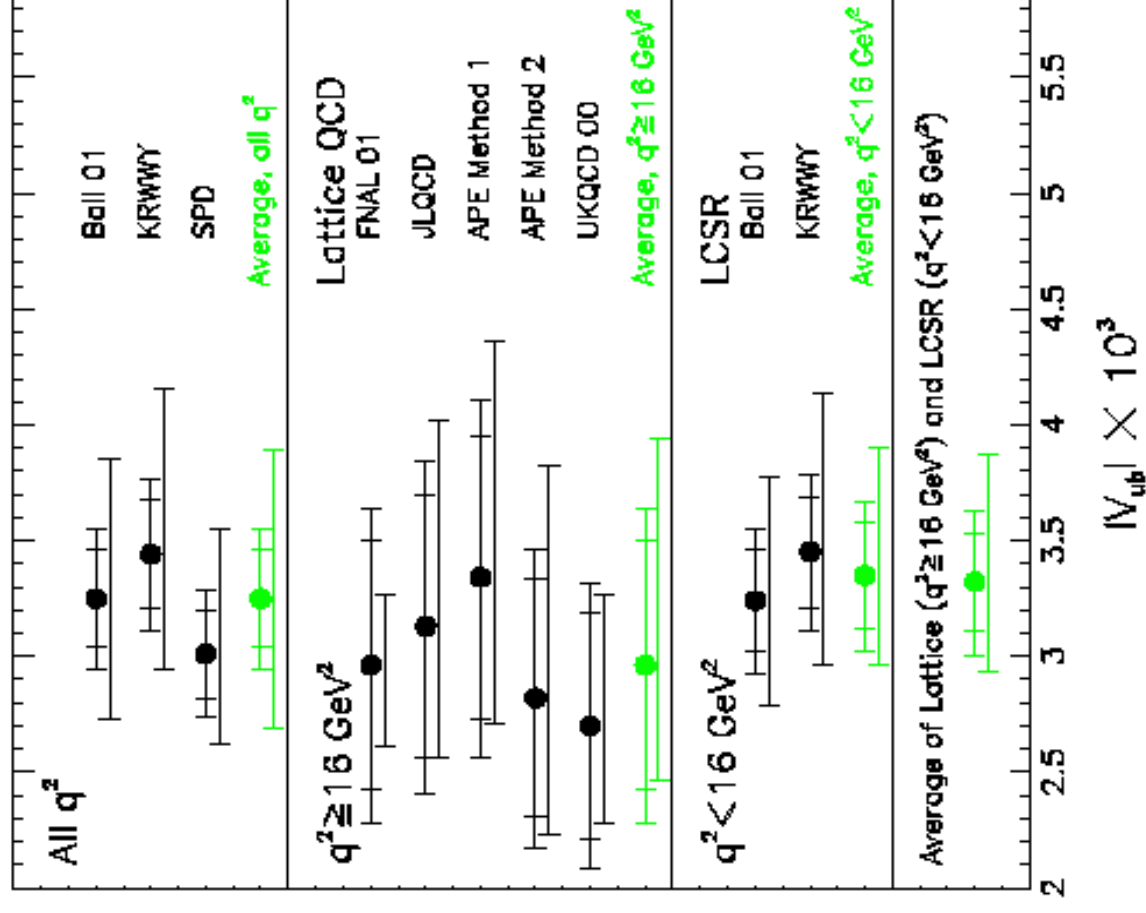


CLEO PRELIMINARY $B \rightarrow \pi \ell \bar{\nu}$



Observe $\text{Prob}(\text{ISGW-II}) < 1\%$
 making it unreliable for $|V_{ub}|$ extraction.

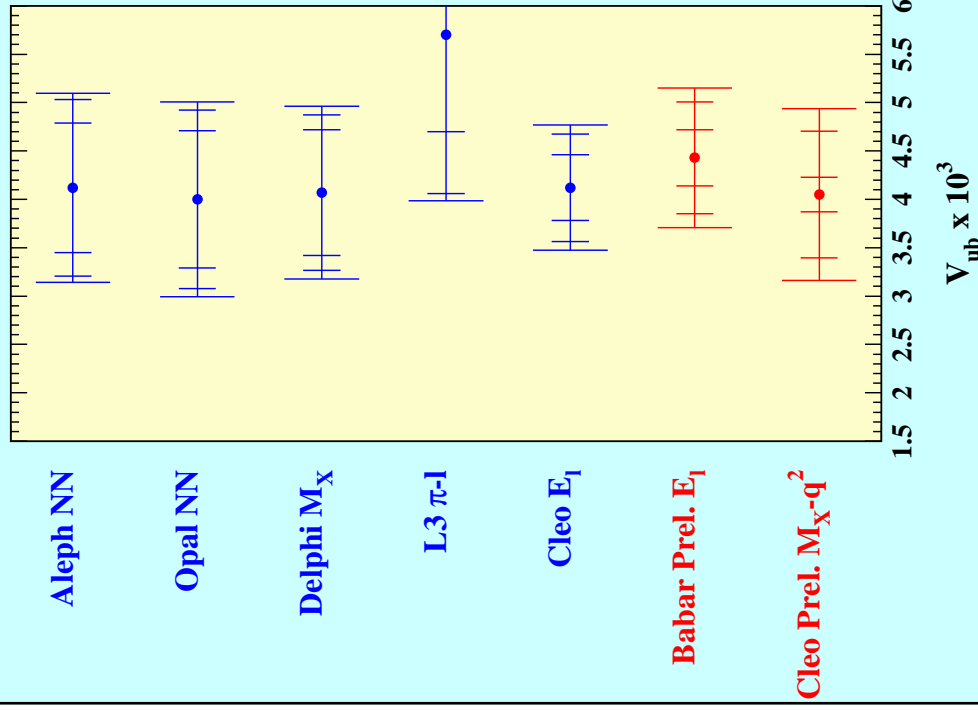
CLEO includes Lattice results for high q^2 ;



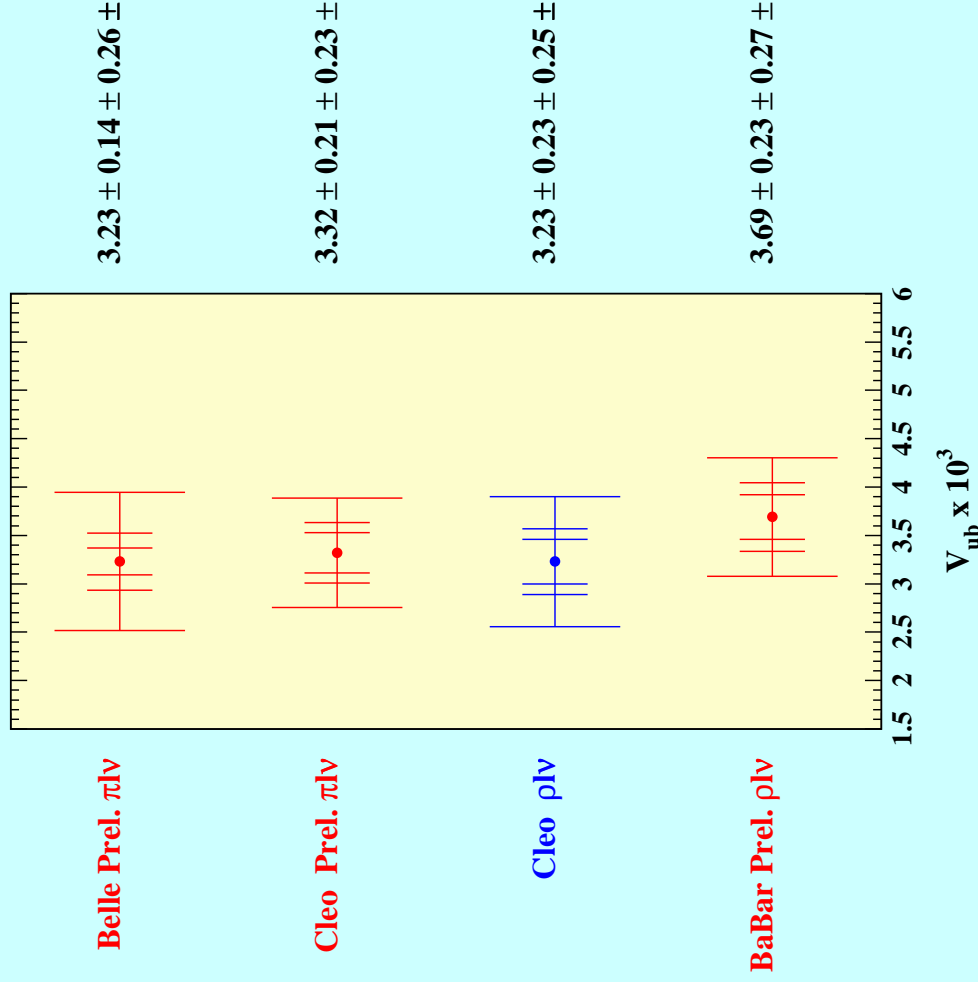
Status of $|V_{ub}|$ Determinations

$$|V_{ub}| \times 10^3$$

Inclusive Determinations



Exclusive Determinations



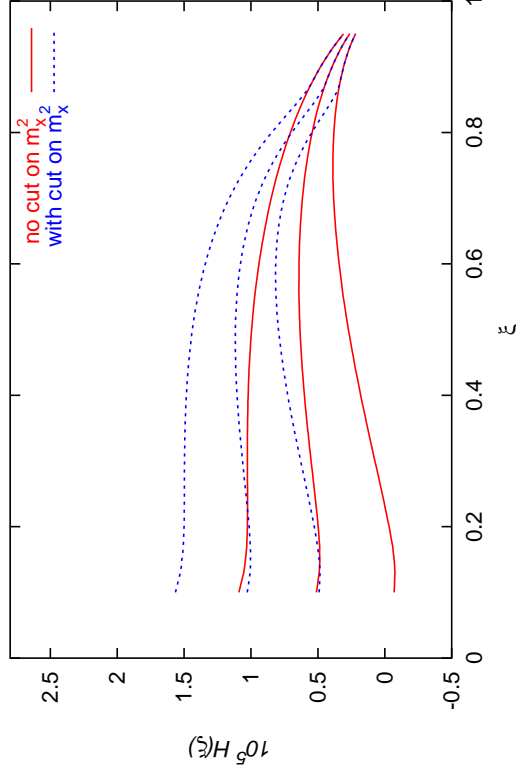
Other Paths to $|V_{ub}|$

$|V_{ub}|$ from Direct Ratio of $s\gamma$ and $u\ell\bar{\nu}$ Spectra

Aglietti, Ciuchini & Gambino

$$\xi_{\text{sl}\nu} = \frac{2t}{1+t} \quad t = \sqrt{1 - \frac{M_X^2}{E_X^2}}$$

$$\frac{|V_{ub}|^2}{|V_{cb}|^2} = K \frac{d\Gamma}{d\xi_{\text{sl}\nu}} / \frac{d\Gamma}{dx_{s\gamma}} (x = \xi) (1 \pm 0.10)$$



$|V_{ub}|$ from $B \rightarrow D_s \pi$

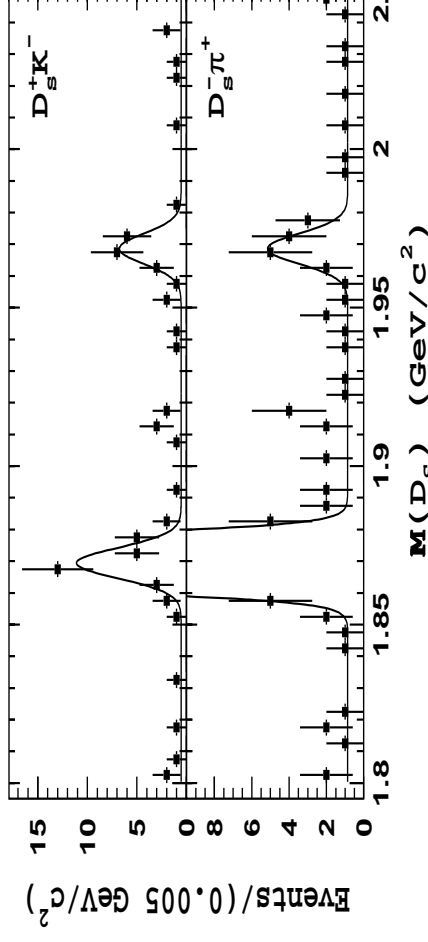
Kurimoto et al., Kim et al

BELLE PRELIMINARY

$$\frac{\Gamma(B^0 \rightarrow D_s^+ \pi^-)}{\Gamma(B^0 \rightarrow D_s^+ D^-)} = (0.424 \pm 0.041) \frac{|V_{ub}|}{|V_{cb}|}$$

$$= (3.0_{-1.6}^{+1.8}) \times 10^{-3}$$

$$|V_{ub}| = (3.25 \pm 1.0) \times 10^{-3}$$



V_{cb}



$$|V_{cb}|$$

Inclusive Determinations

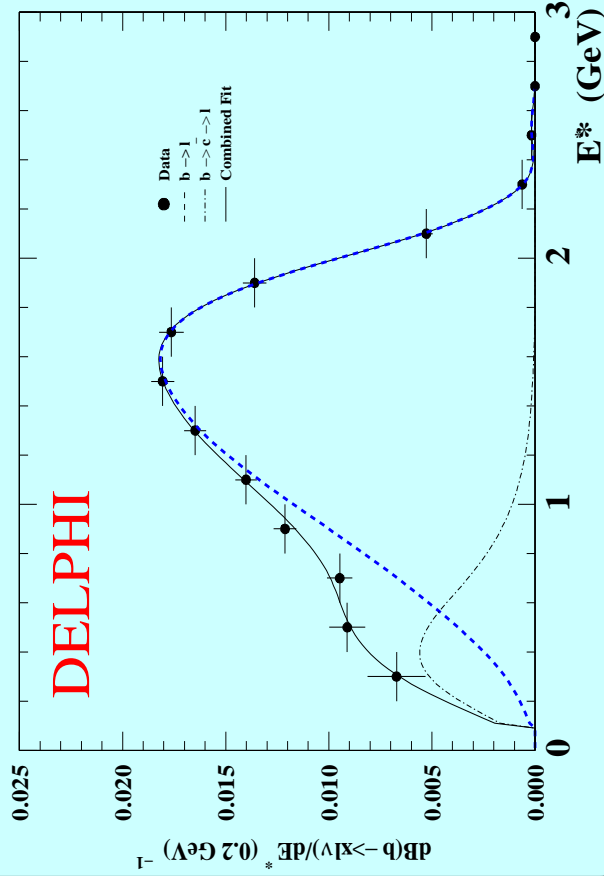
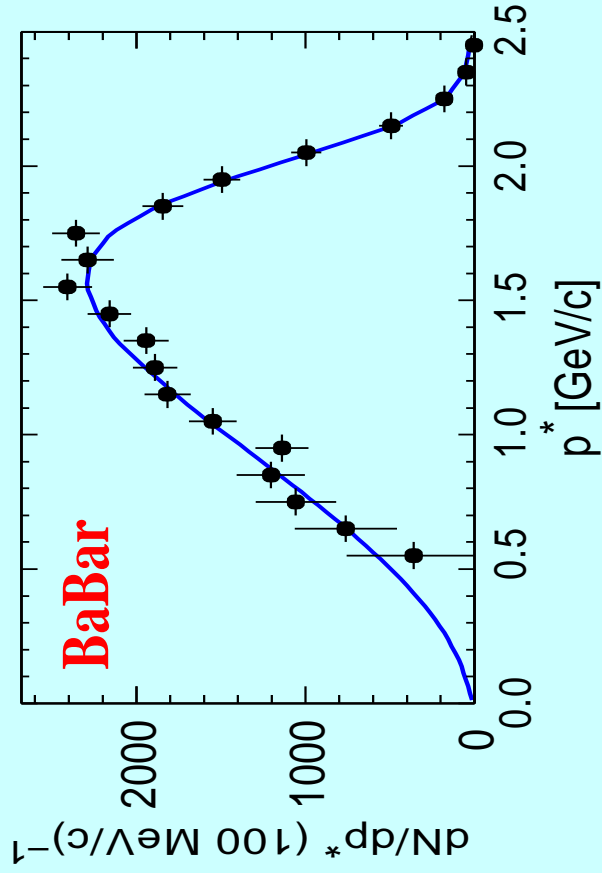
$$\Gamma(b \rightarrow X_c \ell \bar{\nu}) = \frac{\text{BR}(B \rightarrow X_c \ell \bar{\nu})}{\tau_b} = K(m_b, \lambda_1, \dots) \times |V_{cb}|^2$$

- ⇨ Accurate determinations of s.l. branching fraction $\text{BR}(b \rightarrow X \ell \bar{\nu})$ and of b -lifetime τ_b :

$$\text{BR}(b \rightarrow X_c \ell \bar{\nu}) = (10.46 \pm 0.29)\% \quad \tau_b = 1.573 \pm 0.007 \text{ ps}$$
- ⇨ Experimental accuracy on $|V_{cb}|$ close to 1% makes control of theory systematics crucial;

$$|V_{cb}| = 0.0415 \times (1 - 0.012(\mu_\pi^2) - 0.01(m_b(1 \text{ GeV})) + 0.006(\alpha_s) + 0.007(\rho_D^3))$$
- ⇨ Use $\bar{\Lambda}$, λ_1 results of moment analyses to absorb bulk of m_b and μ_π^2 systs. into expt. uncertainties: remaining theory systs due to $1/m_Q^3$ corrections, α_s , scale, ...

$$|V_{cb}| = (40.7 \pm 0.6 \pm 0.8) \times 10^{-3} \quad (V_{cb} \text{ WG})$$



DETERMINATIONS OF $\text{BR}(b \rightarrow X\ell\bar{\nu})$

Expt.	BR	stat	syst
CLEO	10.49	± 0.17	± 0.43
BELLE (ℓ Tag)	10.90	± 0.12	± 0.49
BABAR (e Tag)	10.87	± 0.18	± 0.30
AVERAGE	10.63	± 0.19	± 0.16

Expt.	BR	stat	syst	model
ALEPH	10.70	± 0.10	± 0.23	± 0.2
DELPHI	10.70	± 0.08	± 0.21	$^{+0.44}$ $^{-0.30}$
L3	10.85	± 0.12	± 0.38	± 0.2
L3 (double tag)	10.16	± 0.13	± 0.20	± 0.2
OPAL	10.83	± 0.10	± 0.20	$^{+0.20}$ $^{-0.13}$
AVERAGE	10.63	± 0.09	± 0.15	± 0.1

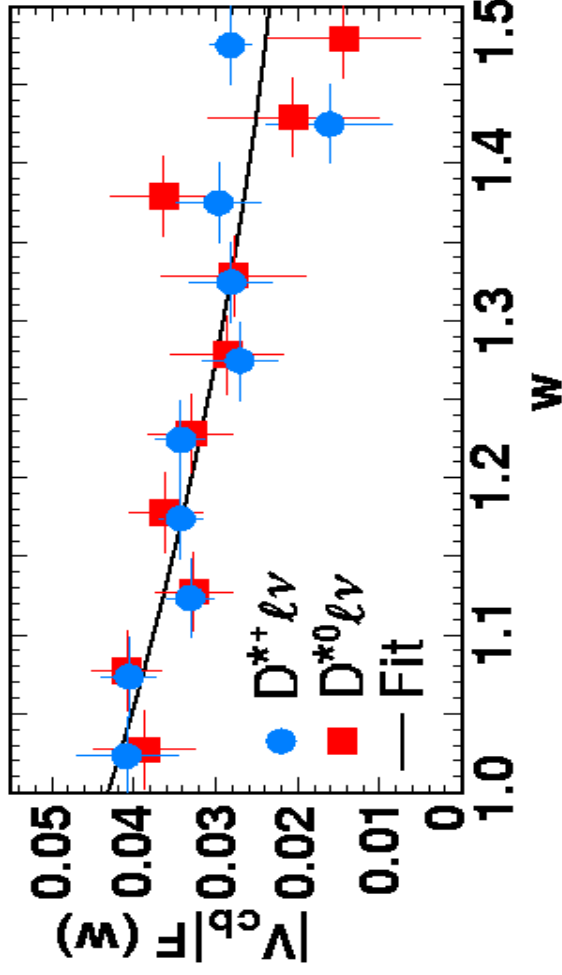
$\Gamma(b \rightarrow X_c \ell \nu) = 0.434 \times (1 \pm 0.018) 10^{-10} \text{ MeV}$

LEP+ $\Upsilon(4S)$ V_{cb} WG Average

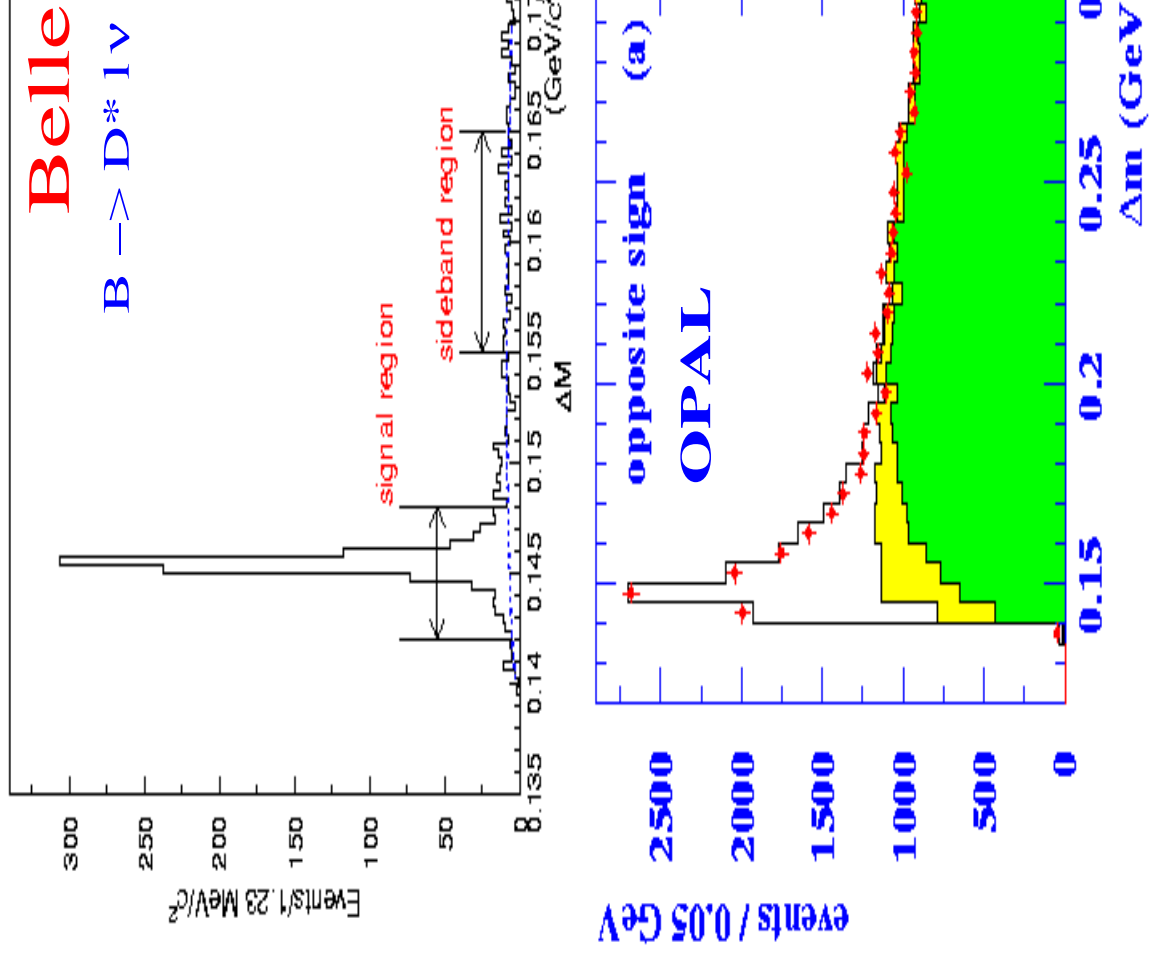
Exclusive Determinations

$$\frac{d\Gamma(B \rightarrow D^* \ell \bar{\nu})}{dw} = \frac{G_F^2 \mathcal{K}(w)}{48\pi^3} (F(w) |V_{cb}|)^2$$

$$w = \frac{M_{D^{*+}}^2 + M_{B^0}^2 - q^2}{2M_{D^{*+}} M_{B^0}^2}$$



\diamond Reconstruction of $B \rightarrow D^* \ell \bar{\nu}$ obtained either exclusively $D^* \rightarrow D\pi$, $D \rightarrow K\pi(\pi)$ or inclusively via $\Delta M = M_{X\pi} - M_X$



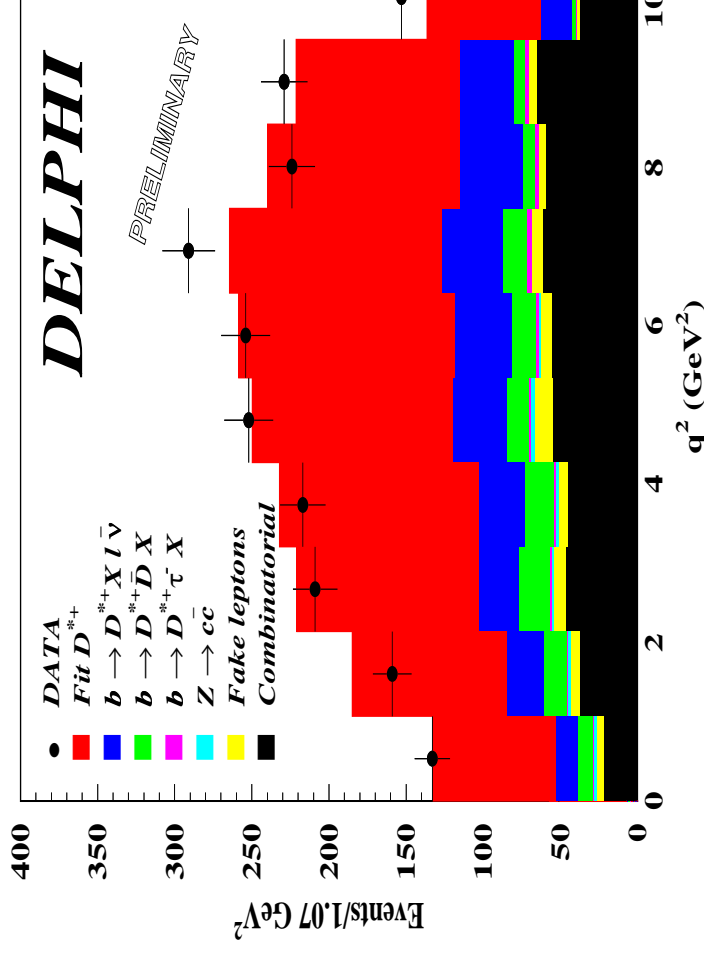
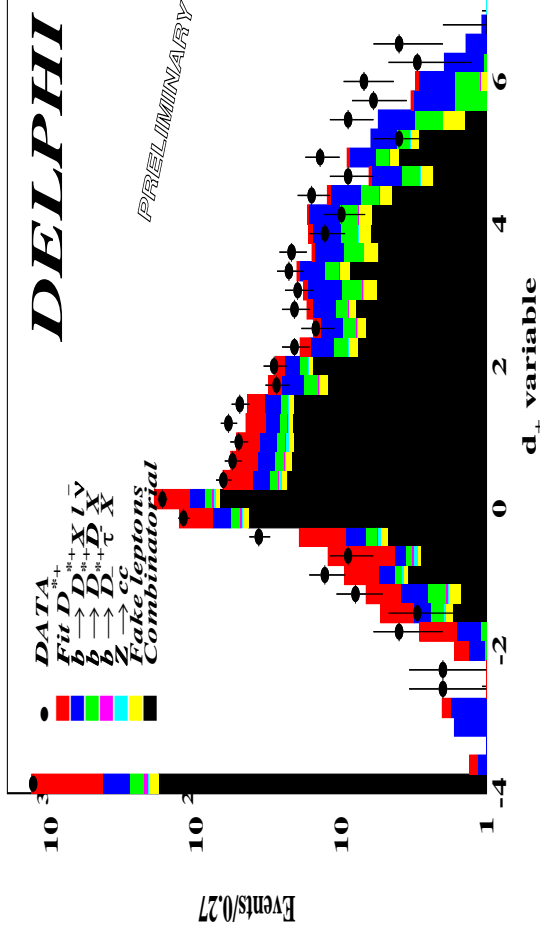
Delphi Exclusive $B^0 \rightarrow D^{*+} \ell^- \bar{\nu}$

PRELIMINARY

- ◆ Reconstruct $D^{*+} \rightarrow D^0 \pi^+$,
 $D^0 \rightarrow K^- \pi^+, K^- \pi^+ \pi^-, K^- \pi^+ (\pi^0)$;

$$q^2 = (p_{B^0} - p_{D^{*+}})^2$$

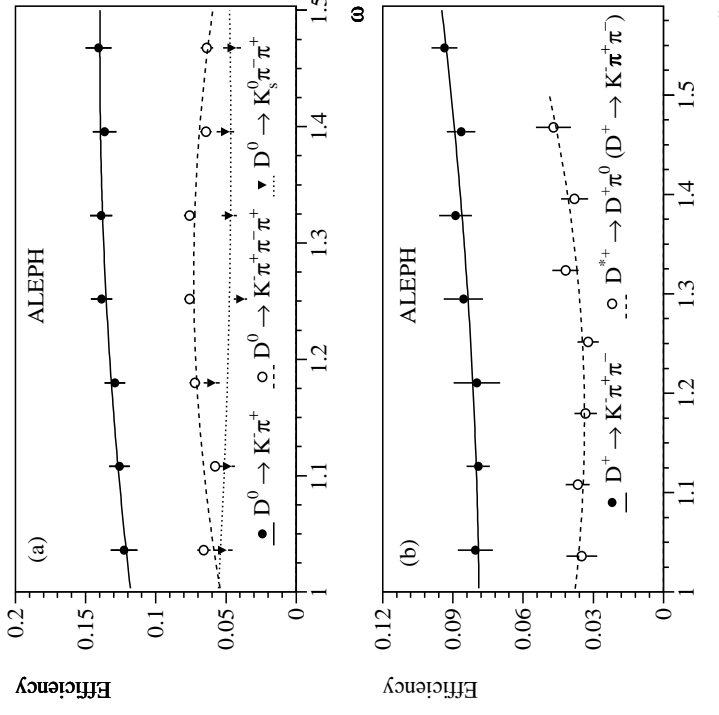
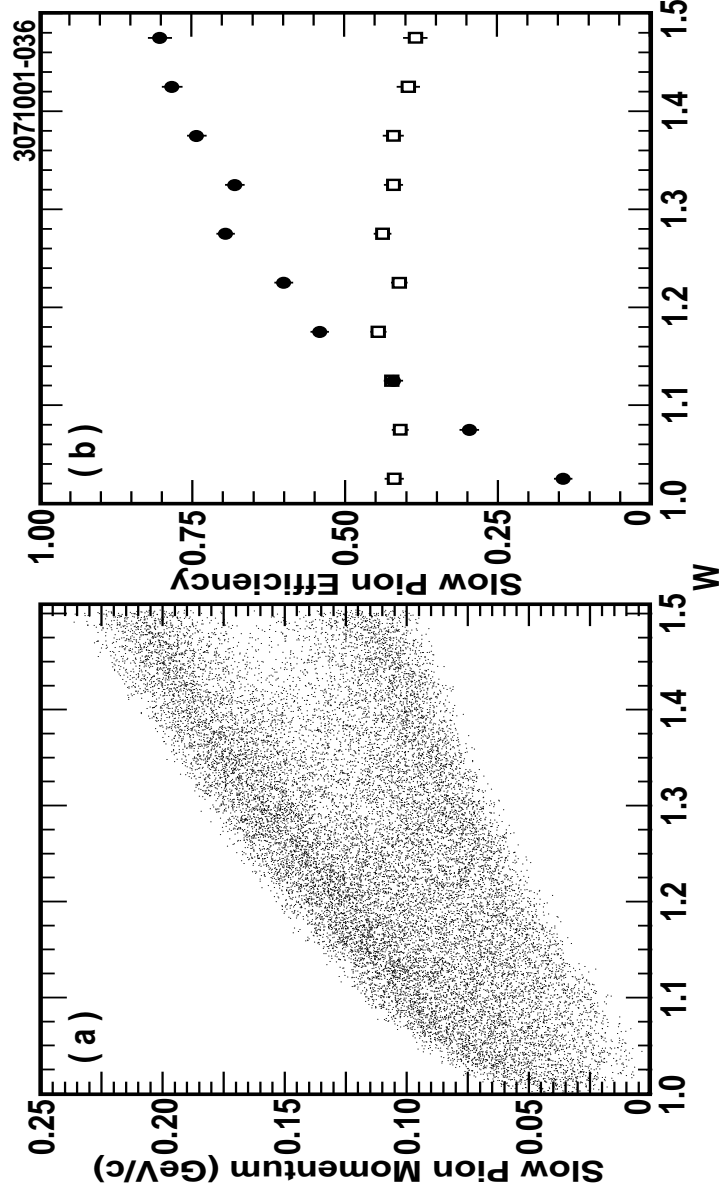
- ◆ verify $\epsilon(q^2)$ flat;
- ◆ identify $D^* X \ell \bar{\nu}$ and $b \rightarrow c \bar{c} s$ by discriminant based on tagged additional secondary tracks;
- ◆ fit event yield vs. q^2 leaving normalization of main components free;
- ◆ extract $\mathcal{F}(1) |V_{cb}|$, $\text{BR}(B^0 \rightarrow D^{*+} \ell^- \bar{\nu})$ and $\text{BR}(b \rightarrow D^{*+} X \ell^- \bar{\nu})$.



SUMMARY OF PROPERTIES OF $D^*\ell\bar{\nu}$ ANALYSES

Technique	ALEPH	BELLE	CLEO	DELPHI	OPAL	OPAL
	PLB395(97)	PLB526(02)	CLEO 01-26	PLB510(01)	PLB395(97)	PLB482 (0
	Excl	Excl	Excl	Incl	Excl	Incl
D^* Stats	579	766	2683	6495	1688	1708
$\frac{b \rightarrow D^* \ell \nu}{b \rightarrow D^*}$	0.86	0.85	0.90	0.72	0.70	0.77
δw	0.07	0.04	0.03	0.13	0.11	0.10
$\Delta \epsilon$	1.0	0.3	0.13/1.	1.0	1.0	1.0

RECONSTRUCTION EFFICIENCY VS. w

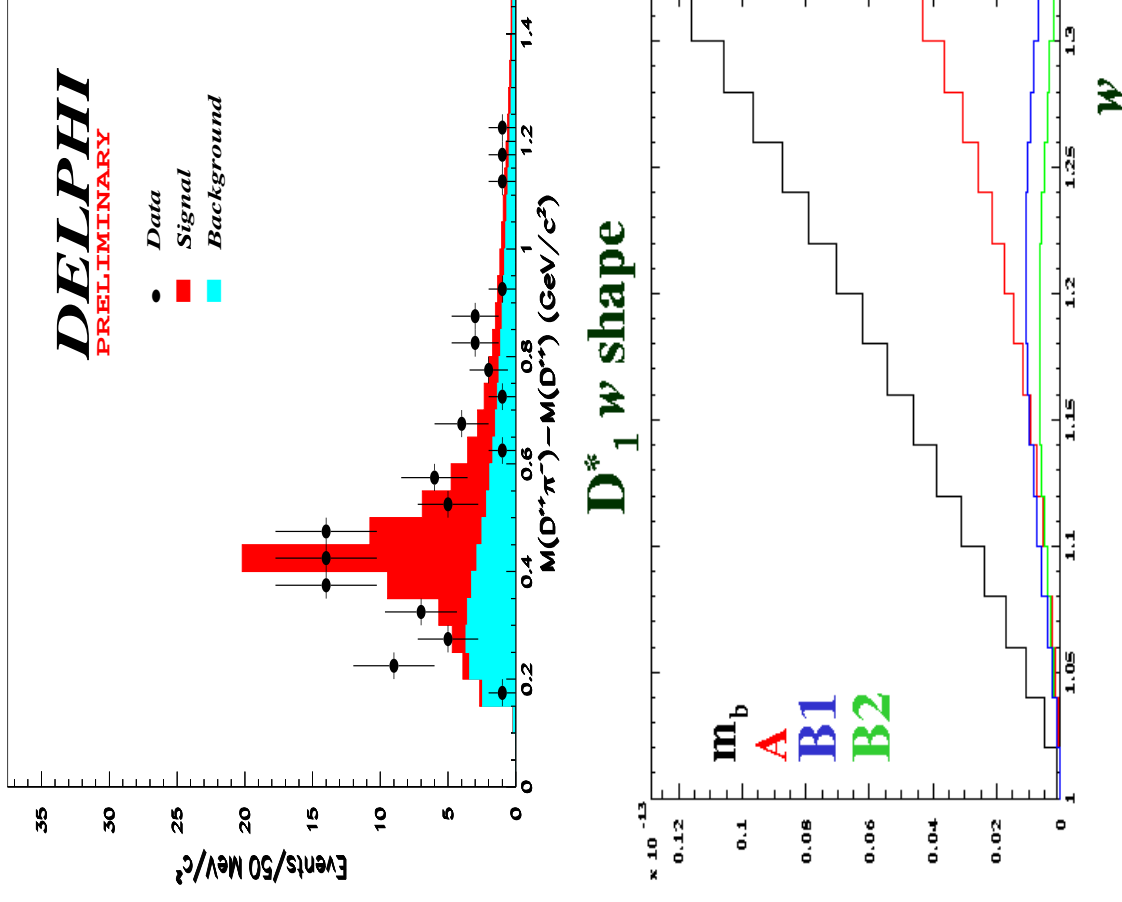


Issues in $|V_{cb}|$ D^{**} Background

- Important correlated syst. uncertainty from $b \rightarrow D^{**} \ell \bar{\nu}$ background;
- Data on narrow and broad D^{**} states becoming available but decay properties remain poorly known;
- Recent analyses fit $D^* X \ell \bar{\nu}$ fraction directly on data by angular distributions or track topology;

DELPHI PRELIMINARY

$$\text{BR}(b \rightarrow D^{*+} X \ell \bar{\nu}) = (0.64 \pm 0.08 \pm 0.09)\%$$



Issues in $|V_{cb}|$ Uncertainties: $\mathcal{F}(1)$

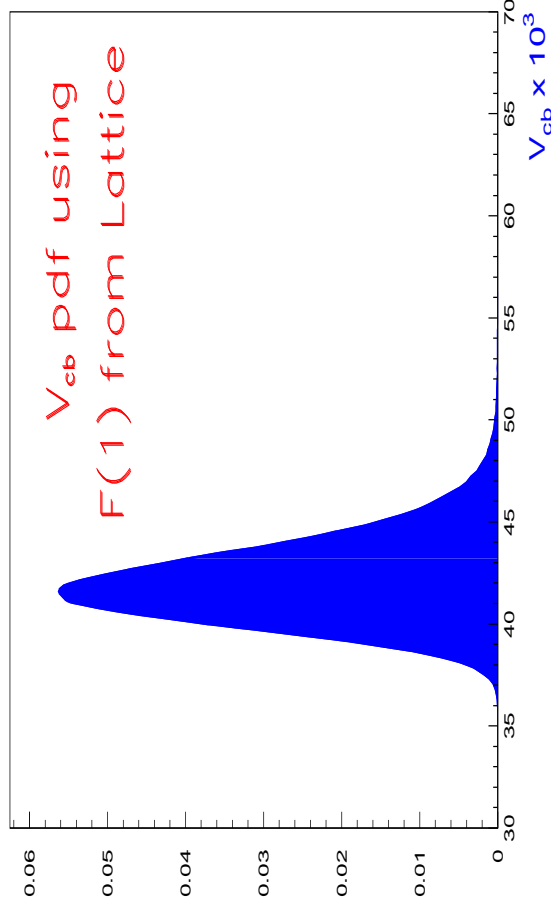
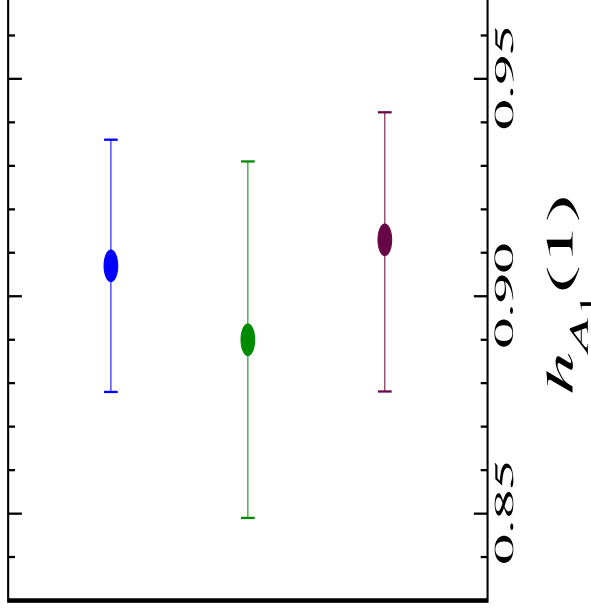
Hashimoto et al. hep-ph0110253

- Form factor \mathcal{F} at zero recoil computed with quark model, sum rule and quenched lattice QCD;
- thorough review of error budget from lattice;
- present value derived from sum rules and lattice QCD:

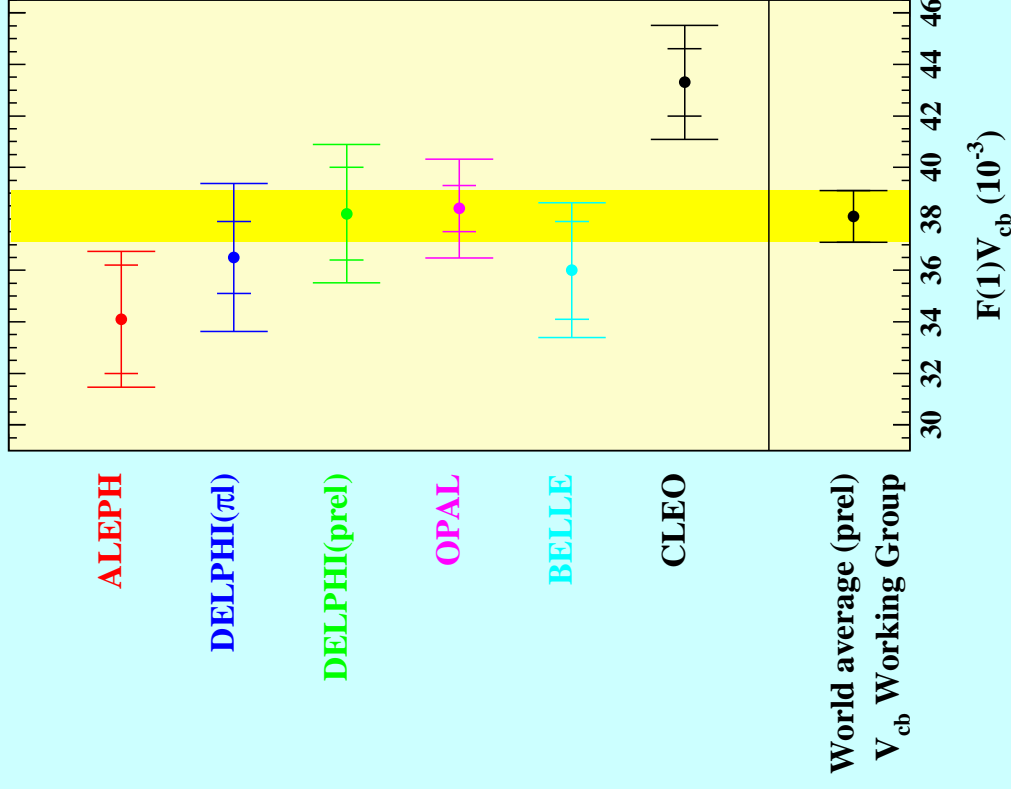
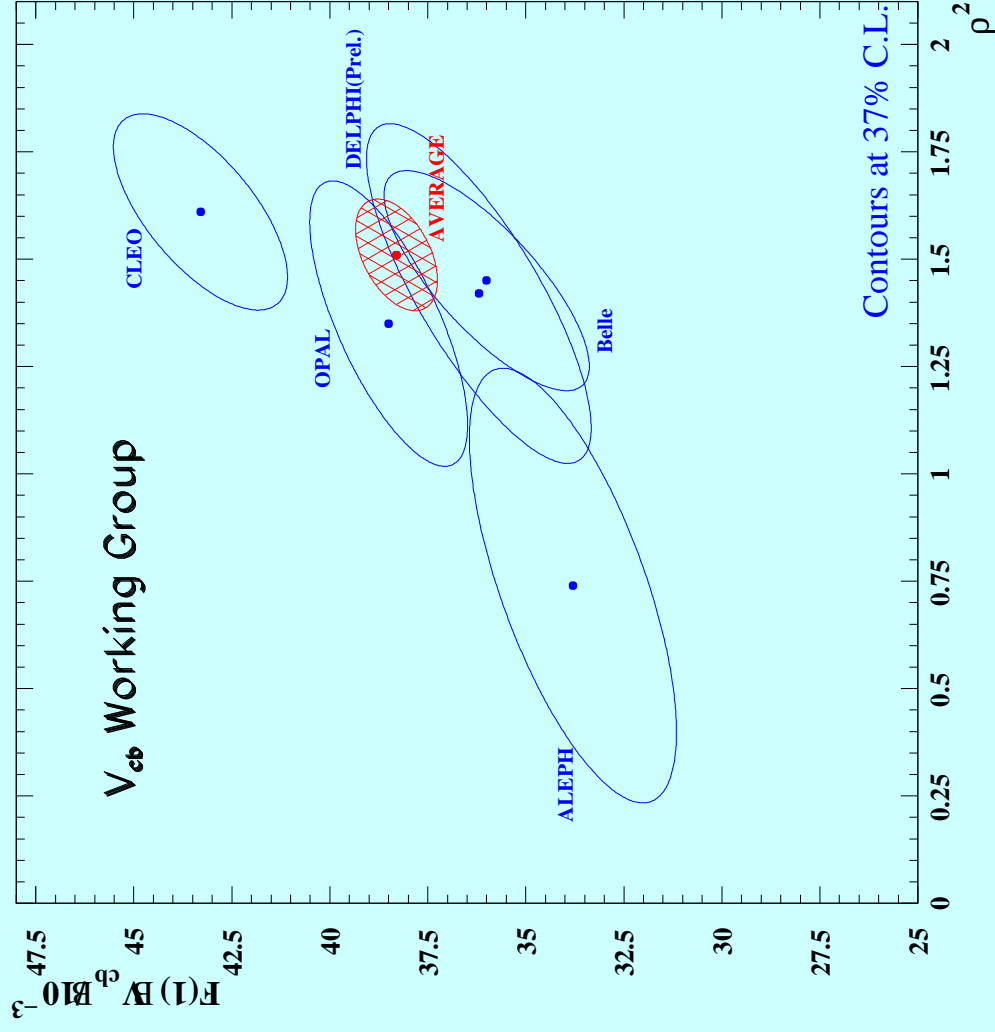
ADOPTED PDG VALUE FOR $\mathcal{F}(1)$

$$\mathcal{F}(1) = 0.91 \pm 0.04$$

- effort to define p.d.f for $\mathcal{F}(1)$ to propagate to $|V_{cb}|$ dets. for CKM fits;



PRELIMINARY $\mathcal{F}(1) \times |V_{cb}|$ COMBINATION



✧ Relevant form factors (R_1 and R_2) need to be measured in future

$$|V_{cb}| = (41.9 \pm 1.1 \pm 1.9) \times 10^{-3}$$

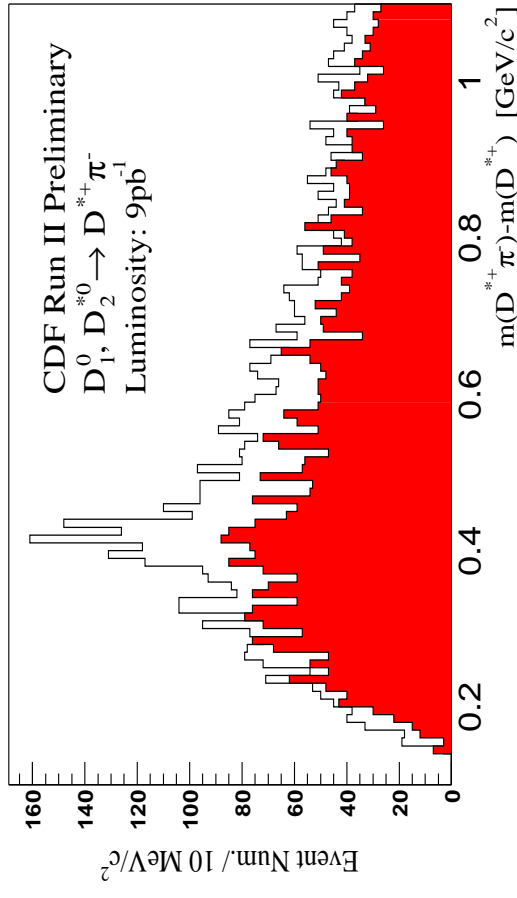
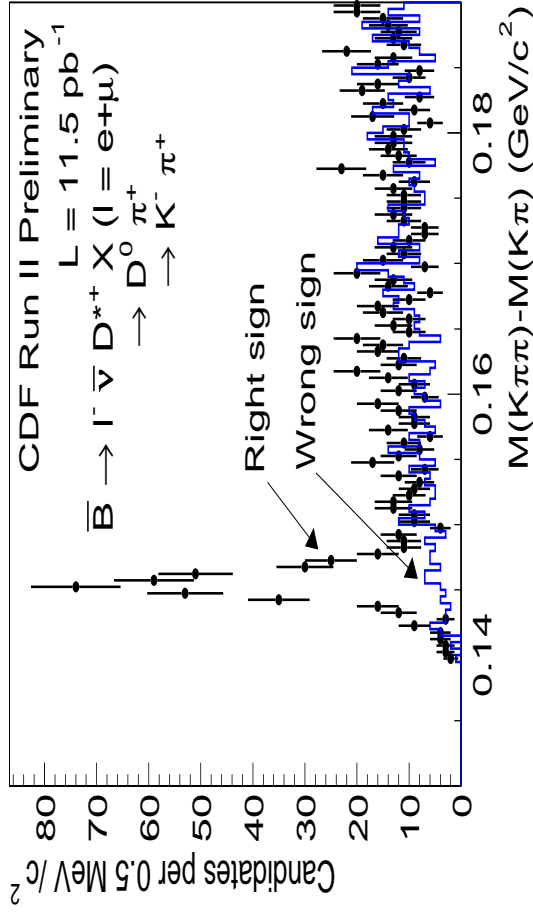
Signals from Tevatron Run II

CDF PRELIMINARY

- First CDF $B \rightarrow D\ell\nu$ signals from $\ell + \text{Si Vertex Trigger}$ ($p_\ell > 4 \text{ GeV}$);
- $B \rightarrow D^*\ell\bar{\nu}$
- ICHEP 2002: $11 \text{ pb}^{-1} = 960 \text{ Evt}$ s
 \rightarrow End of Run II: $2 \text{ fb}^{-1} = 200\text{k Evt}$ s;
- interesting to explore δw resolution and potential for $|V_{cb}|$

$$B \rightarrow D^{**}X$$

- Large D^{**} samples available for helicity analyses, measure M, Γ, BRs ;

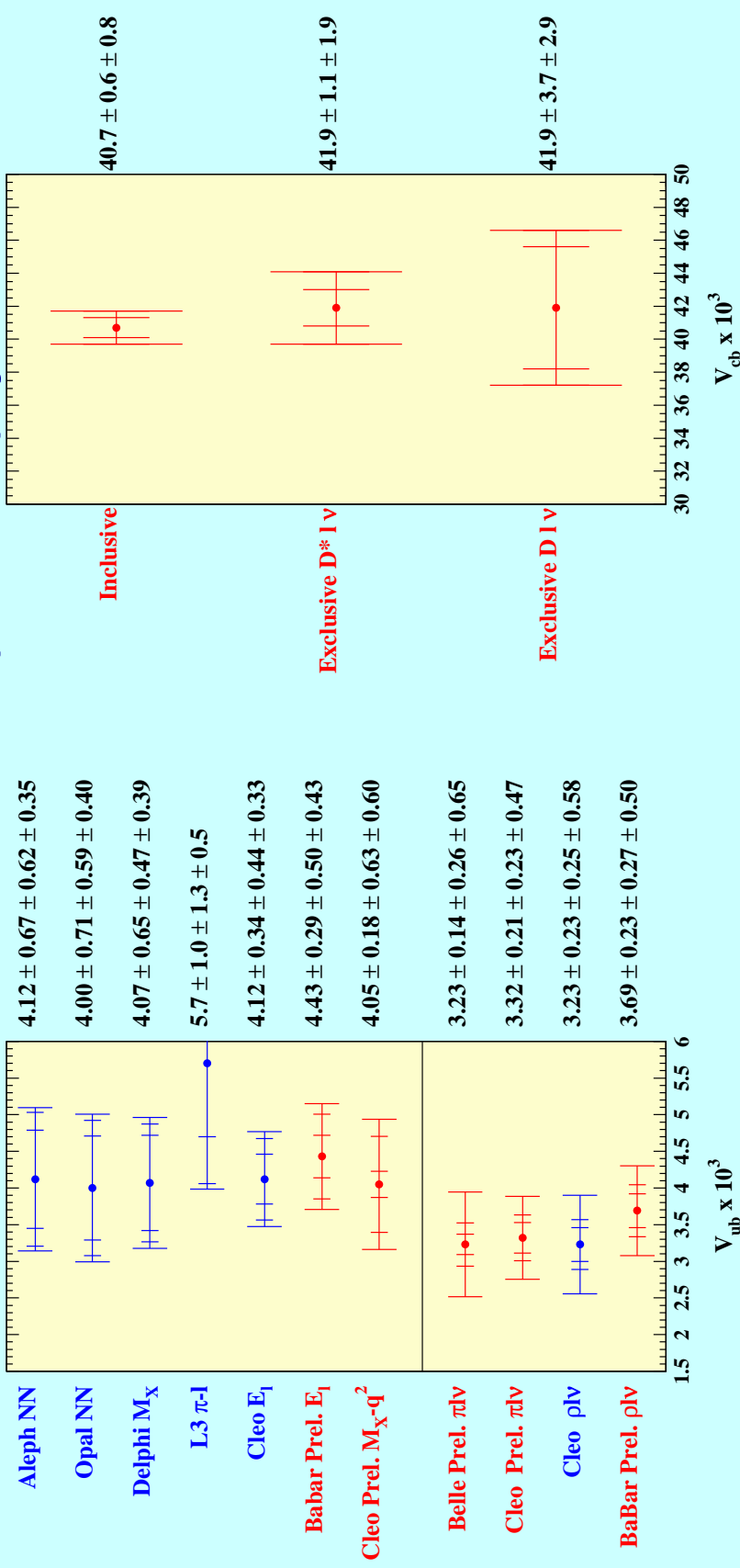


Summary



Large set of determinations of $|V_{ub}|$ and $|V_{cb}|$ exploiting different techniques affected by different assumptions and sources of uncertainties;

Overall consistency encouraging for perspectives to bring $|V_{ub}|$ and $|V_{cb}|$ towards the domain of precision physics:



Averaging inclusive and exclusive results can improve numerical accuracy due to partly uncorrelated uncertainties but needs a deeper understanding of systematics and thorough checks of consistency to \simeq anticipated total error.



V_{ub}

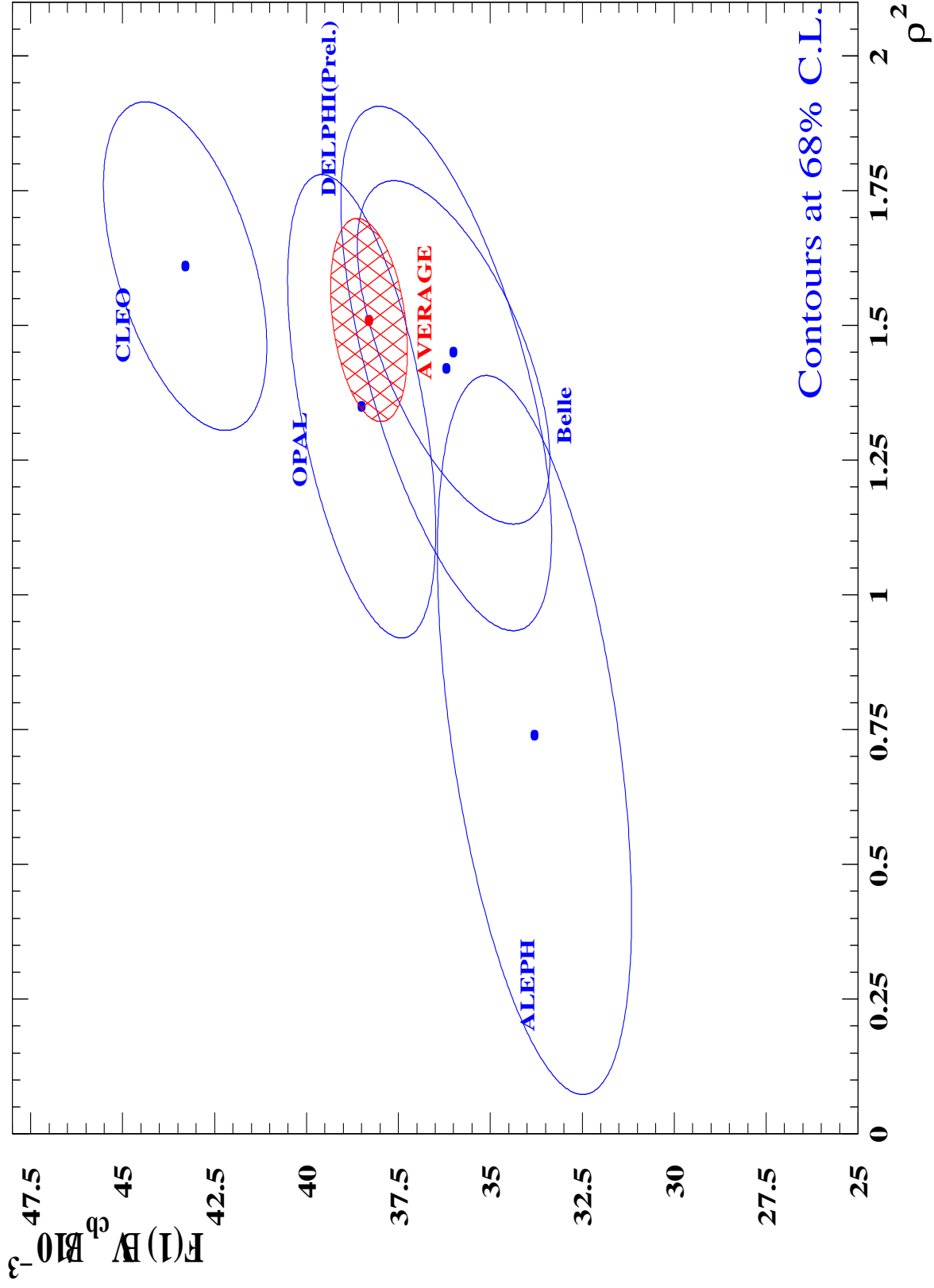


Livermore



V_{cb}

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M Shapiro, A Stocchi, A Tricomi, N Uraltsev, A Warburton and J Vermeer



Contours at 68% C.L.