

Measurements of time dependent CP asymmetry in $B \rightarrow VV$ decays with BELLE

Ryosuke Itoh, KEK

representing

The Belle Collaboration

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Outline



1. Introduction

2. Full time-dependent angular analysis for $B^0 \rightarrow J/\psi K^{*0}$

3. Time-integrated angular analysis for

a) $B^0 \rightarrow D^{*+} D^{*-}$

b) $B^0 \rightarrow D^{*-} \rho^+$

c) $B^+ \rightarrow \rho^+ \rho^0$

4. Summary

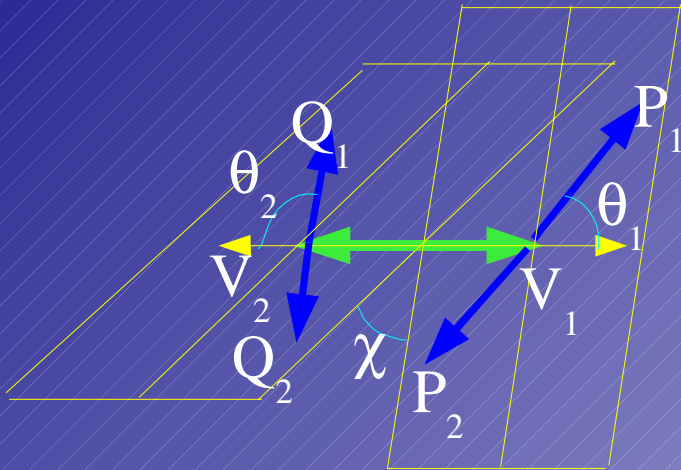
1. Introduction

- There are 3 helicity states in the final state of $B \rightarrow VV$ decay
- CP even and odd states are mixed in the final states
→ causes the dilution in the CP asymmetry
- Using angular analysis, it is possible to project out each CP state in a statistical way.
→ useful to minimize the dilution

Definition of angles

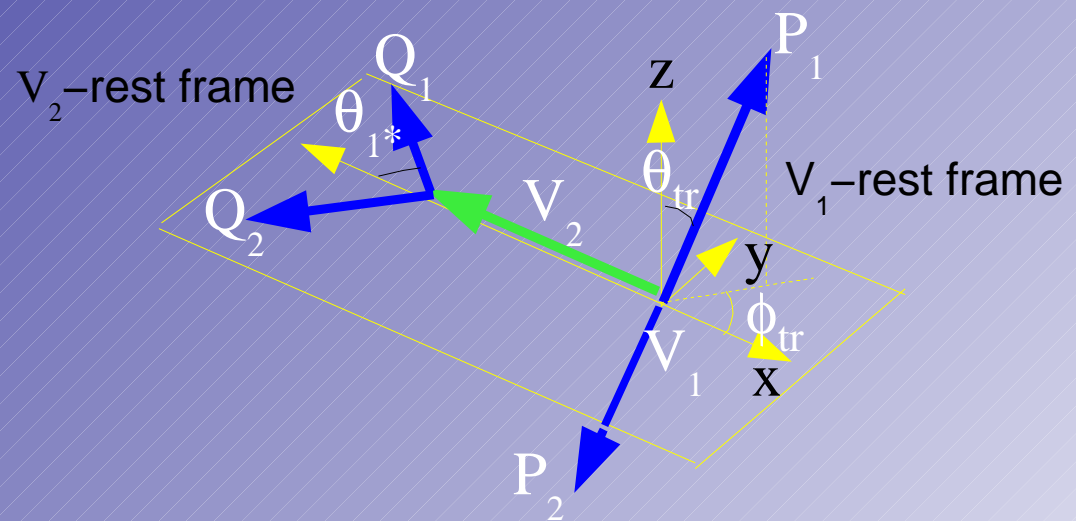
Two definitions of angles

$$\begin{aligned}
 B &\rightarrow V_1 V_2 \\
 V_1 &\rightarrow P_1 P_2 \\
 V_2 &\rightarrow Q_1 Q_2
 \end{aligned}$$



Helicity Basis


– Conventional definition



Transversity Basis

– θ_{tr} can directly be related to CP state of the system

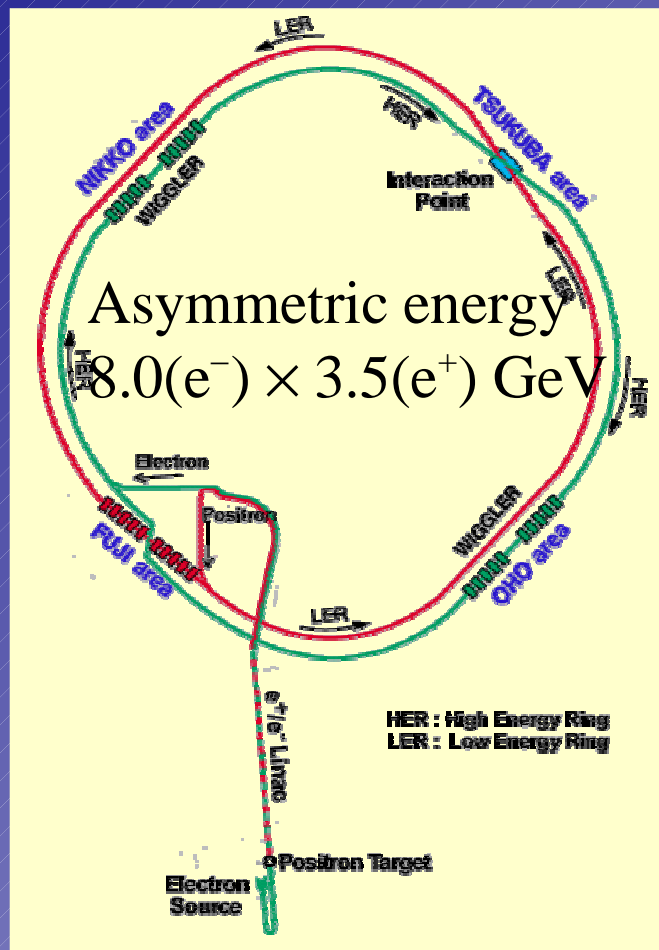
CP violation in angular distribution

- There are 6 components in the differential angular cross section for $B \rightarrow VV$ decay.
 - components for **three helicity states** (3)
 - components for **interferences between helicity states** (3)
- Each term is a product of **angular term** and **amplitude term**.
- Amplitude terms contain CP violating phase(s) as a function of Δt (decay time difference between two B mesons from $Y(4S)$ decay)
i.e. $\sin 2\phi_w \sin \Delta m \Delta t$, etc.

Fitting measured angles and Δt to the cross section formula
→ determination of ϕ_w
- Interference term is a rich source of interesting physics
 - $\cos 2\phi_1$ measurement ($J/\psi K^*$)
 - simultaneous determination of r and $\sin(2\phi_1 + \phi_3)$ ($D^* \rho$)

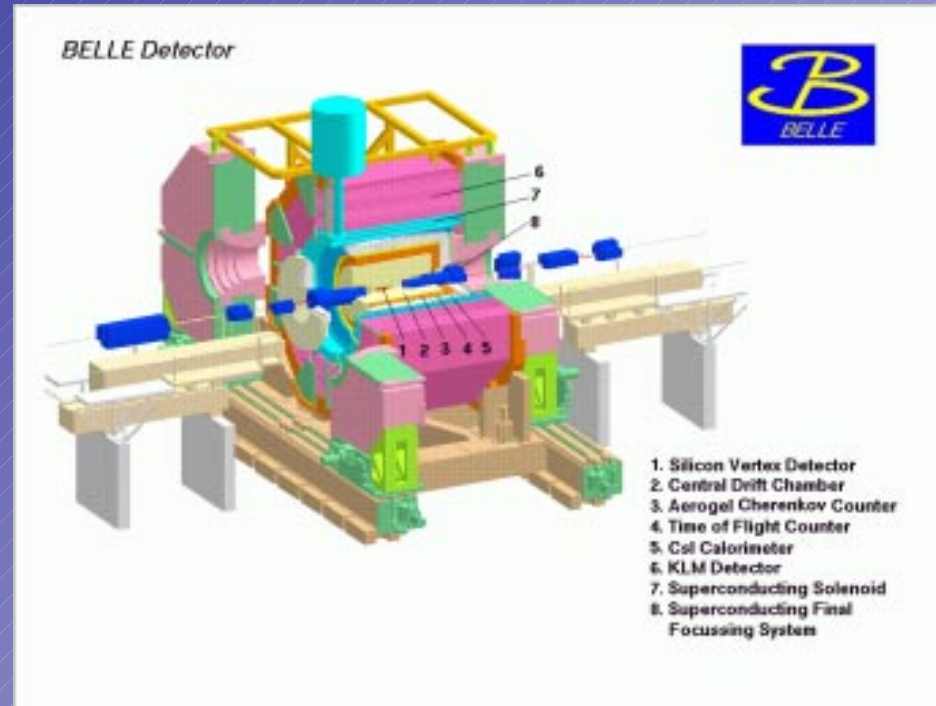
Belle

B factory experiment at KEK in Japan

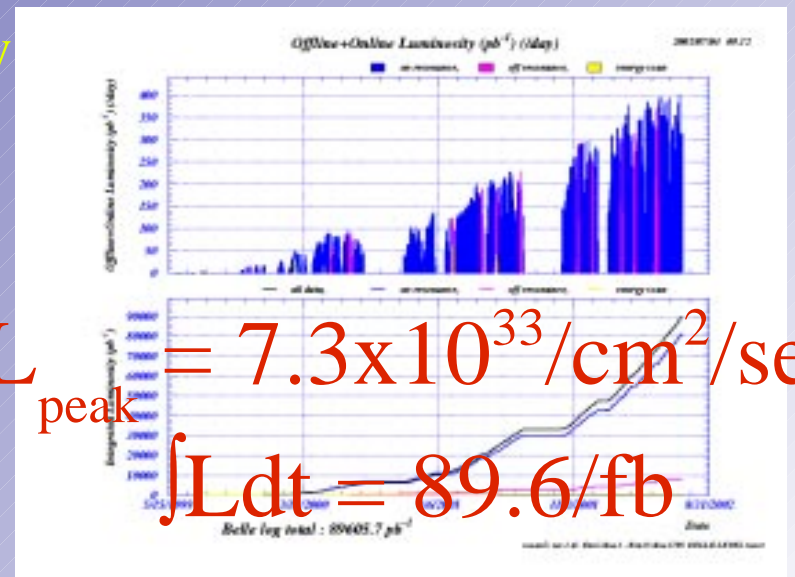
KEKB Accelerator



Belle Detector



Luminosity



$$L_{\text{peak}} = 7.3 \times 10^{33} / \text{cm}^2 / \text{sec}$$

$$\int L dt = 89.6 / \text{fb}$$

2. $B^0 \rightarrow J/\psi K^{*0} (K_S \pi^0)$

Integrated luminosity used for the analysis : 78fb^{-1}

Event selection :

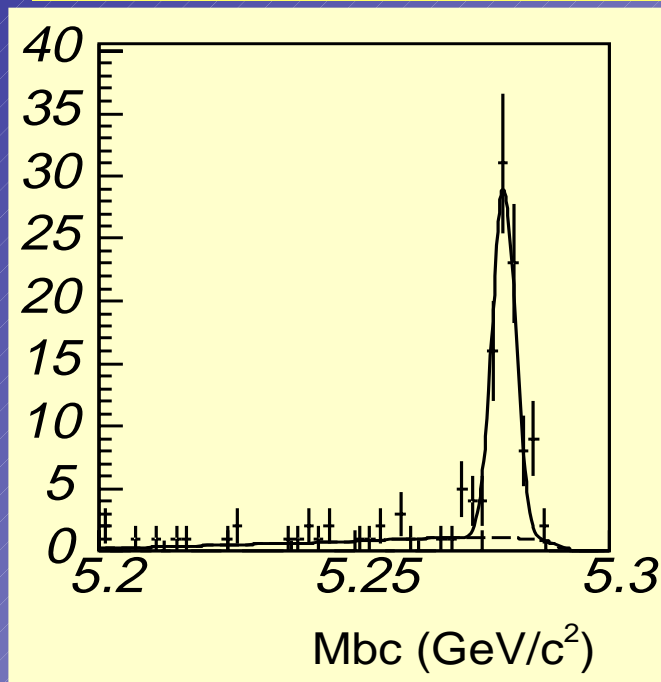
J/ψ : reconstructed using dilepton(e^+e^- , $\mu^+\mu^-$) decay.

K^* : $|M(K_S \pi^0) - M(K^{*0})| < 75\text{MeV}/c^2$

B^0 : $5.27 < M_{bc} < 5.29 \text{ GeV}/c^2$

$-0.05 < \Delta E < 0.03 \text{ GeV}$

slow π^0 rejection : $\cos \theta_1$ (K^* helicity angle) < 0.8



M_{bc} : invariant mass calculated assuming the energy to be beam energy

ΔE : difference between reconstructed B candidate and beam energy

→ 103 events remain

+ vertex quality selection

→ used for CP fit

* vertex reconstruction / flavor determination

→ covered by other talk

Time-dependent angular distribution

(Transversity basis)

$$\frac{d\Gamma}{d\cos\vartheta_{tr} d\phi d\cos\vartheta_{K^*} d\Delta t} = \frac{9}{32\pi} \frac{e^{-|\Delta t|/\tau_B}}{2\tau_B} \sum_{i=1,6} f_i(\vartheta_{tr}, \phi, \vartheta_{K^*}) a_i(\Delta t)$$

$$f_1 = 2\cos^2\vartheta_{K^*} (1 - \sin^2\vartheta_{tr} \cos^2\phi)$$

$$a_1 = |A_0|^2 (1 + \eta \sin 2\phi_1 \sin \Delta m \Delta t)$$

$$f_2 = \sin^2\vartheta_{K^*} (1 - \sin^2\vartheta_{tr} \sin^2\phi)$$

$$a_2 = |A_{//}|^2 (1 + \eta \sin 2\phi_1 \sin \Delta m \Delta t)$$

$$f_3 = \sin^2\vartheta_{K^*} \sin^2\vartheta_{tr}$$

$$a_3 = |A_T|^2 (1 - \eta \sin 2\phi_1 \sin \Delta m \Delta t)$$

$$f_4 = \frac{-1}{\sqrt{2}} \sin 2\vartheta_{K^*} \sin^2\vartheta_{tr} \sin 2\phi$$

$$a_4 = \Re(A_{//}^* A_0) (1 + \eta \sin 2\phi_1 \sin \Delta m \Delta t)$$

$$f_5 = \sin^2\vartheta_{K^*} \sin 2\vartheta_{tr} \sin \phi$$

$$a_5 = \eta \Im(A_{//}^* A_T) \cos \Delta m \Delta t - \eta \Re(A_{//}^* A_T) \cos 2\phi_1 \sin \Delta m \Delta t$$

$$f_6 = \frac{1}{\sqrt{2}} \sin 2\vartheta_{K^*} \sin 2\vartheta_{tr} \cos \phi$$

$$a_6 = \eta \Im(A_0^* A_T) \cos \Delta m \Delta t - \eta \Re(A_0^* A_T) \cos 2\phi_1 \sin \Delta m \Delta t$$

* $A_0, A_{//}, A_T$: helicity amplitudes

* η : +1 for B^0 , -1 for \overline{B}^0

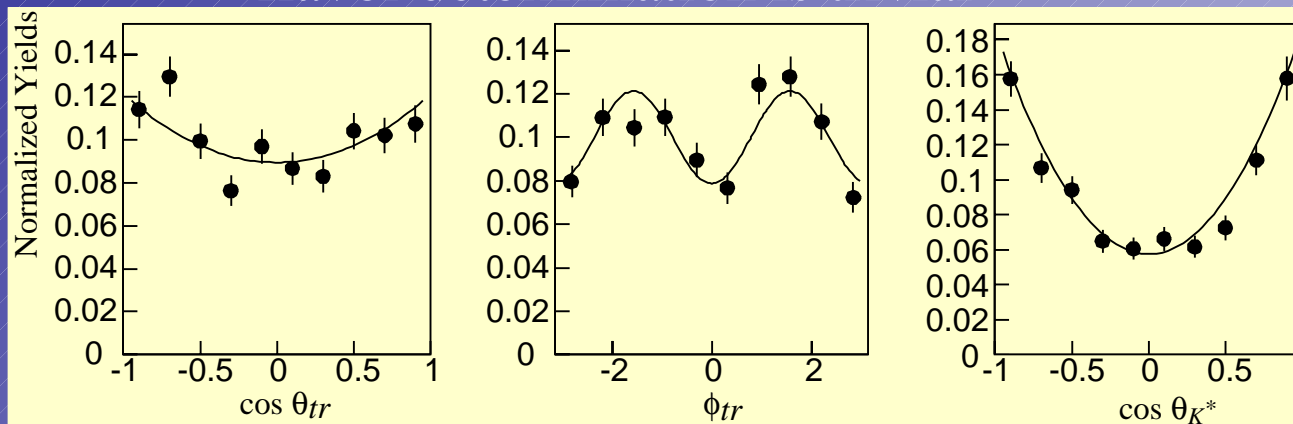
* $\Delta m, \tau_B$: mixing parameter, B lifetime

* ϕ_1 : CP violating angle (β)

$\cos 2\phi_1$ appears in interference terms! → useful to solve 2-fold ambiguity in $2\phi_1$ measured from $\sin 2\phi_1$

Time-integrated angular analysis BELLE-CONF-0213(ABS701)

- A_0 , $A_{//}$ and A_T can be determined by the fit to angular distributions only (time-integrated distributions).
- Non-CP decays ($B^0 \rightarrow J/\psi K^{*0}(K^+\pi^-)$, $B^+ \rightarrow J/\psi K^{*+}(K^+\pi^0, K_S^0\pi^+)$) are used (29.4/fb) ← * higher statistics than CP decay ($B^0 \rightarrow J/\psi K^*(K_S^0\pi^0)$)
- * flavor determination is trivial



$$|A_0|^2 + |A_{//}|^2 + |A_T|^2 = 1$$

$$\arg(A_0) = 0.0$$

$$|A_0|^2 = 0.62 \pm 0.02 \pm 0.03$$

$$|A_T|^2 = 0.19 \pm 0.02 \pm 0.03$$

$$\arg(A_{//}) = 2.83 \pm 0.19 \pm 0.08$$

$$\arg(A_T) = -0.09 \pm 0.13 \pm 0.06$$

Free parameters:
 $\sin 2\phi_1$ and $\cos 2\phi_1$

Probability Density Function (PDF) for CP fit

- Determination of $\sin 2\phi_1$ and $\cos 2\phi_1$ is done by the unbinned maximum likelihood fit to 3 transversity angles and Δt obtained event by event.
 - PDF for the fit is constructed with following effects
 - 1) Detector acceptance for angular distributions
 - as done for time–integrated analysis
 - parameterized 3D efficiency function obtained by MC
 - 2) Background fractions and angular shapes
 - * feed across from other $J/\psi K^*$ subdecays
 - * non–resonant production of $B \rightarrow J/\psi + K + \pi$
 - * combinatorial background
 - obtained from MC and M_{bc} sideband data
 - angular shapes are parameterized in 3D polynomials.
 - 3) Δt resolution of measurement
 - 4) Wrong tagging effect
-) treated in the same manner as those
in Belle's standard CP analysis

$$\begin{aligned}
PDF(M_{bc}, \vartheta_{tr}, \phi_{tr}, \vartheta_{K^*}, \Delta t) = & \\
& f_{sig}(M_{bc}) eff(\vartheta_{tr}, \phi_{tr}, \vartheta_{K^*}) TADF(\vartheta_{tr}, \phi_{tr}, \vartheta_{K^*}, \Delta t; \phi_1) \\
& + \sum_{BG \text{ sources}} f_{bg}(M_{bc}) TADF_{BG}(\vartheta_{tr}, \phi_{tr}, \vartheta_{K^*}, \Delta t)
\end{aligned}$$

Background TADF :

$$\begin{aligned}
\text{feed across : } & e^{-|\Delta t|/\tau_B} / 2\tau_B \times ADF_{fa}(\vartheta_{tr}, \phi_{tr}, \vartheta_{K^*}) \\
\text{non-resonant : } & e^{-|\Delta t|/\tau_B} / 2\tau_B \times ADF_{nr}(\vartheta_{tr}, \phi_{tr}, \vartheta_{K^*}) \\
\text{combinatorial : } & \delta(\Delta t) \times ADF_{combi}(\vartheta_{tr}, \phi_{tr}, \vartheta_{K^*})
\end{aligned}$$

* η is replaced with $-q(1-2w)$ in signal TADF

(q = tagging flavor (± 1), w = wrong tagging fraction)

* PDF is convoluted with proper resolution function for each term

Results

$$\sin 2\phi_1 = 0.13 \pm 0.51 \pm 0.06$$

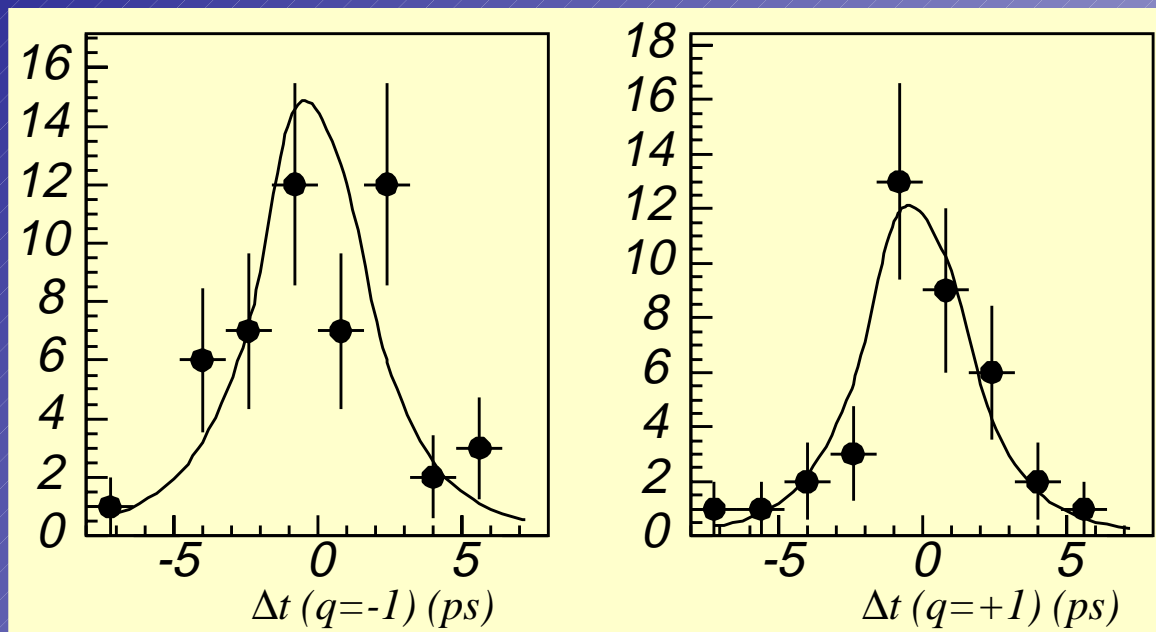
$$\cos 2\phi_1 = 1.40 \pm 1.28 \pm 0.19$$

$$\text{c.f. 2D fit } (\cos\theta_{\text{tr}} \text{ only}) : \sin 2\phi_1 = 0.04 \pm 0.64$$

Systematic error estimation

Item	$\delta\sin 2\phi_1$	$\delta\cos 2\phi_1$
Resolution parameters	± 0.024	± 0.092
Wrong tagging fractions	± 0.019	± 0.041
Helicity amplitudes	± 0.042	± 0.158
Background fraction	± 0.012	± 0.012
Angular shape for BG	± 0.023	± 0.034
Δt distribution for $\delta(t)$ BG	± 0.009	± 0.010
τ_B and Δm	± 0.013	± 0.011
Total	± 0.06	± 0.19

Δt distributions



Lines show the prediction by PDF with obtained CP parameter values

Discussion

– sign of $\cos 2\phi_1$

* 2-fold ambiguity in the choice in phases of helicity amplitudes
(M.Suzuki, PRD 64, 117503)

1) $\phi_{\parallel} = 2.8$ rad., $\phi_{\perp} = -0.09$ rad. (s-quark helicity conserved)

→ used to obtain shown values

2) $\phi_{\parallel} \rightarrow -\phi_{\parallel}$ and $\phi_{\perp} \rightarrow \pi - \phi_{\perp}$ (cannot exclude this)

→ the sign of $\cos 2\phi_1$ flips while $\sin 2\phi_1$ does not change

$$\cos 2\phi_1 = -1.31 \pm 1.28 \pm 0.19$$

– Comparison with other measurements

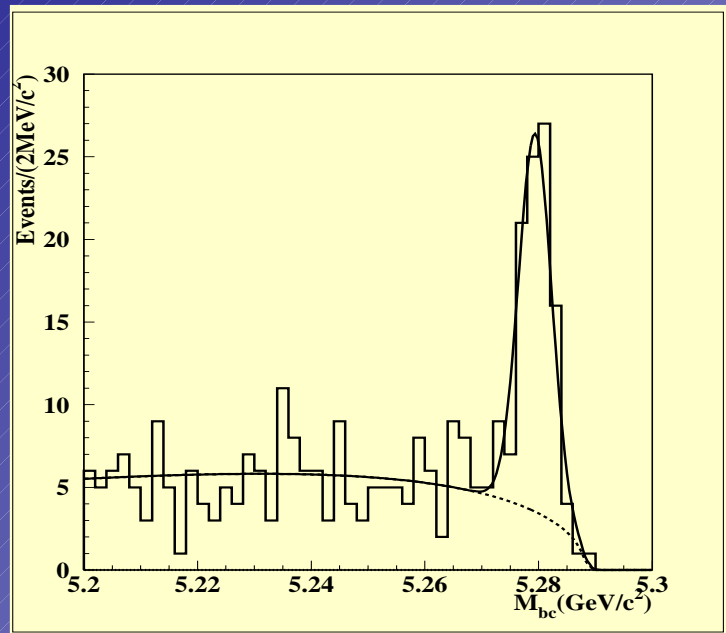
	$\sin 2\phi_1$	$\cos 2\phi_1$
BaBar	$0.22 \pm 0.52^{(*1)}$	$+3.3 (+0.6-1.0) (+0.6-0.7)^{(*2)}$
Belle	$0.13 \pm 0.51 \pm 0.06$	$+1.40 \pm 1.28 \pm 0.19$
	0.82 (fixed) ^(*3)	$+1.02 \pm 1.16$

(*1) hep-ex/0207042, (*2) obtained in global CP fit, hep-ex/0203007, (*3) value shown at Moriond conf.

3. Other channels

- Time-dependent analysis is still in preparation for following modes.
- Status of time-integrated analysis is discussed

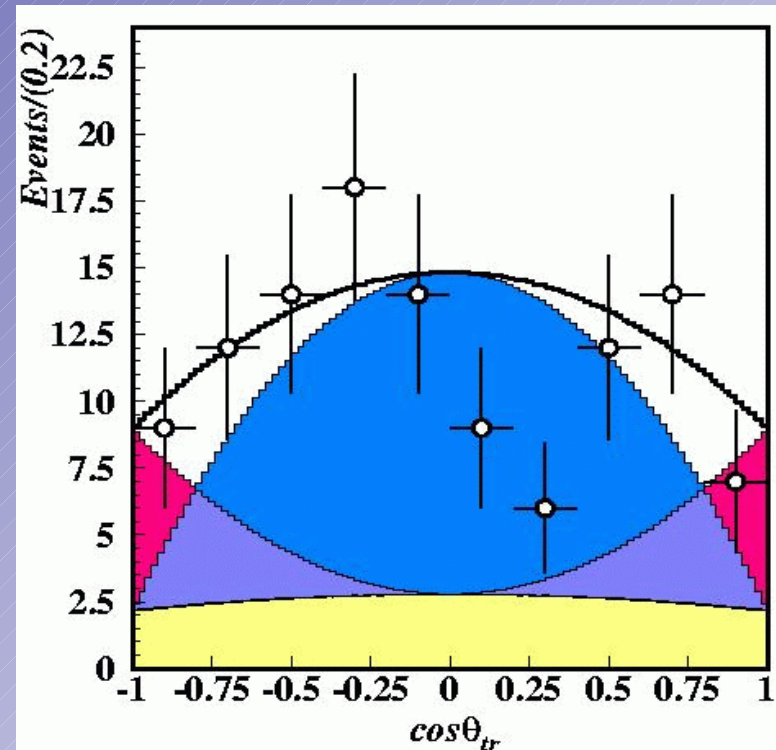
a) $B \rightarrow D^{*+} D^{*-}$ (for $\sin 2\phi_1$ determination)



$$Br(B \rightarrow D^{*+} D^{*-}) = (7.6 \pm 0.9 \pm 1.4) \times 10^{-4}$$

(with 78fb^{-1})

$$\frac{d\Gamma}{d \cos \vartheta_{tr}} = \frac{3}{4} (1 - R_T) \sin^2 \vartheta_{tr} + \frac{3}{2} R_T \cos^2 \vartheta_{tr}$$



b) $B \rightarrow D^* \rho$ (for $\sin(2\phi_1 + \phi_3)$ determination)

– Fit to projected helicity angles

→ Transversity amplitudes with imaginary parts

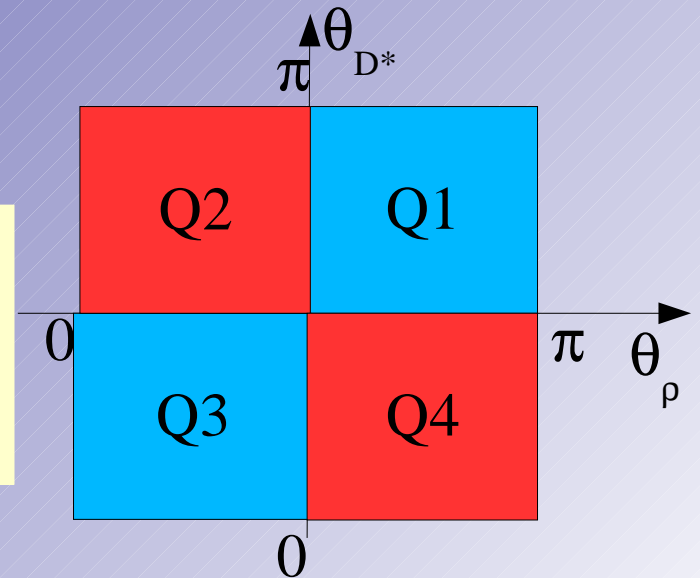
$$\frac{d\Gamma}{d\cos\vartheta_i} = \frac{4\pi}{3} |A_0|^2 \cos^2\vartheta_i + \frac{2\pi}{3} (|A_T|^2 + |A_{//}|^2) \sin^2\vartheta_i$$

$$\frac{d\Gamma}{d\phi} = \left(\frac{4}{9}|A_0|^2 + \frac{8}{9}|A_T|^2\right) \sin^2\phi + \left(\frac{4}{9}|A_0|^2 + \frac{8}{9}|A_{//}|^2\right) \cos^2\phi$$

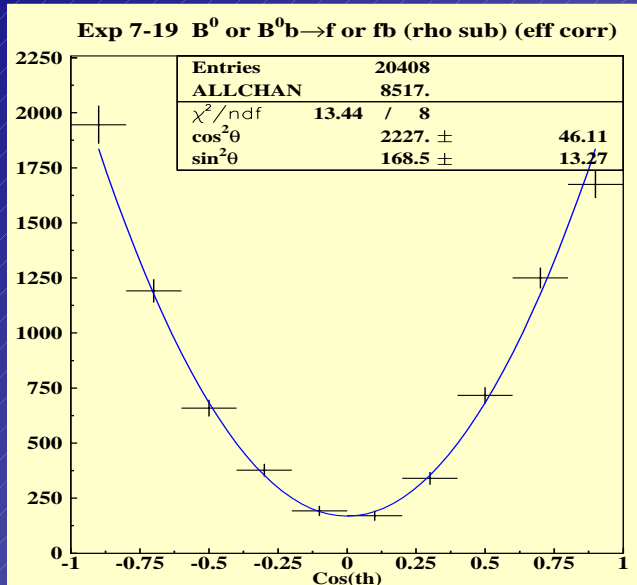
Interference components appears in "half projected" angular distribution

$$\Delta = (Q1 + Q3) - (Q2 + Q4)$$

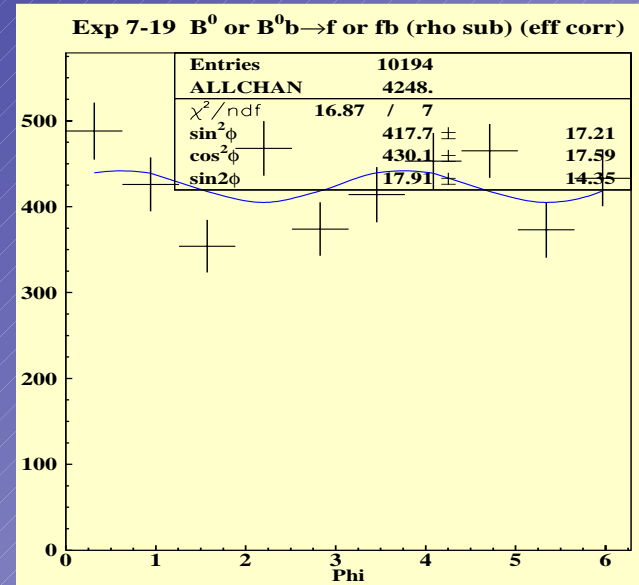
$$\frac{d\Delta}{d\phi} = \frac{-8}{9\sqrt{2}} \Im(A_0^* A_T) \sin\phi + \frac{8}{9\sqrt{2}} \Re(A_0^* A_{//}) \cos\phi$$



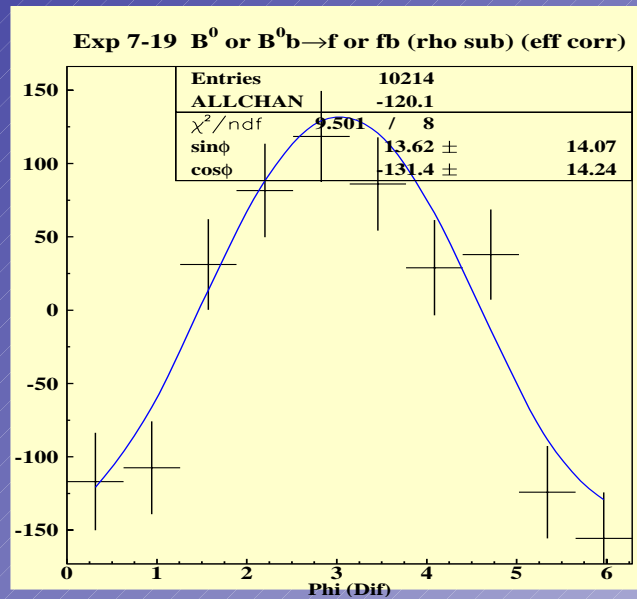
$$\cos\theta_1 + \cos\theta_2$$



$$\chi$$

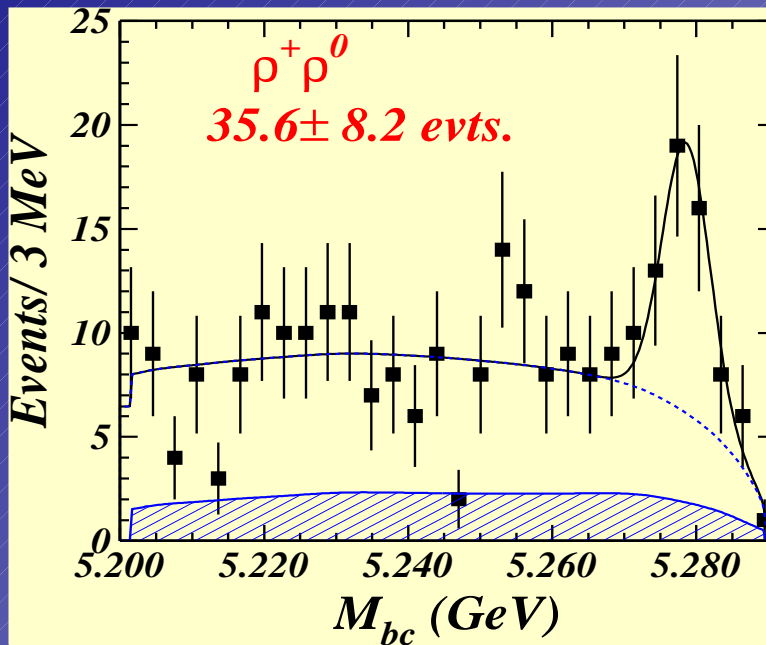


$$\Delta$$

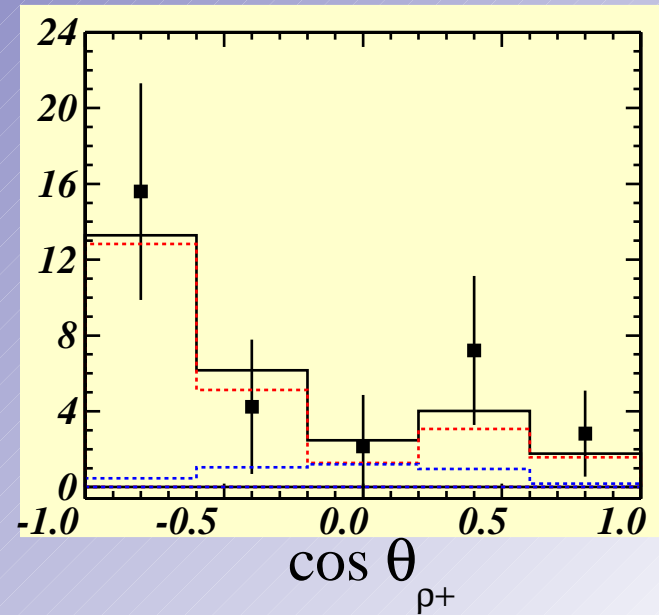
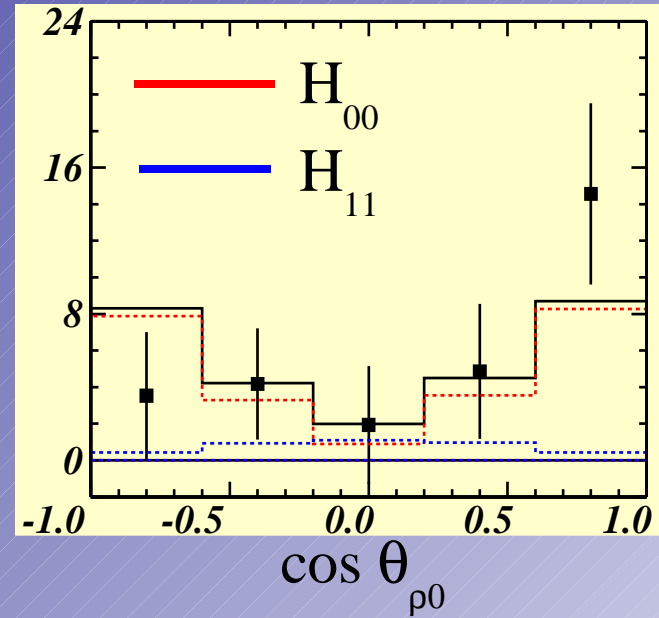


Helicity amplitudes for $B\rightarrow D^*\rho$ will be determined soon.

c) $B^+ \rightarrow \rho^+ \rho^0$ – Detail is covered by other talk (A.Gordon in HQ-3)



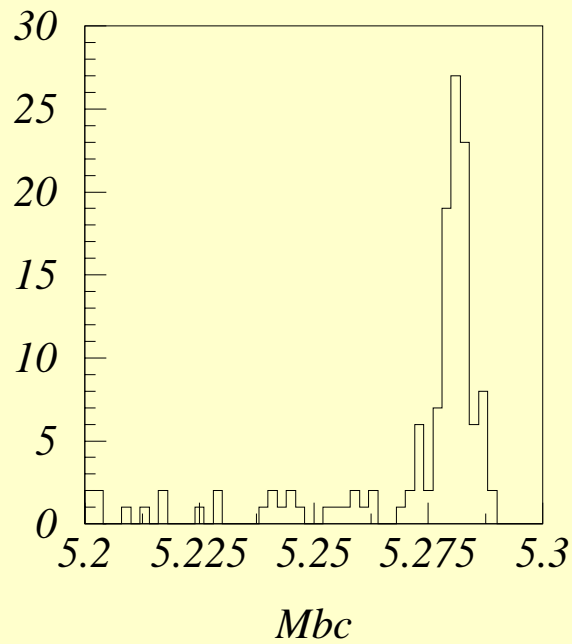
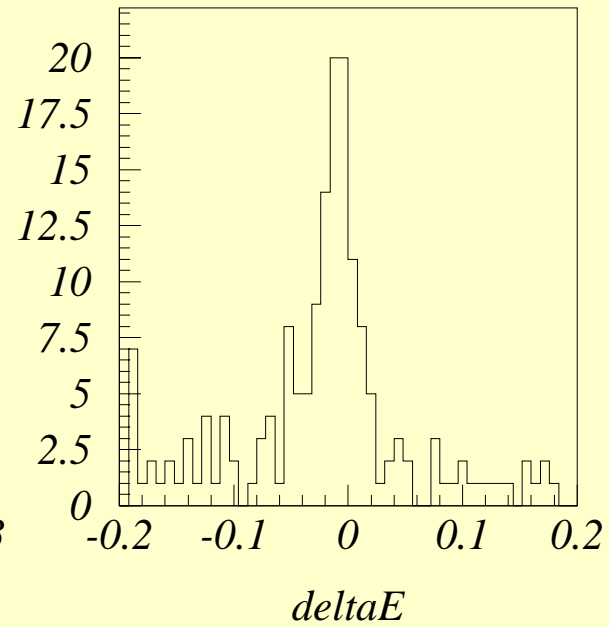
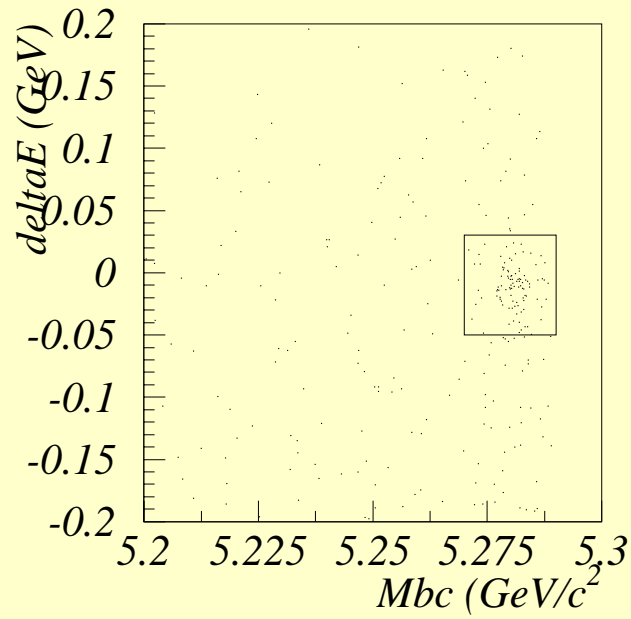
$$1 - \frac{\Gamma_T}{\Gamma} = 0.92 \pm 0.61$$



5. Summary

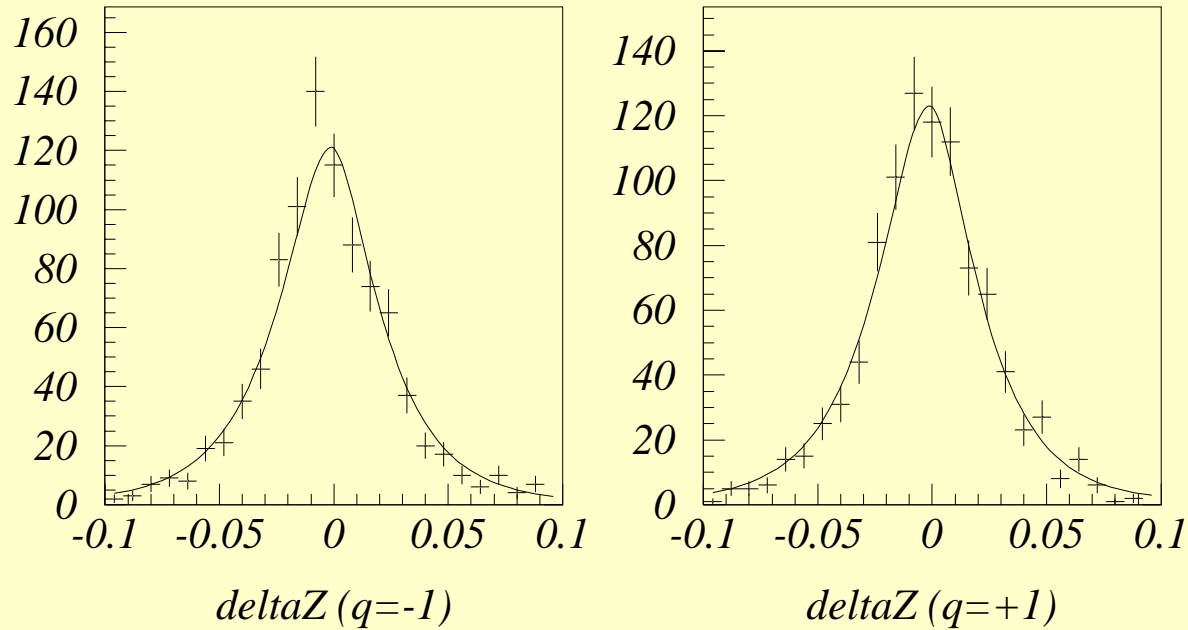
- Full time-dependent angular analysis is performed for $B \rightarrow J/\psi K^*$ decays collected with Belle detector at KEK B-factory.
- CP violation parameters $\sin 2\phi_1$ and $\cos 2\phi_1$ are determined to be
$$\sin 2\phi_1 = +0.13 \pm 0.51 \pm 0.06$$
$$\cos 2\phi_1 = +1.40 \pm 1.28 \pm 0.19$$
- When fixing $\sin 2\phi_1 = +0.82$, $\cos 2\phi_1 = +1.02 \pm 1.16$
- Taking s-quark helicity conservation choice of amplitude phases, obtained sign of $\cos 2\phi_1$ prefers $2\phi_1 = 55^\circ$ with $\sin 2\phi_1 = +0.82$ (namely, choice of $2\phi_1 = 145^\circ$ is not preferred) although statistical error is still too large.
- The angular analysis for other modes are in progress.

Backup Slides



ΔE vs. M_{bc}
 $(B^0 \rightarrow J/\psi K^{*0}(K_S \pi^0))$

Δz distributions for $J/\psi K^*(K^+\pi^-)$; selftag



Lines show the prediction by PDF with $\sin 2\phi_1 = \cos 2\phi_1 = 0.0$

Fit to $J/\psi K^*(K^+\pi^-)$

$$"\sin 2\phi_1" = 0.04 \pm 0.14$$

$$"\cos 2\phi_1" = 0.27 \pm 0.32$$

→ consistent with 0

c.f. selftag

$$"\sin 2\phi_1" = 0.00 \pm 0.07$$

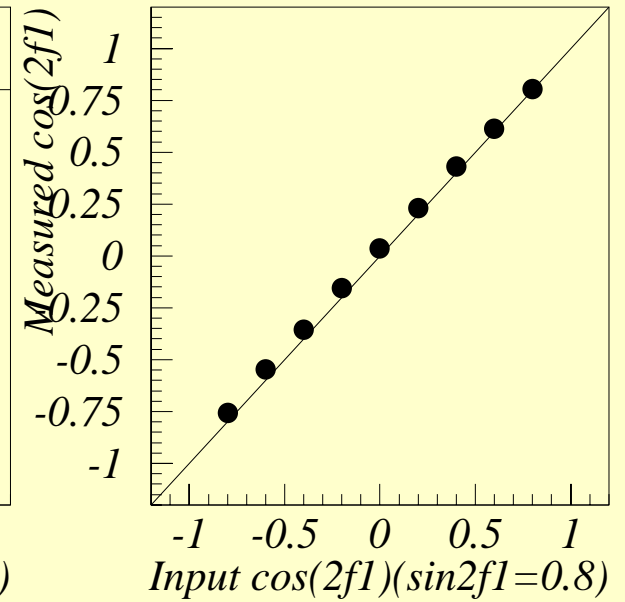
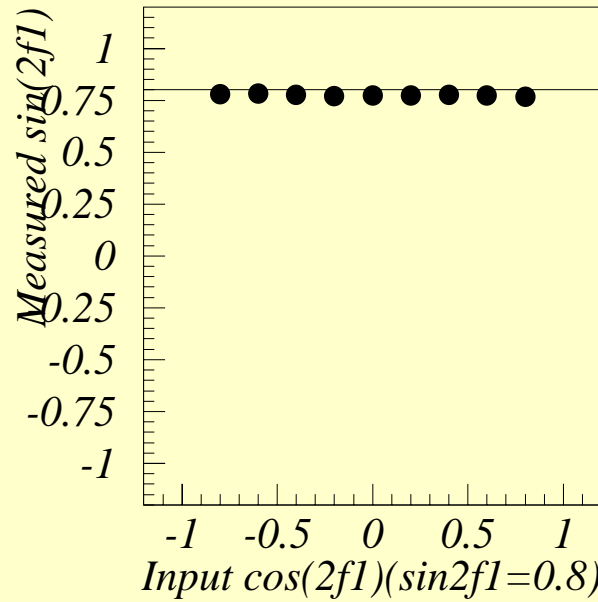
$$"\cos 2\phi_1" = -0.01 \pm 0.18$$

Linearity check

Case I:

$\sin 2\phi_1 = 0.8$ fixed

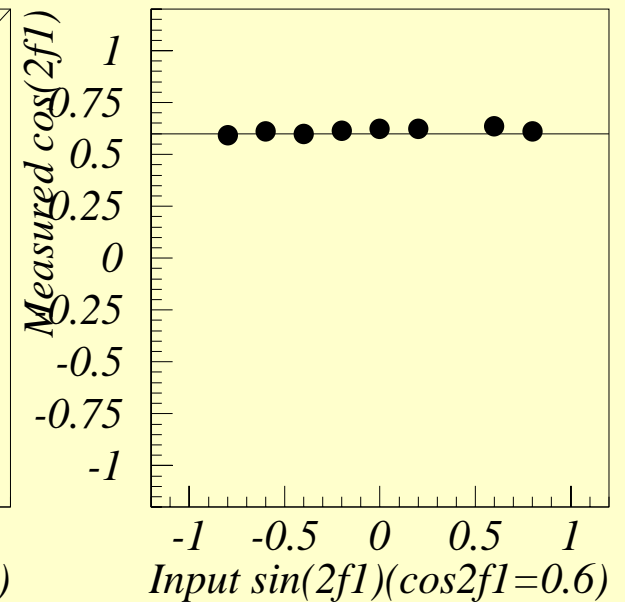
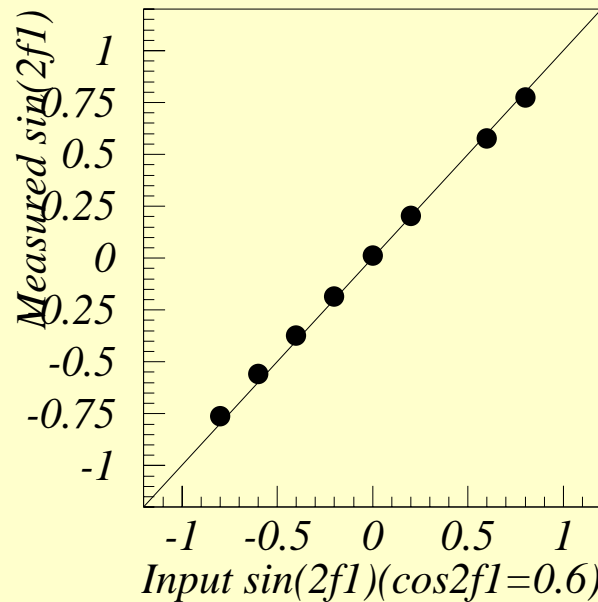
scan $\cos 2\phi_1$



Case II:

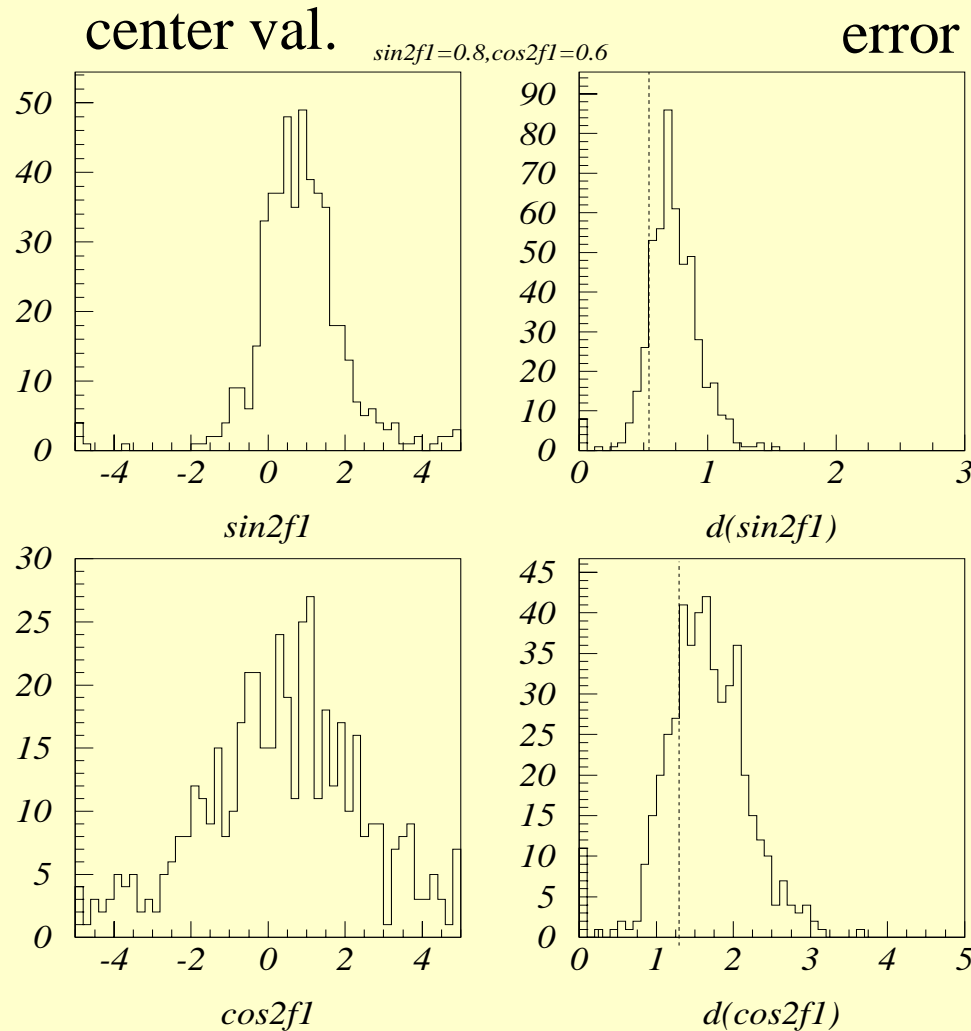
$\cos 2\phi_1 = 0.6$ fixed

scan $\sin 2\phi_1$



Ensemble test

- 500 sets of samples with 100 events are fitted and the distributions of output are checked. (Input: $\sin 2\phi_1 = 0.8$, $\cos 2\phi_1 = 0.6$)

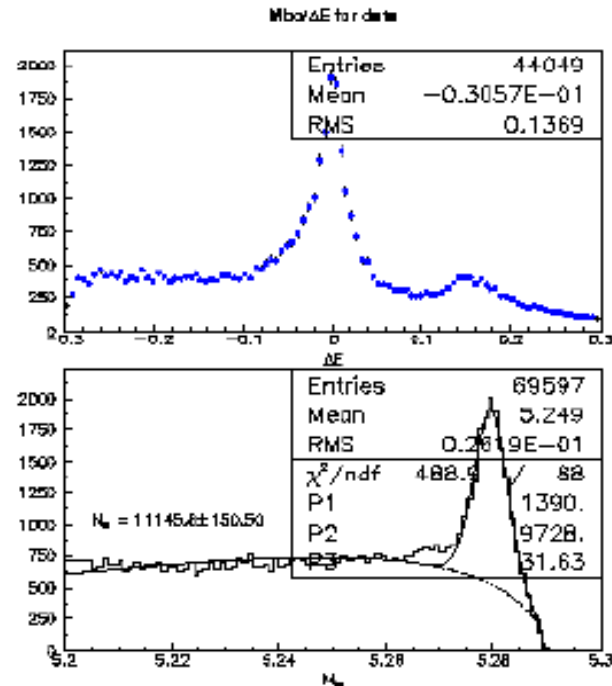




$\Delta E/M_{bc}$ for data

◆ with $M_{bc} < 5.27 \text{ GeV}/c^2$

◆ $-100 < \Delta E < 50 \text{ MeV}$:



Argus function doesn't describe the background for $M_{bc} < 5.27 \text{ GeV}/c^2$
(behaviour expected for such hadronic B decays)

Mike Peters, Trabelsi Karim

$D^+ \rho^-$ angular analysis

Belle General Meeting