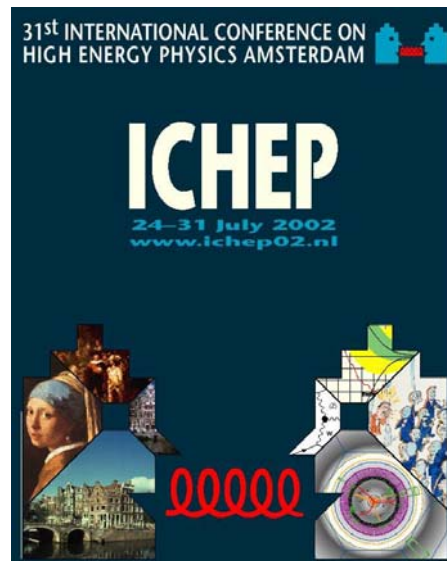


# Meson Lifetimes, Decays, Mixing and CPV in FOCUS

Sandra Malvezzi  
I.N.F.N. Milano



Sandra Malvezzi - Charm Meson  
Results in Focus



# A new charm-physics era

The **high statistics** and **excellent quality of data** allow for unprecedented sensitivity & sophisticated studies

**Investigation of decay dynamics both in the hadronic and semileptonic sector**

Phases and Quantum Mechanics interference

FSI role & CP studies

**Lifetime measurements @ better than 1%**  
non-spectator processes

**Mixing**

possible window on physics beyond SM

# Outline

- Hadronic decays



→ First clear evidence (DSCD)



→ First evidence (SCSD)

- Amplitude Analysis of three pseudoscalar channels



→ First Dalitz analysis

→ New method for CPV

- Semileptonic decays

Anomaly in  $D^+ \rightarrow (K^- \pi^+) \mu^+ \nu$  decay → s-wave interference

New BR of  $\frac{\Gamma(D^+ \rightarrow \bar{K}^{*0} \mu^+ \nu)}{\Gamma(D^+ \rightarrow K^- \pi^+ \pi^+)}$  and  $\frac{\Gamma(D_s^+ \rightarrow \phi \mu^+ \nu)}{\Gamma(D_s^+ \rightarrow \phi \pi^+)}$

- Lifetimes

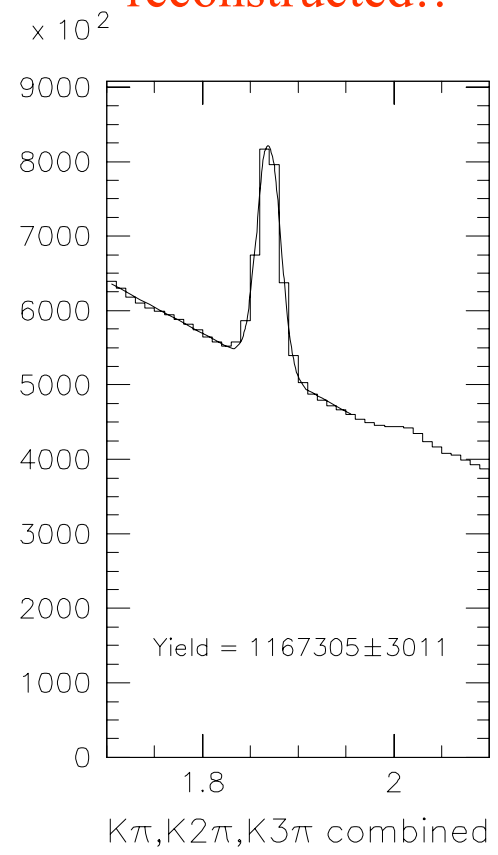
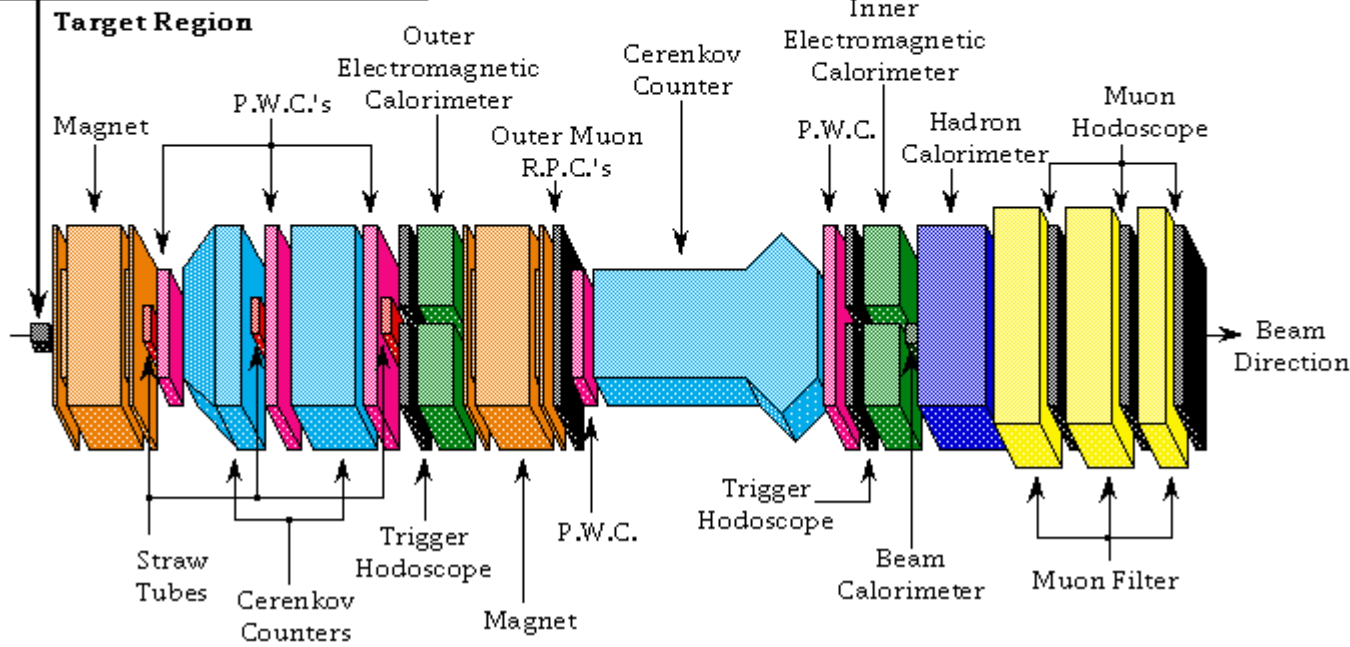
Precise measurements for  $D^+, D^0$  and preliminary for  $D_s$

- Mixing

Preliminary results from  $D^0 \rightarrow K^+ \pi^-$  and  $D^0 \rightarrow K^+ \mu^- \nu$



Over 1 million reconstructed!!



Successor to E687. Designed to study charm particles produced by  $\sim 200$  GeV photons using a fixed target spectrometer with upgraded **Vertexing**, **Cerenkov**, **E+M Calorimetry**, and **Muon id** capabilities. Includes groups from USA, Italy, Brazil, Mexico, Korea

**1 million charm particles reconstructed into  $D \rightarrow K\pi, K2\pi, K3\pi$**

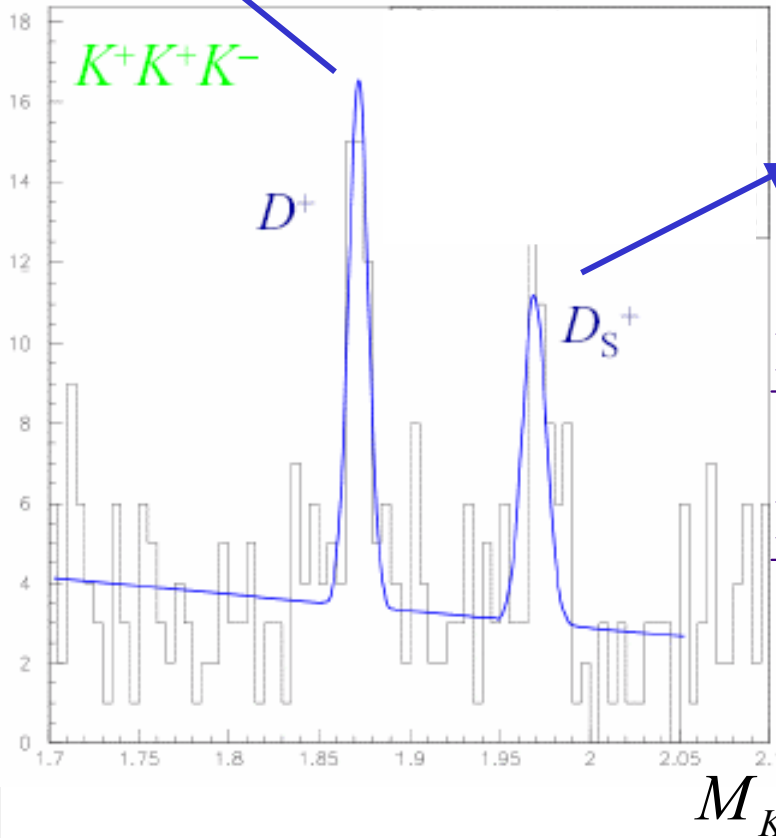
# $D^+, D_s^+ \rightarrow K^- K^+ K^+$

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First clear observation

Yield  $D^+ = 65.5 \pm 15.0$

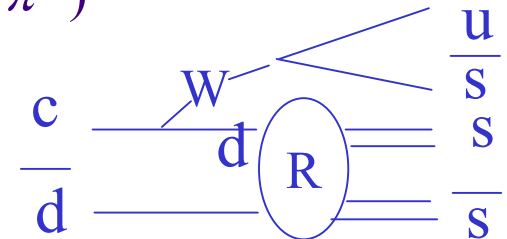
Yield  $D_s = 31.4 \pm 7.4$



First observation

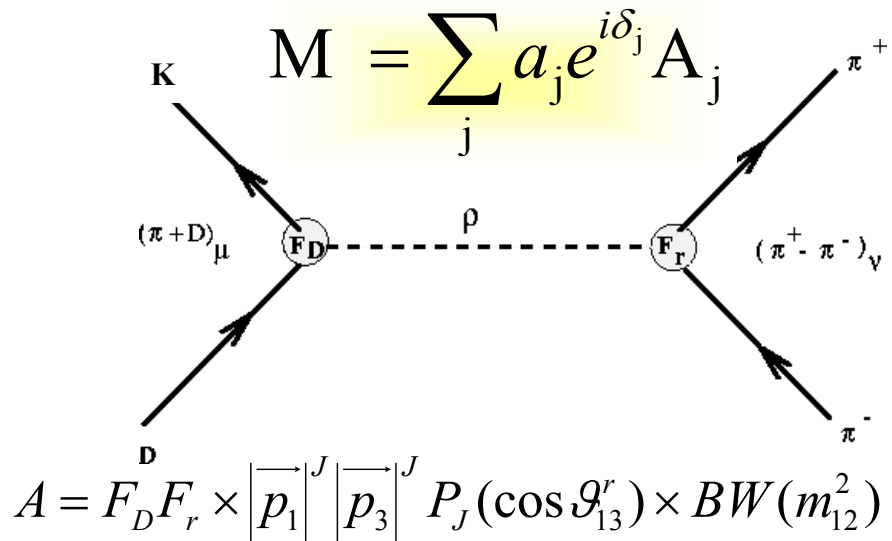
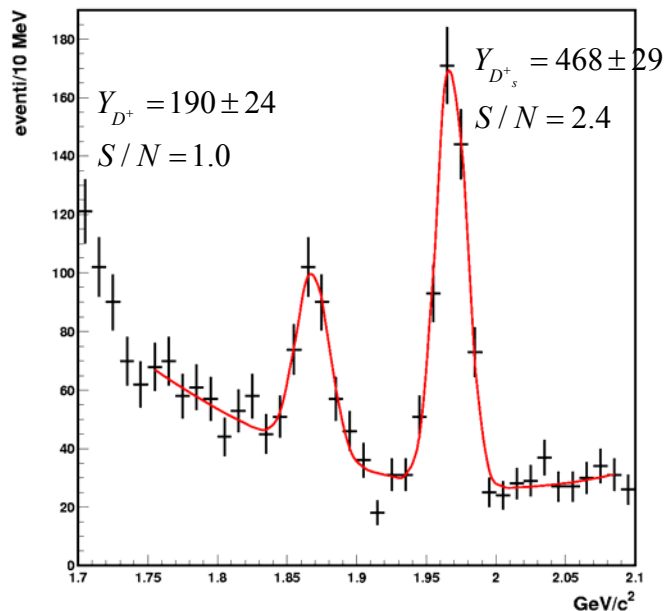
$$\frac{\Gamma(D^+ \rightarrow K^- K^+ K^+)}{\Gamma(D^+ \rightarrow K^- \pi^+ \pi^+)} = (9.49 \pm 2.17 \pm 0.22) \times 10^{-4}$$

$$\frac{\Gamma(D_s^+ \rightarrow K^- K^+ K^+)}{\Gamma(D_s^+ \rightarrow K^- K^+ \pi^+)} = (8.62 \pm 2.04 \pm 2.07) \times 10^{-3}$$



Intervention of resonances coupling both to  $\pi\pi$  and KK or annihilation

# Dalitz plot analysis of $D^+, D_s^+ \rightarrow K^+ \pi^+ \pi^-$



Where

$$F = 1$$

$$F = (1 + R^2 p^2)^{-1/2}$$

$$F = (9 + 3R^2 p^2 + 3R^4 p^4)^{-1/2}$$

Spin 0

Spin 1

Spin 2

$$P_J = 1$$

$$P_J = (-2 \vec{p}_3 \cdot \vec{p}_1)$$

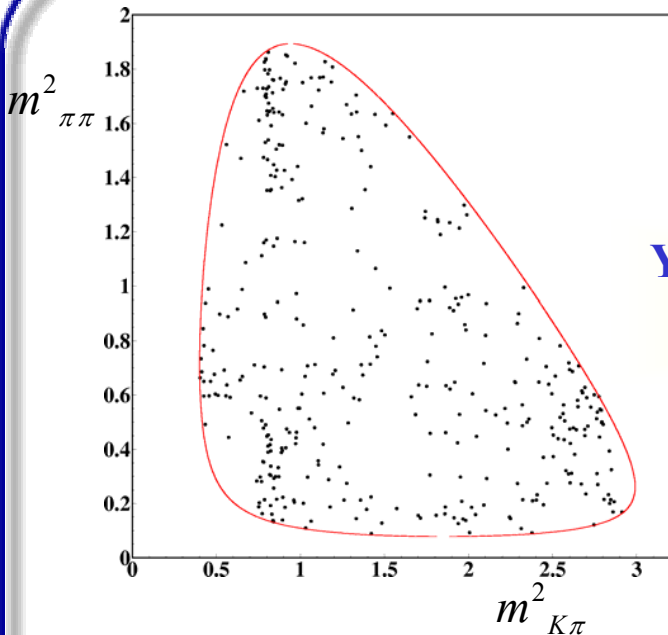
$$P_J = 2(p_3 p_1)^2 (3 \cos^2 \vartheta_{13} - 1)$$

and

$$BW(12|r) = \frac{F_D F_r}{M_r^2 - m_{12}^2 - i\Gamma M_r}$$

$$\Gamma = \Gamma_r \left[ \frac{p}{p_0} \right]^{2j+1} \frac{M_r F_r^2(p)}{m_{12} F_r^2(p_0)}$$

# DCS



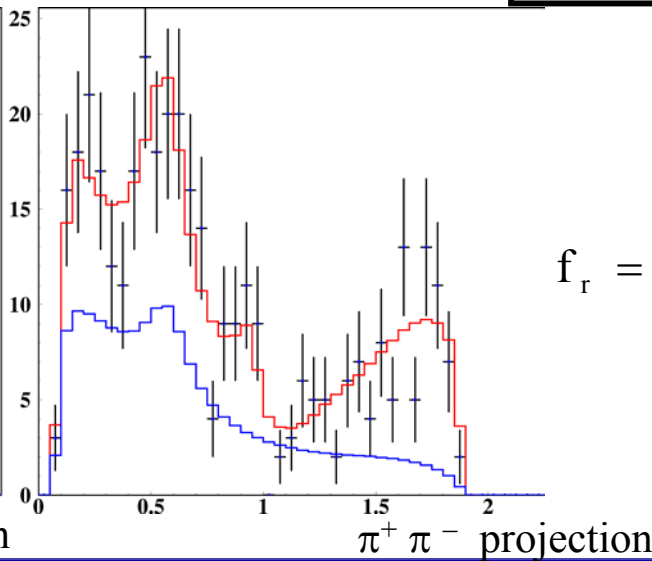
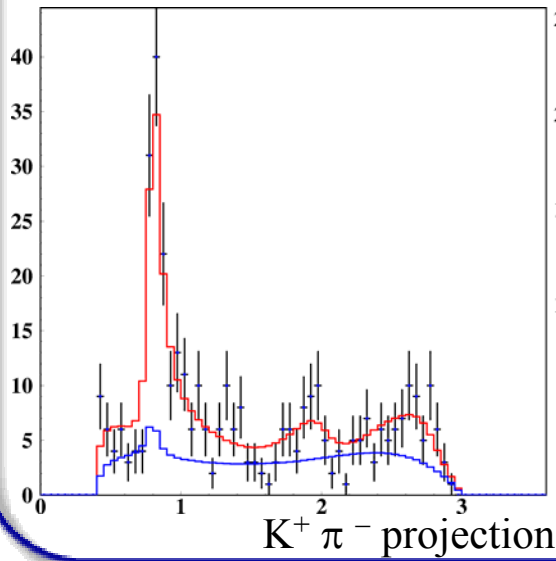
Yield  $D^+ = 190 \pm 24$

S/N  $D^+ = 1.0$

Preliminary

## Decay fractions and phases

NR	= $9 \pm 5$ %	$(-6 \pm 16)^\circ$
$K^*(892)$	= $43 \pm 7$ %	$(208 \pm 16)^\circ$
$K^*(1410)$	= $12 \pm 8$ %	$(133 \pm 23)^\circ$
$K_2(1430)$	= $6 \pm 3$ %	$(48 \pm 27)^\circ$
$K^*(1680)$	= $22 \pm 10$ %	$(2 \pm 20)^\circ$
$\rho(770)$	= $51 \pm 10$ %	(0 fixed)
$f_0(980)$	= $9 \pm 5$ %	$(73 \pm 31)^\circ$
$\rho(1450)$	= $10 \pm 5$ %	$(-113 \pm 15)^\circ$



$$f_r = \frac{\int |a_r e^{i\delta_r} A_r|^2 dm_{12}^2 dm_{13}^2}{\int |\sum_j a_j e^{i\delta_j} A_j|^2 dm_{12}^2 dm_{13}^2}$$



# SCS



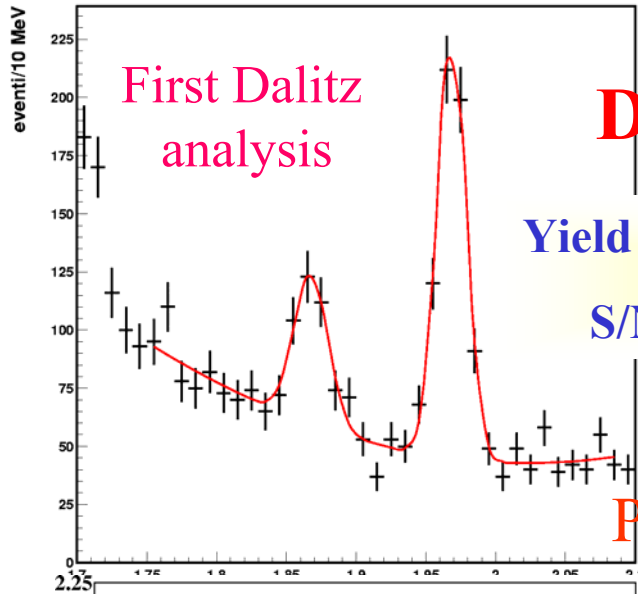
Yield  $D_s^+ = 468 \pm 29$

S/N  $D_s^+ = 2.4$

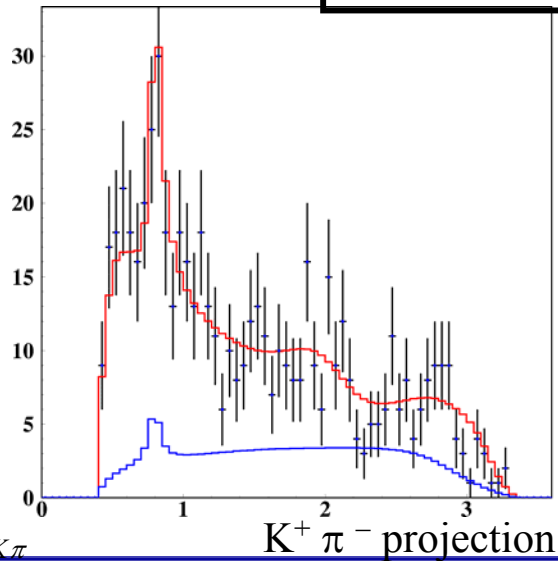
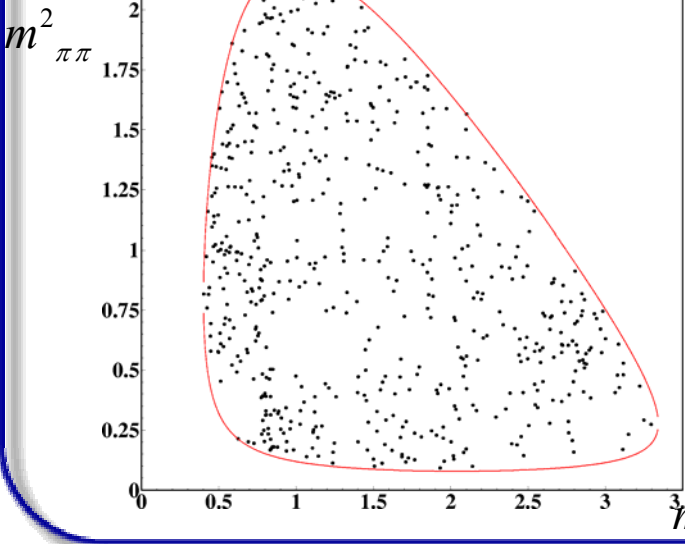
Preliminary

## Decay fractions and phases

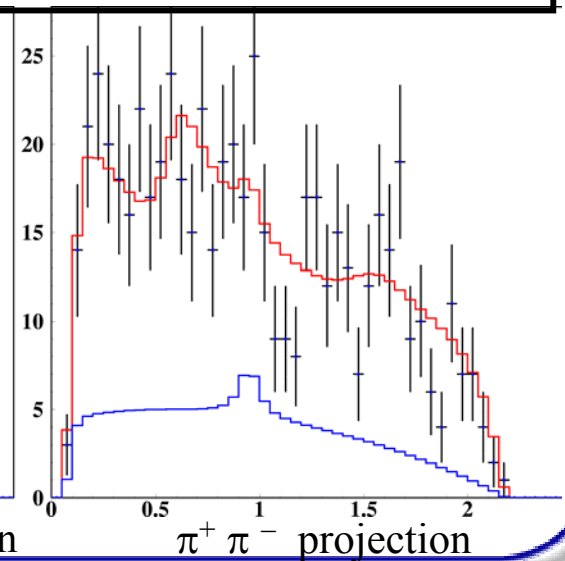
NR	$= 18 \pm 4 \%$	$(34 \pm 7)^\circ$
$K^*(892)$	$= 22 \pm 3 \%$	$(163 \pm 7)^\circ$
$K^*(1410)$	$= 14 \pm 5 \%$	$(-10 \pm 7)^\circ$
$K^*_0(1430)$	$= 14 \pm 6 \%$	$(68 \pm 7)^\circ$
$\rho(770)$	$= 40 \pm 4 \%$	(0 fixed)
$f_2(1270)$	$= 2 \pm 1 \%$	$(33 \pm 21)^\circ$
$\rho(1450)$	$= 8 \pm 2 \%$	$(219 \pm 14)^\circ$



First Dalitz analysis



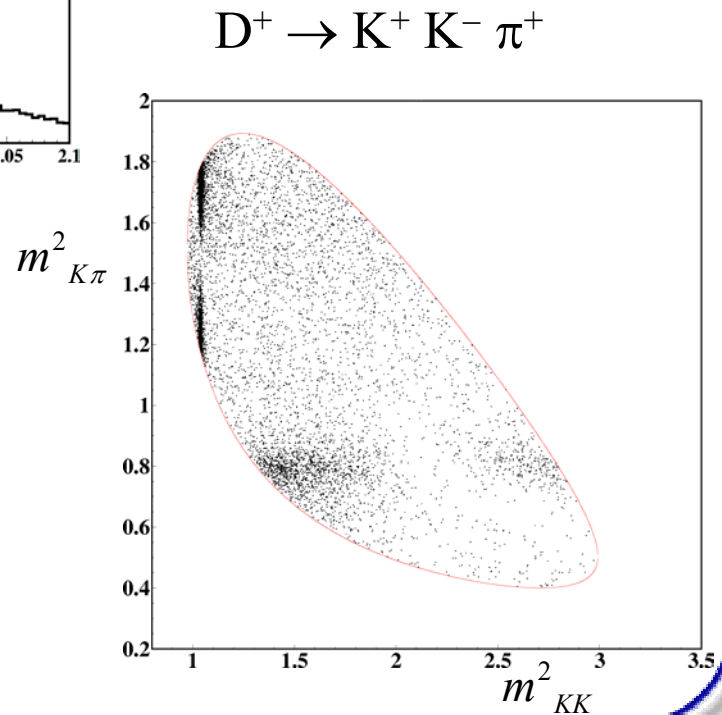
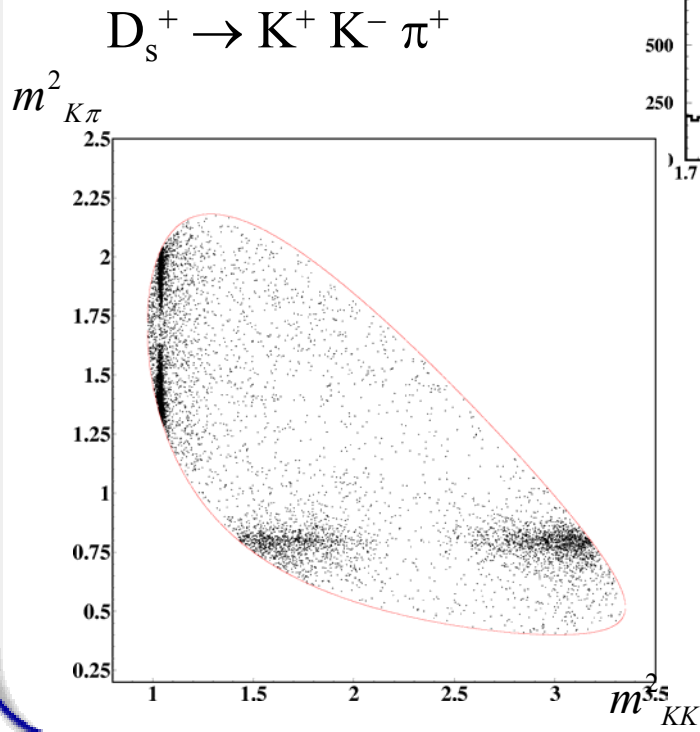
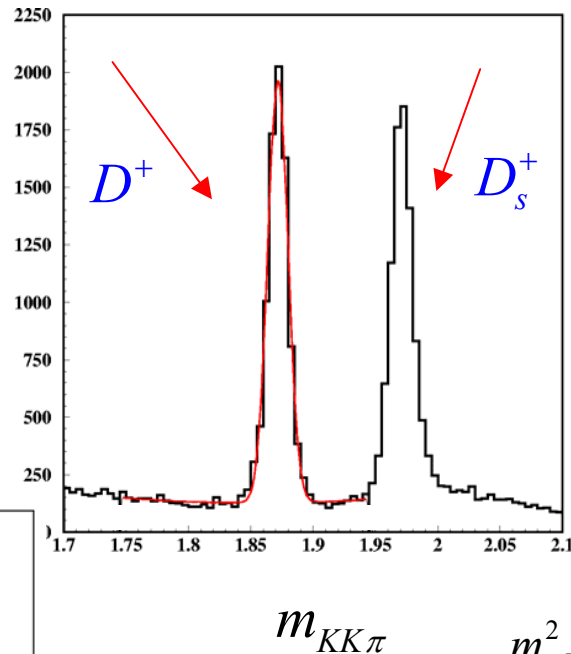
$K^+ \pi^-$  projection



$\pi^+ \pi^-$  projection



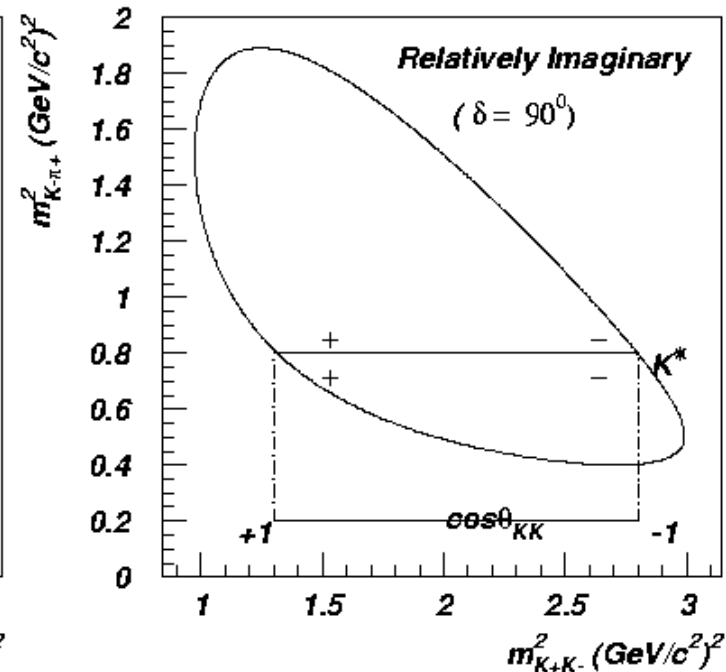
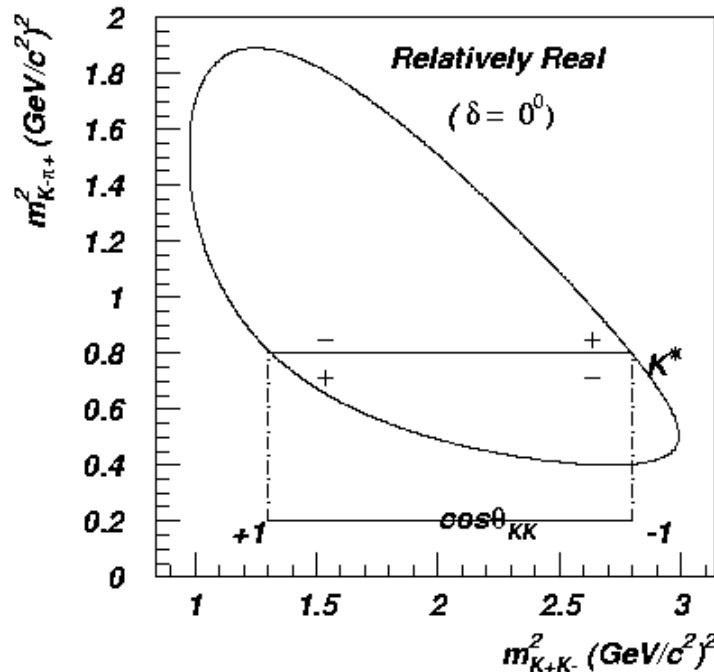
# $D_s, D^+ \rightarrow KK\pi$

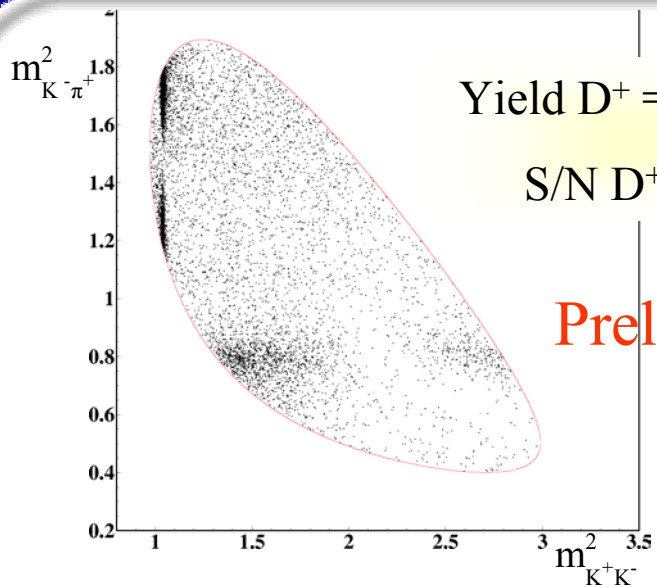


# Interference term

$$2\text{Re} \left[ (\cos \delta + i \sin \delta)^* \frac{\cos \theta_{KK}}{m_r^2 - m_{K\pi}^2 - i\Gamma m_r} \right] =$$

$$= 2 \frac{(m_r^2 - m_{K\pi}^2) \cos \theta_{KK} \cos \delta}{(m_r^2 - m_{K\pi}^2)^2 + \Gamma^2 m_r^2} + 2 \frac{\Gamma M_r \cos \theta_{KK} \sin \delta}{(m_r^2 - m_{K\pi}^2)^2 + \Gamma^2 m_r^2}$$

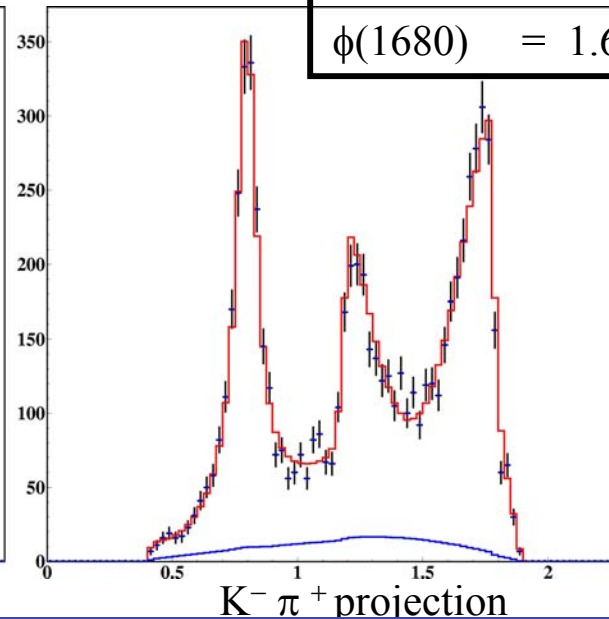
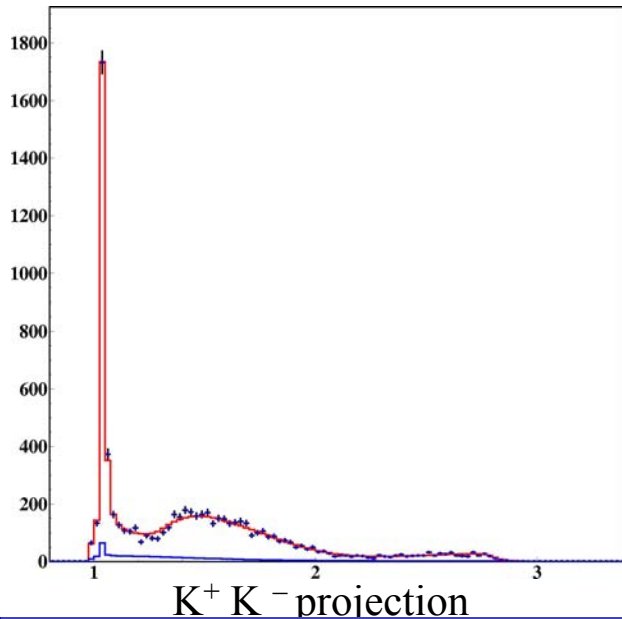




Preliminary

### Decay Fraction and phases

$\bar{K}^*(892)$	$= 20.7 \pm 1.0 \%$	$(0 \text{ fixed})$
$\phi(1020)$	$= 27.8 \pm 0.7 \%$	$(243.1 \pm 5.2)^\circ$
$\bar{K}^*(1410)$	$= 10.7 \pm 1.9 \%$	$(-47.4 \pm 4.9)^\circ$
$\bar{K}^*(1430)$	$= 66.5 \pm 6.0 \%$	$(61.8 \pm 3.8)^\circ$
$f_0(1370)$	$= 7.0 \pm 1.1 \%$	$(60.0 \pm 5.3)^\circ$
$a_0(980)$	$= 27.0 \pm 4.8 \%$	$(145.6 \pm 4.3)^\circ$
$f_2(1270)$	$= 0.8 \pm 0.2 \%$	$(11.6 \pm 7.0)^\circ$
$\phi(1680)$	$= 1.6 \pm 0.4 \%$	$(-74.3 \pm 7.5)^\circ$



# CP violation

For a two amplitude decay

$$A_{\text{tot}} = g_1 M_1 e^{i\delta_1} + g_2 M_2 e^{i\delta_2}$$

⇓ CP conjugate

$$\bar{A}_{\text{tot}} = g_1^* M_1 e^{i\delta_1} + g_2^* M_2 e^{i\delta_2}$$

$\delta_i =$  strong phase

CP asymmetry:

$$a_{\text{CP}} = \frac{|A_{\text{tot}}|^2 - |\bar{A}_{\text{tot}}|^2}{|A_{\text{tot}}|^2 + |\bar{A}_{\text{tot}}|^2} = \frac{2\text{Im}(g_2 g_1^*) \sin(\delta_1 - \delta_2) M_1 M_2}{|g_1|^2 M_1^2 + |g_2|^2 M_2^2 + 2\text{Re}(g_2 g_1^*) \cos(\delta_1 - \delta_2) M_1 M_2}$$

2 different amplitudes

strong phase-shift

# CP violation: Dalitz analysis

Dalitz plot = **FULL OBSERVATION** of the decay



**COEFFICIENTS** and **PHASES** for each amplitude

Measured phase:

$$\theta = \delta + \phi$$

CP conserving

CP violating

CP conjugate

$$\bar{\delta} = \delta$$

$$\bar{\phi} = -\phi$$



$$\bar{\theta} = \delta - \phi$$

E831



Measure of direct CP violation:

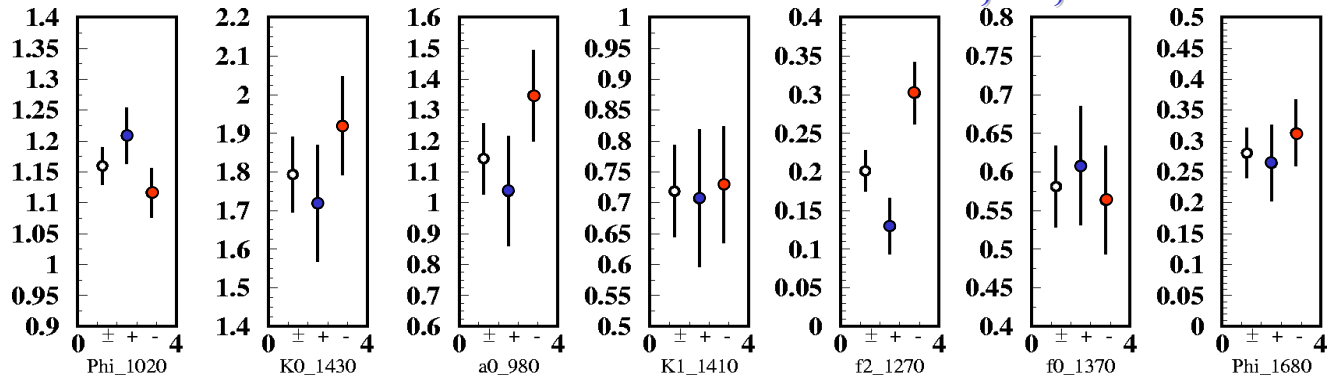
asymmetrys in decay rates of  $D^{\pm} \rightarrow K^{\mp} K \pi^{\pm}$

$$a_{CP} = 0.006 \pm 0.011 \pm 0.005$$

# D<sup>+</sup>/D<sup>-</sup> split sample analysis

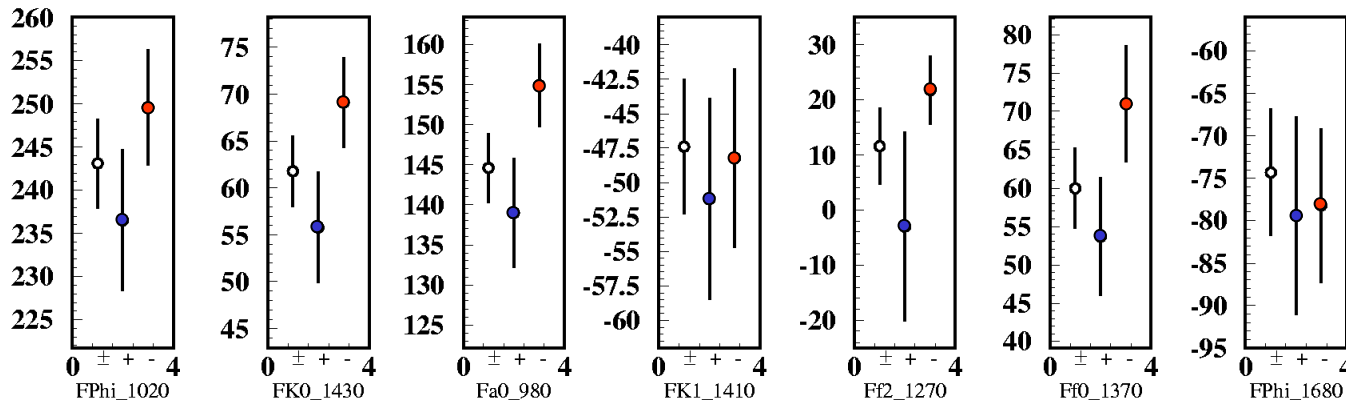
Coefficients: D<sup>±</sup>, D<sup>+</sup>, D<sup>-</sup>

Preliminary!



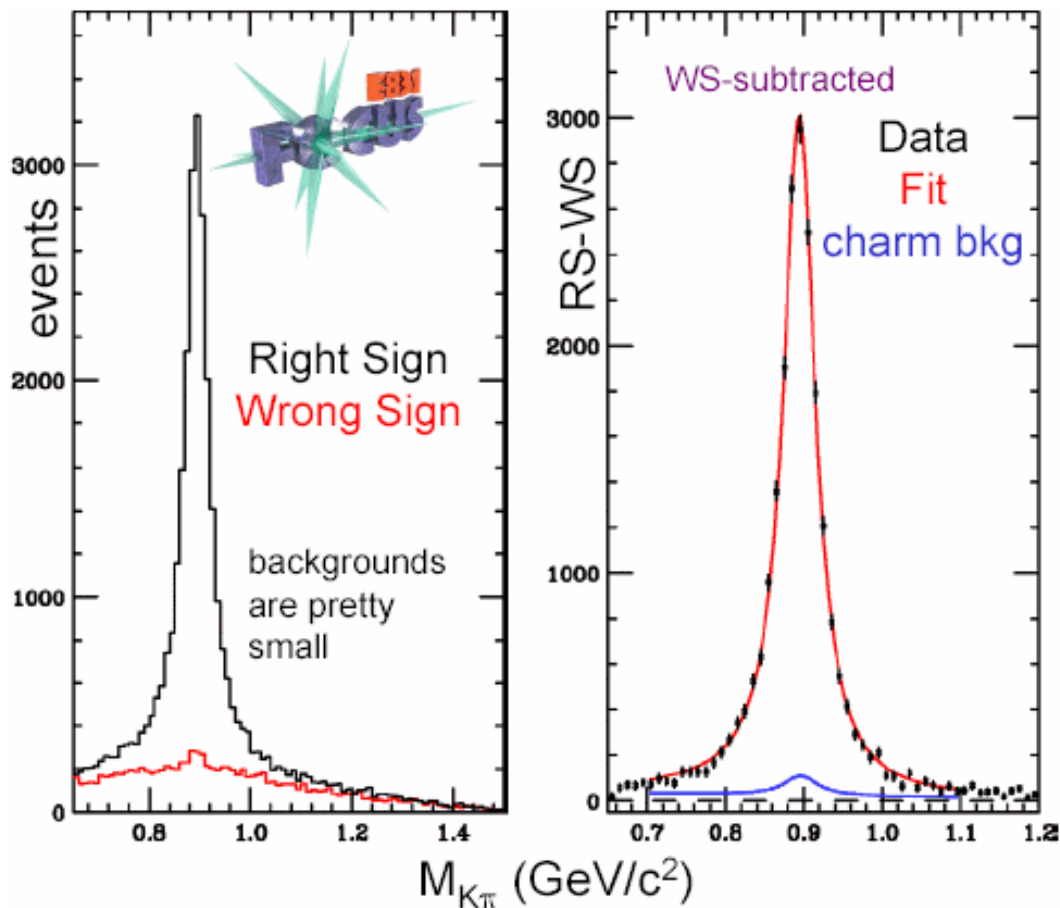
Phases: D<sup>±</sup>, D<sup>+</sup>, D<sup>-</sup>

No evidence of CPV



K-matrix approach to improve the quality of the analysis

# New results on $D^+ \rightarrow K\pi\mu\nu$



Our  $K\pi$  spectrum looks like 100%  $K^*(892)$

This has been known for about 20 years

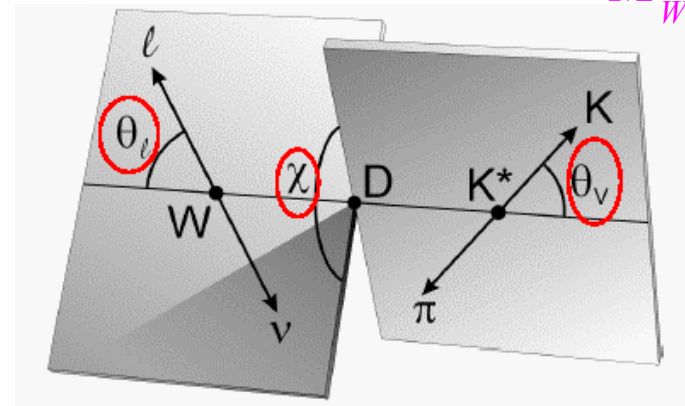
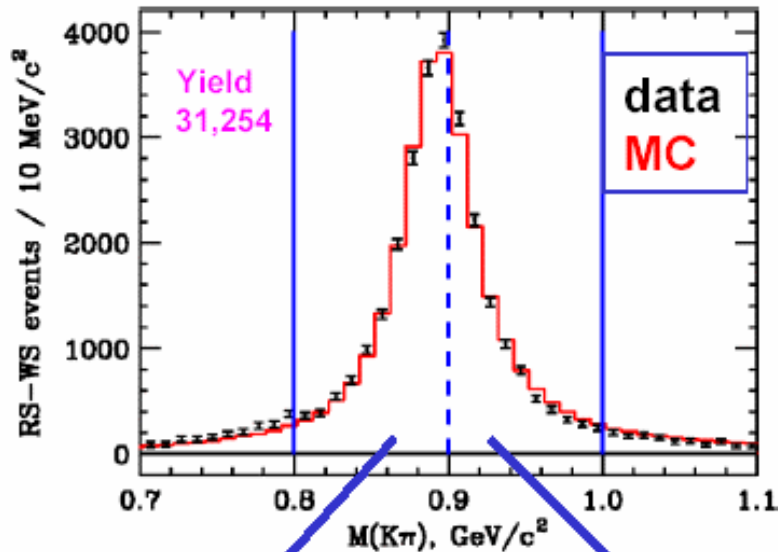
...but a funny thing happened when we tried to measure the form factor ratios by fitting the angular distributions

# An unexpected asymmetry in the $K^*$ decay

A 4-body decays requires  
5 kinematics variables: 3 angles  
and 2 masses

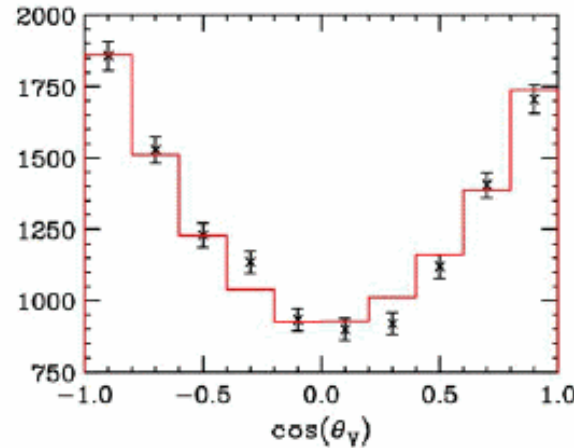
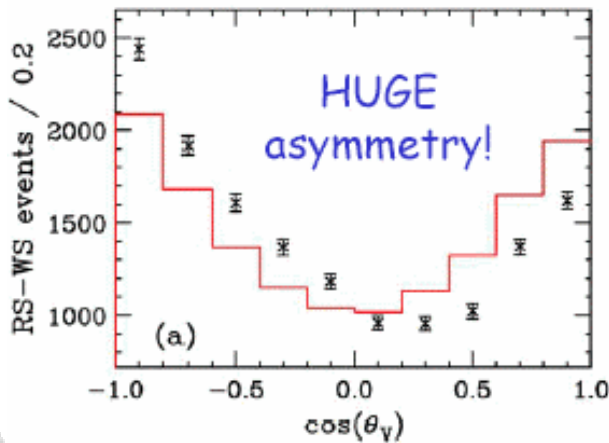
$$M_{W^2} \equiv q^2 \equiv t$$

$$M_{K\pi}$$



$0.8 < M(K\pi) < 0.9 \text{ GeV}/c^2$

$0.9 < M(K\pi) < 1.0 \text{ GeV}/c^2$



$$\frac{d\Gamma}{d\Omega} \propto 1 + \alpha \cos^2 \theta_\nu$$

forward-backward  
asymmetry in  
 $\cos \theta_\nu$  below the  $K^*$   
pole but almost none  
above the pole

**Sounds like  
QM interference**



# Try an interfering spin-0 amplitude

Phys.Lett.B535,43,2002

$$|M|^2 \propto (t - m_\mu^2) \left[ \frac{(1 + \cos \theta_l) \sin \theta_V}{2\sqrt{2}} e^{i\chi} BH_+ + \frac{(1 - \cos \theta_l) - \sin \theta_V}{2\sqrt{2}} e^{-i\chi} BH_- + \frac{-\sin \theta_l (\cos \theta_V B + Ae^{i\delta}) H_0}{\sqrt{2}} \right]^2$$

(plus mass terms)

$Ae^{i\delta}$  will produce  
3 interference terms

$$B \equiv \frac{\sqrt{m_0 \Gamma}}{m^2 - m_0^2 + im_0 \Gamma}$$

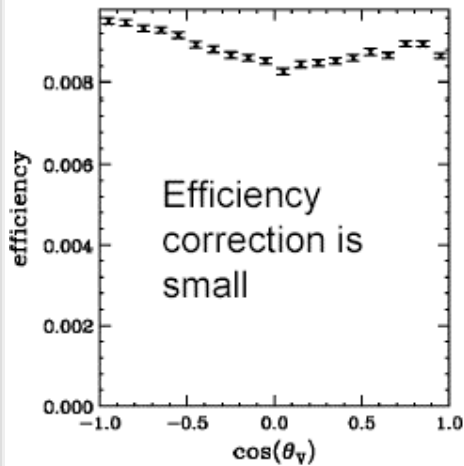
We simply add a constant amplitude  $Ae^{i\delta}$  in the place where the  $K^*$  couples to an  $m=0$   $W^+$  with amplitude  $H_0$

# Studies of the acoplanarity-averaged interference

$$8 \cos \theta_V \sin^2 \theta_V A \operatorname{Re}(e^{-i\delta} B_{K^*}) H^2_0$$

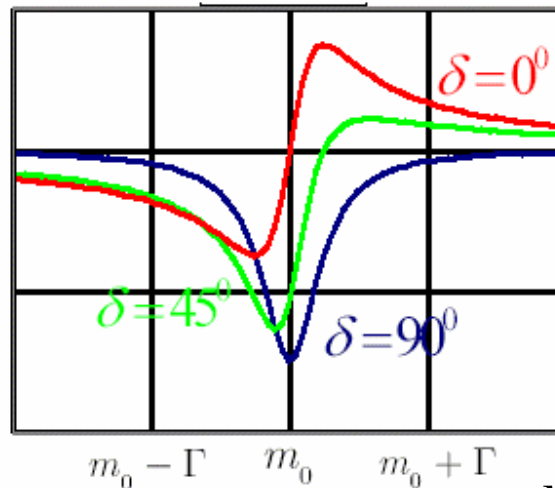
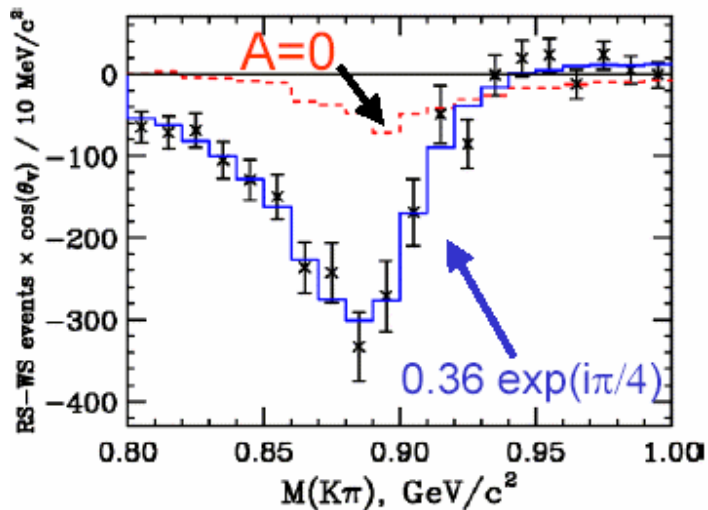
Extract this interference term by weighting data by  $\cos \theta_V$

Since all other  $\chi$ -averaged terms in the decay intensity are constant or  $\propto \cos^2 \theta_V$



We begin with the mass dependence:  $\operatorname{Re}(e^{-i\delta} B_{K^*})$

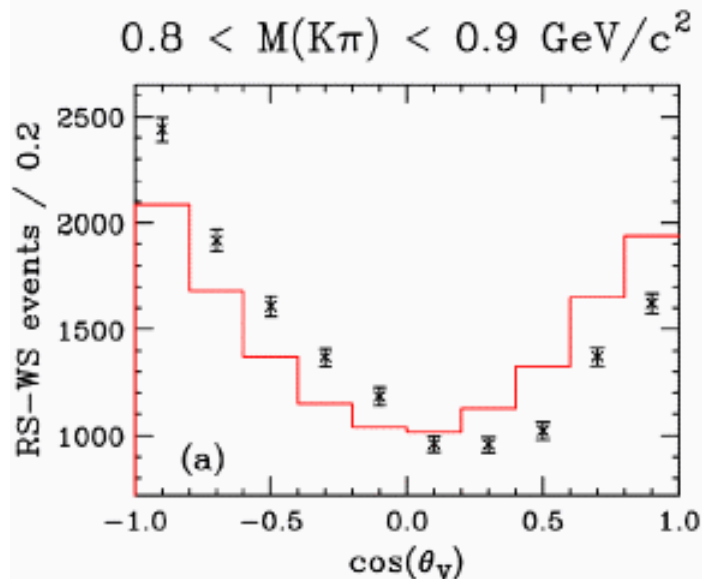
Our weighted mass distribution... ..looks just like the calculation



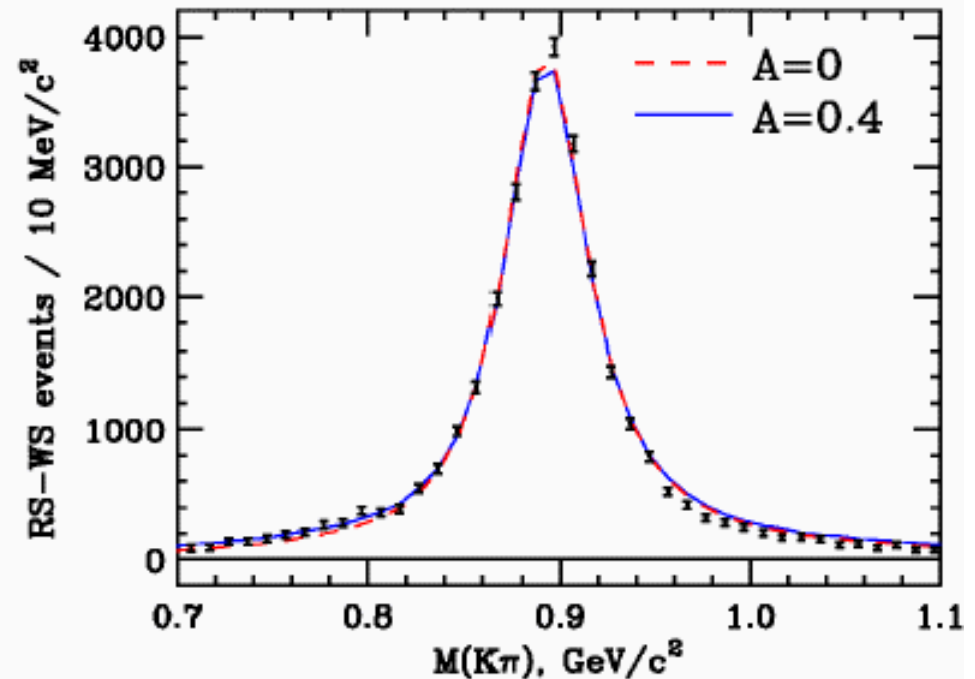
A constant 45° phase works great....  
...but the solution is not unique

$M_{K\pi}$

But surely an effect this large must have been observed before?



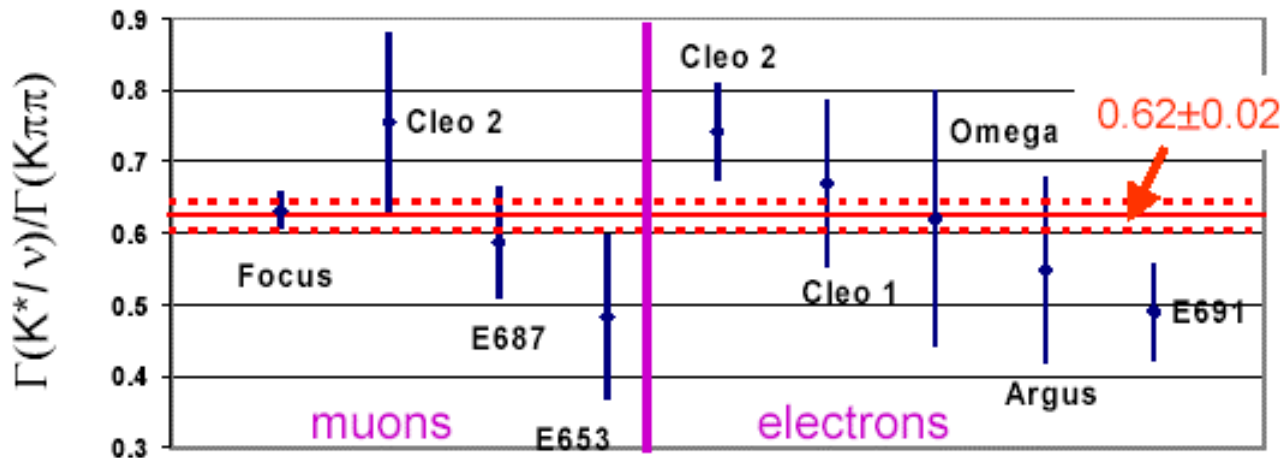
Although the interference *significantly* distorts the decay intensity....



...the interference is nearly invisible in the  $K\pi$  mass plot.

# New FOCUS semileptonic BRs & Form Factors

$$\frac{\Gamma(D^+ \rightarrow \overline{K}^{*0} \mu^+ \nu)}{\Gamma(D^+ \rightarrow K^- \pi^+ \pi^+)} = 0.602 \pm 0.01(\text{stat}) \pm 0.021(\text{sys})$$



Our number is 1.59  
standard deviation  
below CLEO and 2.1  
standard deviation  
above E691

All values consistent with their average value with a CL of 19%

# $\Gamma(D^+ \rightarrow \overline{K}^{*0} \mu^+ \nu)$ Form Factors

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The vector and axial form factors are generally parametrized by a pole dominance form

$$A_i(q^2) = \frac{A_i(0)}{1 - q^2/M_A^2} \quad V(q^2) = \frac{V(0)}{1 - q^2/M_V^2}$$

$$M_A = 2.5 \text{ GeV} / c^2$$
$$M_V = 2.1 \text{ GeV} / c^2$$

Decay intensity (including s-wave amplitude) parametrized by

Nominal spectroscopic pole masses

$$r_V \equiv V(0)/A_1(0) \quad r_2 \equiv A_2(0)/A_1(0) \quad r_3 \equiv A_3(0)/A_1(0)$$

New FOCUS  
results →

$$r_V = 1.504 \pm 0.057 \pm 0.039$$

$$r_2 = 0.875 \pm 0.049 \pm 0.064$$

## Form Factor Ratios

Group	$r_v$	$r_2$
<i>FOCUS</i>	$1.504 \pm 0.057 \pm 0.039$	$0.875 \pm 0.049 \pm 0.064$
<i>BEATRICE</i>	$1.45 \pm 0.23 \pm 0.07$	$1.00 \pm 0.15 \pm 0.03$
<i>E791(e)</i>	$1.90 \pm 0.11 \pm 0.09$	$0.71 \pm 0.08 \pm 0.09$
<i>E791(<math>\mu</math>)</i>	$1.84 \pm 0.11 \pm 0.09$	$0.75 \pm 0.08 \pm 0.09$
<i>E687</i>	$1.74 \pm 0.27 \pm 0.28$	$0.78 \pm 0.18 \pm 0.11$
<i>E653</i>	$2.00 \pm 0.33 \pm 0.16$	$0.82 \pm 0.22 \pm 0.11$
<i>E691</i>	$2.0 \pm 0.6 \pm 0.3$	$0.0 \pm 0.5 \pm 0.2$

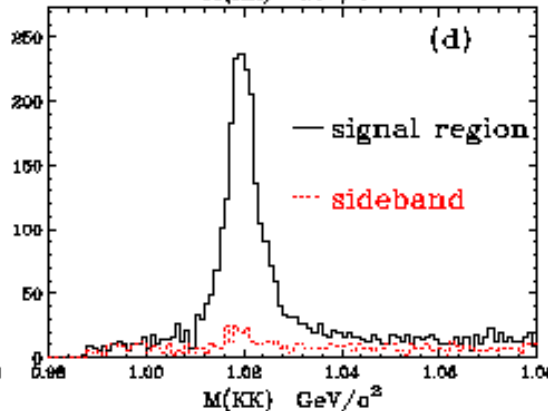
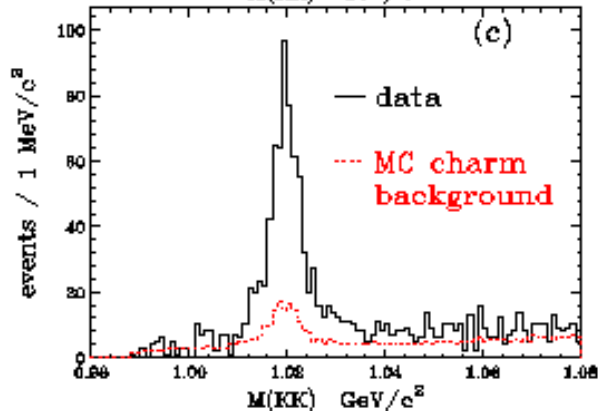
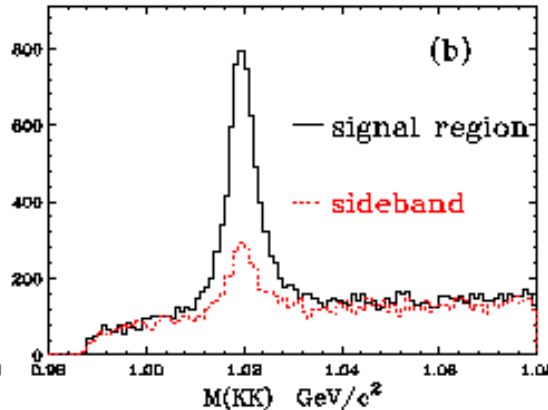
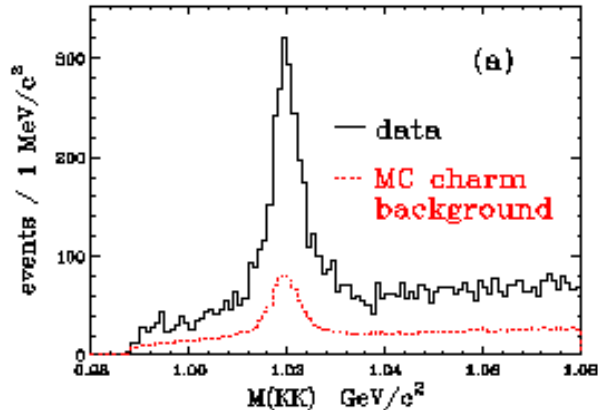
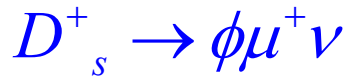
Our analysis is the first to include the effects on the acceptance due to changes in the angular distribution brought about the s-wave interference

$$A = 0.330 \pm 0.022 \pm 0.015 \text{ GeV}^{-1}$$

$$\delta = 0.68 \pm 0.07 \pm 0.05 \text{ rad}$$



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Baseline cuts

a) 2682 evts

b) 4695 evts

Baseline, out-of-material.  
isolation cuts

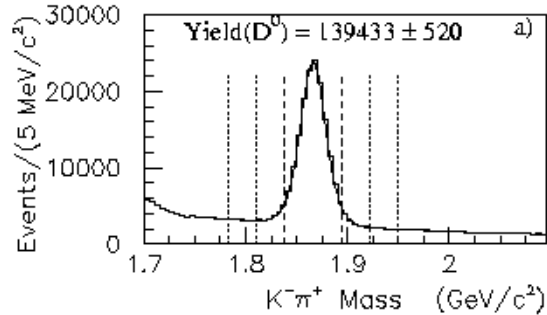
c) 793 evts

d) 2192 evts

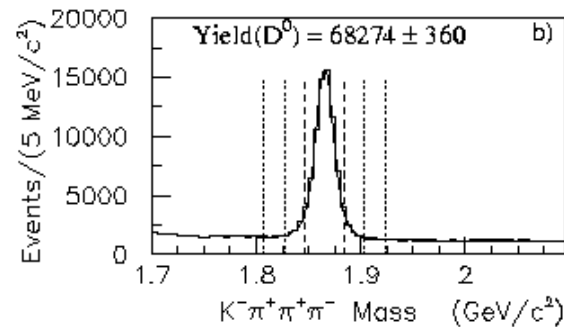
$$\frac{\Gamma(D_s^+ \rightarrow \phi \mu^+ \nu)}{\Gamma(D_s^+ \rightarrow \phi \pi^+)} = 0.54 \pm 0.033(stat) \pm 0.048(sys)$$

# Charm Meson Lifetimes

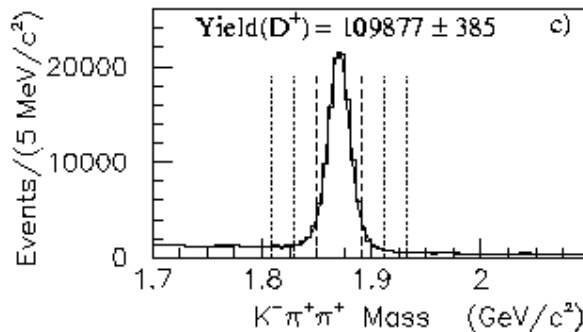
## $D^0, D^+$ Signal



$139433 \pm 520$  evts

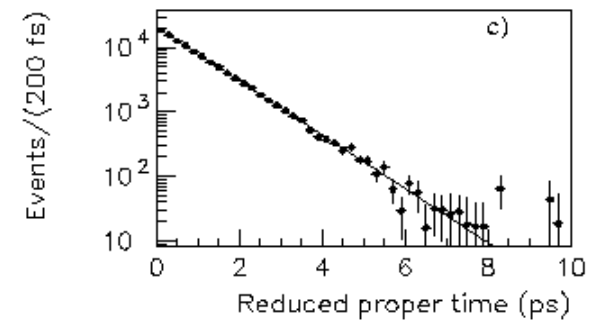
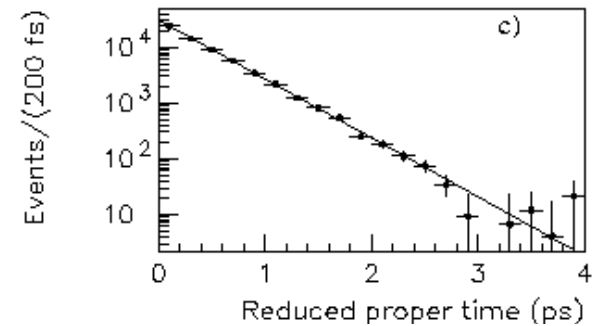
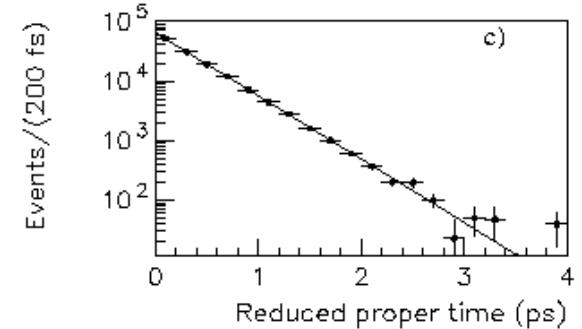


$68274 \pm 360$  evts



$109877 \pm 385$  evts

## $D^0, D^+$ Lifetime fits





$$\tau(D^0) = 409.6 \pm 1.1(stat) \pm 1.5(sys) \quad \text{fs}$$

$$\tau(D^+) = 1039.4 \pm 4.3(stat) \pm 7.0(sys) \quad \text{fs}$$

Phys.Lett.B537,192 ,2002

$$\frac{\tau(D^+)}{\tau(D^0)} = 2.538 \pm 0.023$$

<i>Exp</i>	$D^0 (\times 10^{-12} s)$	$D^+ (\times 10^{-12} s)$
<i>E687</i>	$0.413 \pm 0.004 \pm 0.003$	$1.048 \pm 0.015 \pm 0.011$
<i>CLEOII</i>	$0.4085 \pm 0.0041^{+0.0035}_{-0.0034}$	$1.0336 \pm 0.0221^{+0.0099}_{-0.0127}$
<i>E791</i>	$0.413 \pm 0.003 \pm 0.004$	
<i>FOCUS</i>	$0.4096 \pm 0.0011 \pm 0.0015$	$1.0394 \pm 0.0043 \pm 0.0070$

$$\frac{\Gamma(D^0 \rightarrow eX)}{\Gamma(D^+ \rightarrow eX)} = \frac{B(D^0 \rightarrow eX)}{B(D^+ \rightarrow eX)} \times \frac{\tau(D^+)}{\tau(D^0)} = 1.01 \pm 0.13$$

FOCUS

$$D^+ \rightarrow eX = (17.2 \pm 1.9)\%$$

$$D^0 \rightarrow eX = (6.87 \pm 0.28)\%$$

.....difference in the hadronic sector

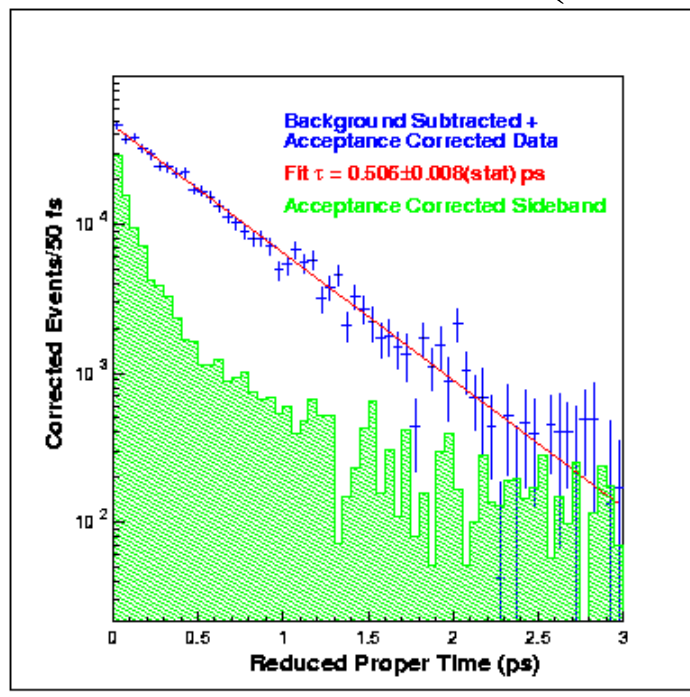
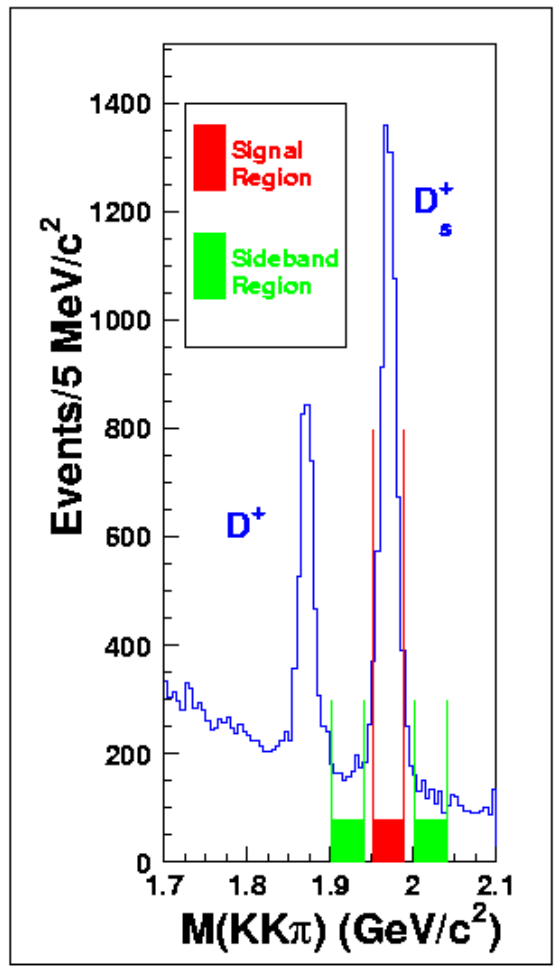
PDG2002

# $D_s \rightarrow \phi\pi$ signal

PDG 2002  $490 \pm 9$  fs

Lifetime  $506 \pm 8$  fs

$5668 \pm 95$  events (50% FOCUS data)



Preliminary

$$\frac{\tau(D_s)}{\tau(D^0)} = 1.23 \pm 0.02$$

4 x statistics including  $\overline{K}^*0 K$

Theoretical prediction (Bigi Uraltsev)  
 1.00-1.07 (no WA/WX)  
 0.8-1.27 (different process interference)



# Mixing

- Neutral charm mesons:

$$D^0 = c\bar{u}, \bar{D}^0 = \bar{c}u$$

- If  $H_{12}, H_{21} \neq 0$ , they are not eigenstates.

$$i\frac{\partial}{\partial t} \begin{pmatrix} D^0 \\ \bar{D}^0 \end{pmatrix} = \begin{pmatrix} H_{11} & H_{12} \\ H_{21} & H_{22} \end{pmatrix} \begin{pmatrix} D^0 \\ \bar{D}^0 \end{pmatrix}$$

where  $H_{ij} = M_{ij} - i\Gamma_{ij}/2$ .

- If CP is conserved,

$$D_{1,2} = (D^0 \pm \bar{D}^0) / \sqrt{2}$$

with mass and lifetime as

$$M_{1,2} = M \pm \Re[H_{12}H_{21}]^{1/2} = M \pm 1/2\Delta M$$

$$\Gamma_{1,2} = \Gamma \mp 2\Im[H_{12}H_{21}]^{1/2} = \Gamma \mp \Delta\Gamma$$

$$x = \frac{\Delta M}{\Gamma}; y = \frac{\Delta\Gamma}{2\Gamma}$$

Direct comparison of CP final state lifetime

$$D^0 \rightarrow K^+ K^- (CP+) \rightarrow \Gamma_2$$

$$D^0 \rightarrow K^- \pi^+ (\frac{1}{2}CP+ \& \frac{1}{2}CP-)$$

$$\rightarrow \Gamma(K^- \pi^+) \approx \frac{1}{2}(\Gamma_1 + \Gamma_2)$$

$$y_{CP} = \frac{\tau(D^0 \rightarrow K\pi)}{\tau(D^0 \rightarrow KK)} - 1$$

$$y_{CP} = (3.42 \pm 1.39 \pm 0.74)\%$$

Phys.Lett.B485,62,2000

# New Mixing Results

**Preliminary**



$$R(t) = e^{-t} \left( R_{DCS} + \sqrt{R_{DCS}} y' t + \frac{x'^2 + y'^2}{2} t^2 \right)$$

$$x' \equiv x \cos \delta + y \sin \delta$$

$$y' \equiv y \cos \delta - x \sin \delta$$

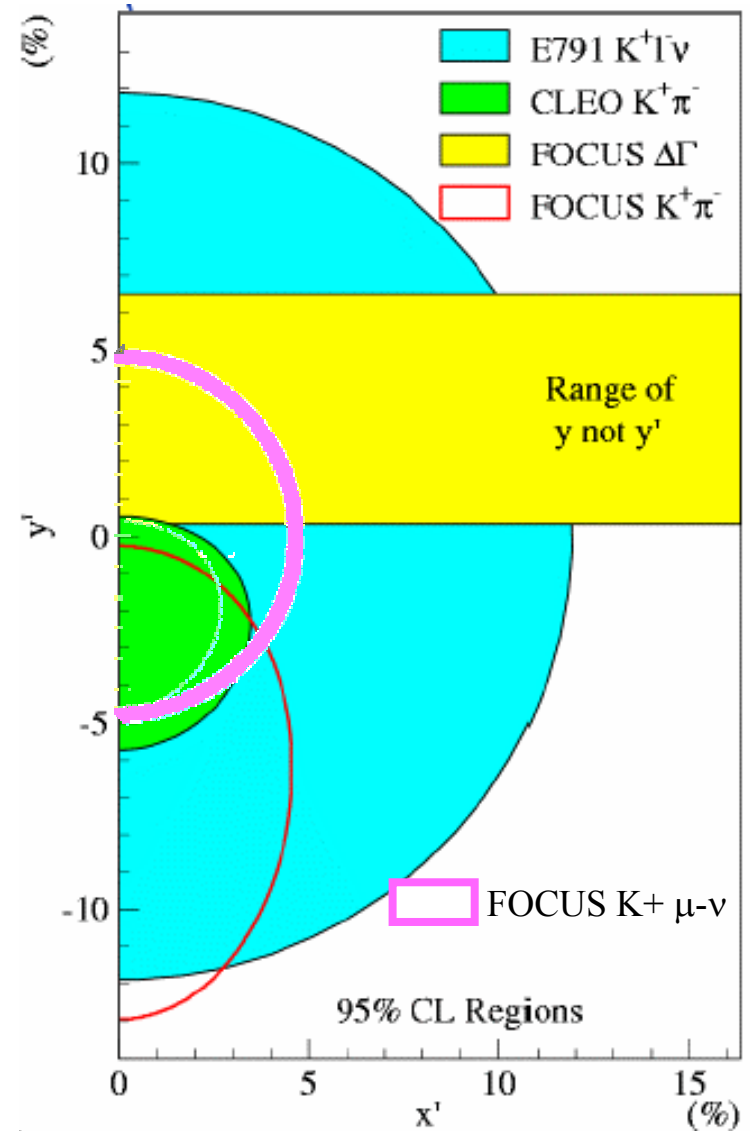
$\delta$  is the relative strong phase



$$r_{mix} < 0.0012 \quad @ 95\% \text{ C.L.}$$

**only statistical error !**

....towards CLEO & a big relative phase



# Conclusion

Charm physics is revealing itself a rich source  
of new results

**FOCUS** is playing a **crucial role** in understanding the charm  
phenomenology

**new suppressed decay modes**

**decay dynamics** of

three-body hadronic channels via quasi two-body decays  
semileptonic sector

**very precise lifetime measurements** (will dominate PDG)

**mixing**

