

# Measurement of $\pi^+\pi^-$ atom lifetime at DIRAC.

ICHEP02

Amsterdam, 25–31 July, 2002.

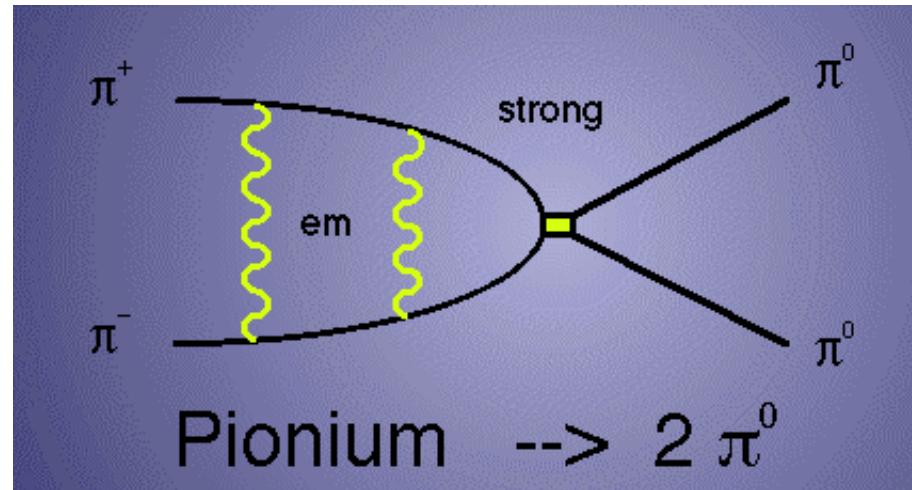
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Laboratory of Nuclear Problems,  
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# DIRAC

## DImeson Relativistic Atomic Complexes

Lifetime Measurement of  $\pi^+\pi^-$  atoms to test low energy QCD predictions.



Basel Univ., Bern Univ., Bucharest IAP, CERN, Dubna JINR, Frascati LNF-INFN, Ioannina Univ., Kyoto-Sangyo Univ., Kyushu Univ. Fukuoka, Moscow NPI, Paris VI Univ., Prague TU, Prague FZU-IP ASCR, Protvino IHEP, Santiago de Compostela Univ., Tokyo Metropolitan Univ., Trieste Univ./INFN, Tsukuba KEK, Waseda Univ.

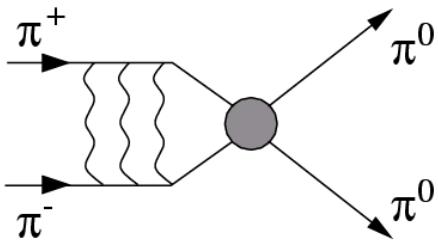
83 Physicists from 19 Institutes

# The Goal

The goal of the DIRAC Experiment is to measure the  $\pi^+ \pi^-$  atom lifetime of order  $3 \cdot 10^{-15}$  s with 10% precision. This measurement will provide in a model independent way the difference between S-wave  $\pi\pi$  scattering lengths  $|a_2 - a_0|$  with 5 % precision. Low energy QCD - chiral perturbation theory - predicts nowadays scattering lengths with very high accuracy  $\sim 2$  %. Therefore, such a measurement will be a sensitive check of the understanding of chiral symmetry breaking of QCD by giving an indication about the value of the quark condensate, an order parameter of QCD.

# Theoretical Motivation

$\pi^+\pi^-$  atoms ( $A_{2\pi}$ ) in the ground state decay by strong interaction mainly into  $\pi^0\pi^0$ .



$$\Gamma = \frac{1}{\tau} = \Gamma_{2\pi_0} + \Gamma_{2\gamma} \quad \frac{\Gamma_{2\gamma}}{\Gamma_{2\pi_0}} \approx 4 \times 10^{-3}$$

Chiral Perturbation Theory (ChPt), which describes the strong interaction at low energies provides, at NLO in isospin symmetry breaking, a precise relation between  $\Gamma_{2\pi}$  and the  $\pi\pi$  scattering lengths:

(Deser et al)

(Gall et al., Jalloli et al, Ivanov et al)

$$\Gamma_{2\pi^0}^{LO} = C |a_0 - a_2|^2$$

$$\Gamma_{2\pi^0}^{NLO} = \Gamma_{2\pi^0}^{LO} (1 + \delta\Gamma)$$

$a_0$  and  $a_2$  are the strong  $\pi\pi$  S-wave scattering lengths for isospin I=0 and I=2.

$$\delta\Gamma = (5.8 \pm 1.2)\% \quad \Rightarrow \quad \tau = (2.9 \pm 0.1) \times 10^{-15} s$$

$$\sigma\tau / \tau = 10\% \quad \Rightarrow \quad \sigma(a_0 - a_2) / (a_0 - a_2) = 5\%$$

# Theoretical Status

In ChPT the effective Lagrangian which describes the  $\pi\pi$  interaction is an expansion in (even) terms:

$$L_{eff} = L^{(2)} + L^{(4)} + L^{(6)} + \dots$$

1966 Weinberg (tree):	$L^{(2)}$	$a_0 - a_2 = 0.20$
1984 Gasser-Leutwyler (1-loop):	$L^{(4)}$	$a_0 - a_2 = 0.25 \pm 0.01$
1995 Knecht et al. (2-loop):	$L^{(6)}$	gChPT
1996 Bijnens et al. (2-loop):	$L^{(6)}$	$a_0 - a_2 = 0.258 \pm (< 3\%)$
2001 Colangelo et al. (& Roy):	$L^{(6)}$	$a_0 - a_2 = 0.265 \pm 0.004(1.5\%)$

And the theoretical results for the scattering lengths up to 2-loops are:

	Tree (Weinberg)	1-loop (Gass.&Leut.)	2-loop (Bijnens et al.)	2loop+Roy (Colangelo et al.)
$a_0$	0.16	0.203	0.219	0.220
$a_2$	-0.045	-0.043	-0.042	-0.044

# Experimental Status

Experimental data on  $\pi\pi$  scattering lengths can be obtained via the following indirect processes:

Model independent,  $K^+ \rightarrow \pi^+ \pi^- e^+ \nu_e$  ( $K_{e4}$ )

$$a_0 = 0.28 \pm 0.05 \quad \text{L. Rosselet et al., Phys. Rev. D 15 (1977) 574}$$

$$a_0 = 0.26 \pm 0.05 \quad \begin{aligned} &\text{M.Nagels et al., Nucl.Phys. B 147 (1979) 189} \\ &\text{Combined analysis of } K_{e4}, \text{ Roy equation and peripheral reaction} \\ &\pi N \rightarrow \pi\pi N \text{ data} \end{aligned}$$

$$\begin{aligned} a_0 &= 0.216 \pm 0.013 \pm 0.004 (\text{syst}) && \text{New measurement at BNL (E865)} \\ &\pm 0.005 (\text{theor}) && \text{S.Pislak et al., Phys.Rev.Lett. 87 (2001) 221801} \end{aligned}$$

Model dependent:  $\pi N \rightarrow \pi\pi N$  near threshold

$$a_0 = 0.26 \pm 0.05 \text{ } m_\pi^{-1} \quad \text{C.D. Froggatt, J.L. Petersen, Nucl. Phys. B 129 (1977) 89}$$

...

$$a_0 = 0.204 \pm 0.014 \pm 0.008 (\text{syst}) \quad \text{M. Kermani et al., Phys. Rev. C 58 (1998) 3431}$$

# $A_{2\pi}$ production

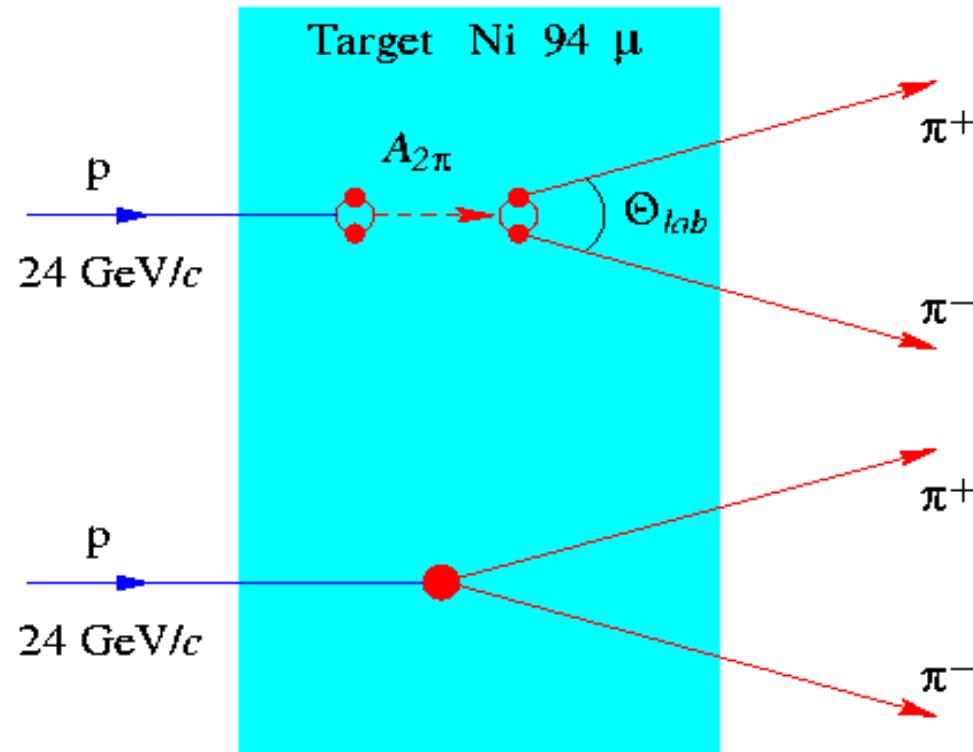
- The pionic atoms are produced by the Coulomb interaction of a pion pair in proton-target collisions (Nemenov):
- Also free Coulomb pairs are created in the proton-target collisions.
- The atom production is proportional to the low relative momentum Coulomb pairs production ( $N_A = K \times N_C$ ).
- The pionic atoms evolve in the target and some of them ( $n_A$ ) are broken. The broken atomic pairs are emitted with small C.M.S. relative momentum ( $Q < 3 \text{ MeV}/c$ ) and opening angle  $\Theta < 0.3 \text{ mrad}$ .
- DIRAC aims to detect and identify Coulomb and atomic pairs samples to calculate the break-up probability  
 $P_{br} = n_A / N_A$

Wave function at origin (accounts for Coulomb interaction).

$$\frac{d\sigma_{nlm}^A}{d\vec{P}} = (2\pi)^3 \frac{E}{M} \left| \psi_{nlm}^{(C)}(0) \right|^2 \frac{d\sigma_s^0}{d\vec{p} d\vec{q}} \Big|_{\vec{p}=\vec{q}}$$

Lorentz Center of Mass to Laboratory factor.

Pion pair production from short lived sources.



# Lifetime and breakup probability

The  $P_{br}$  value depends on the lifetime value,  $\tau$ . To obtain the precise  $P_{br}(\tau)$  curve a large differential equation system must be solved:

$$\frac{dp_{nlm}(s)}{ds} = \sum_{n'l'm'} a_{nlm}^{n'l'm'} p_{n'l'm'}(s)$$

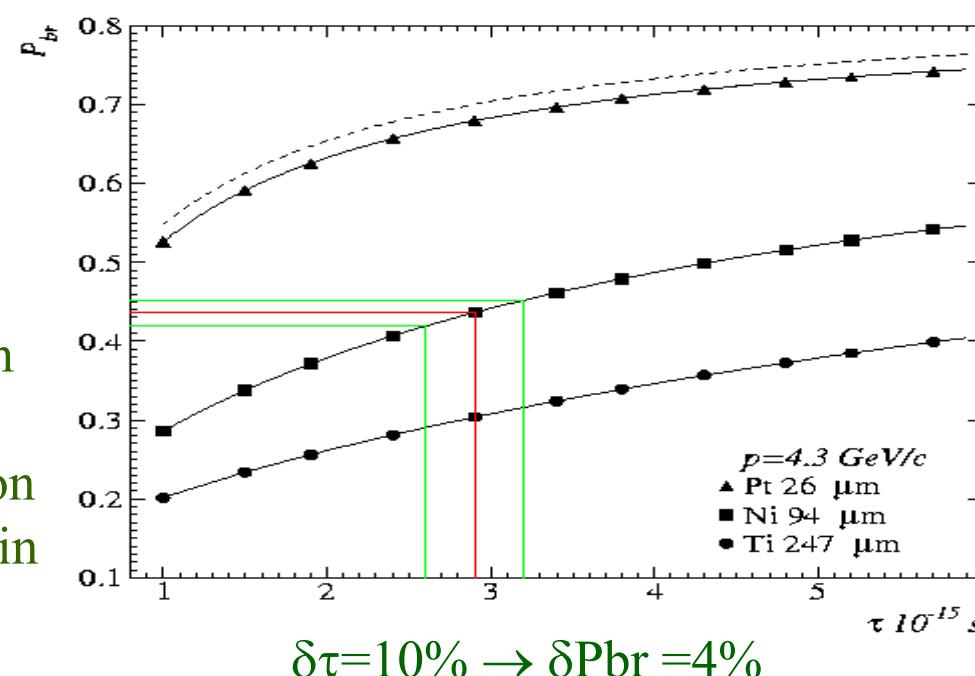
where  $s$  is the position in the target,  $p_{nlm}$  is the population of a definite hydrogen-like state of pionium. The  $a_{nlm}^{n'l'm'}$  coefficients are given by:

$$a_{nlm}^{n'l'm'} = \frac{\sigma_{nlm}^{n'l'm'} \rho N_0}{A}, \text{ if } nlm \neq n'l'm', a_{nlm}^{nlm} = -\frac{\sigma_{nlm}^{tot} \rho N_0}{A}$$

$$-\begin{cases} 2M_\pi / P c \tau_n & l=0. \\ 0 & l \neq 0. \end{cases}$$

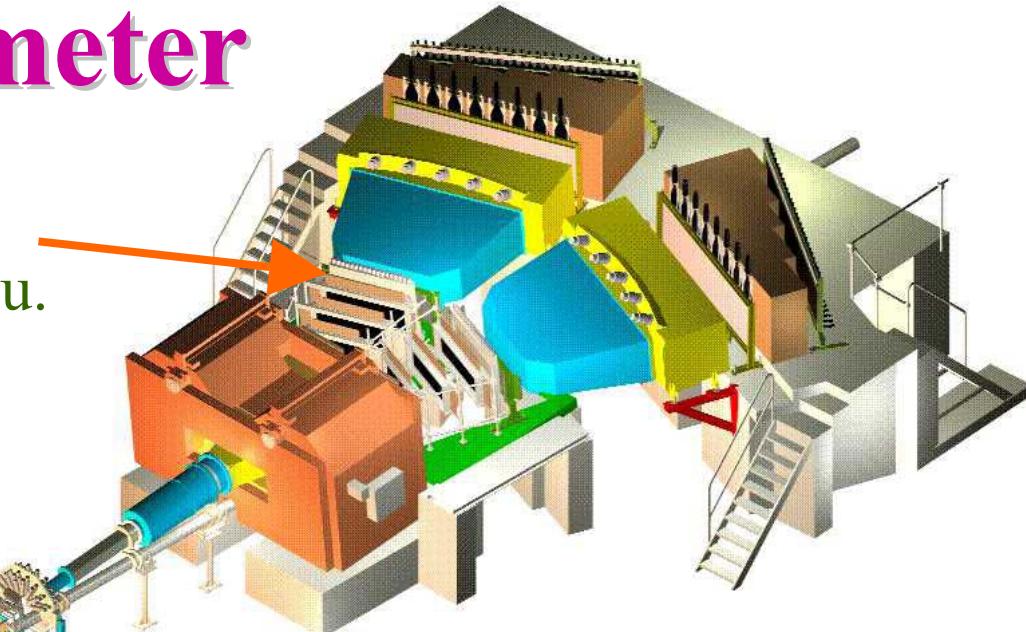
$\sigma_{nlm}^{n'l'm'}$  being the electro-magnetic pionium-target atom cross section,  $N_0$  the Avogadro Number,  $\rho$  the material density and  $A$  its atomic weight.

The detailed knowledge of the cross sections (Afanasyev&Tarasov; Trautmann et al) (Born and Glauber approach) together with the accurate solution of the differential equation system permits us to know the curves within 1%.

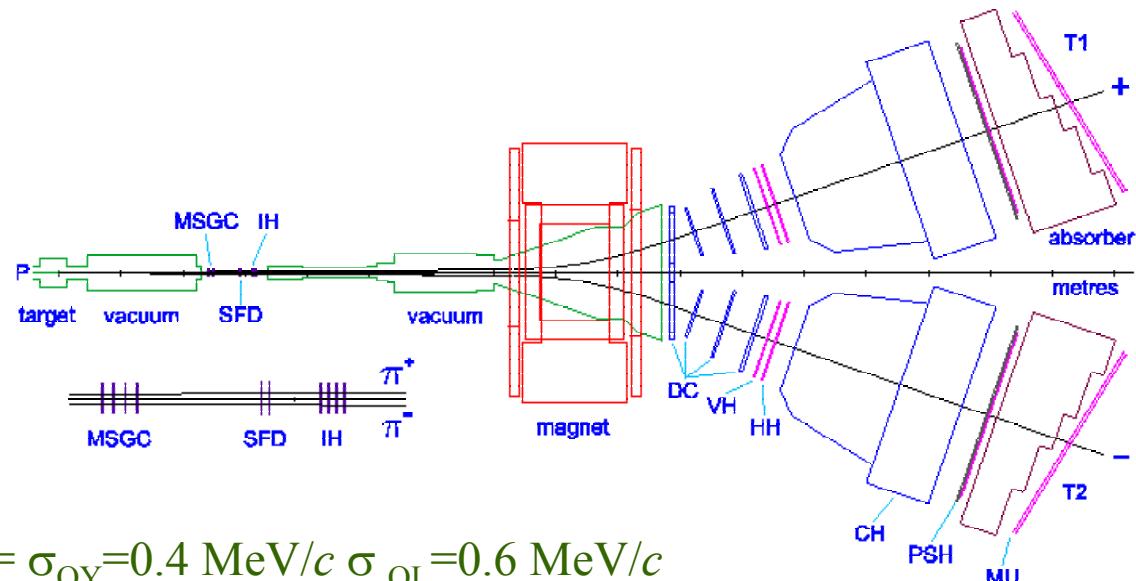
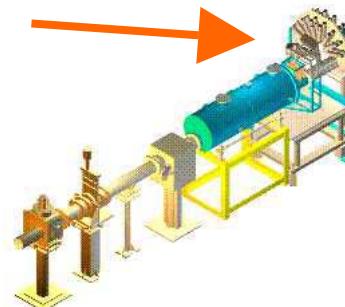


# DIRAC Spectrometer

Downstream detectors:  
DCs, VH, HH, C, PSh, Mu.



Upstream detectors:  
MSGCs, SciFi, IH.



Setup features:

angle to proton beam  $\Theta=5.7^\circ$

channel aperture  $\Omega=1.2 \cdot 10^{-3}$  sr

magnet  $1.85 \text{ T} \cdot \text{m}$

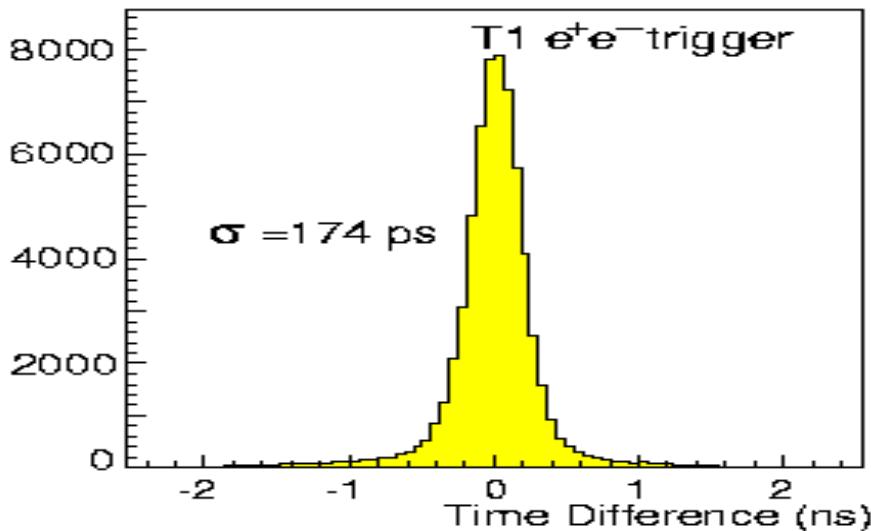
momentum range  $1.2 \leq p_\pi \leq 7 \text{ GeV}/c$

resolution on relative momentum  $\sigma_{QX} = \sigma_{QY} = 0.4 \text{ MeV}/c$   $\sigma_{QL} = 0.6 \text{ MeV}/c$

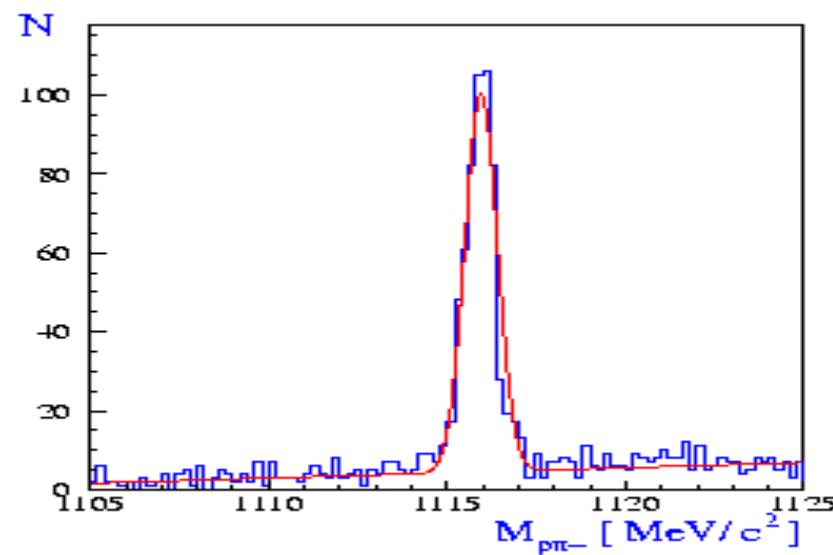
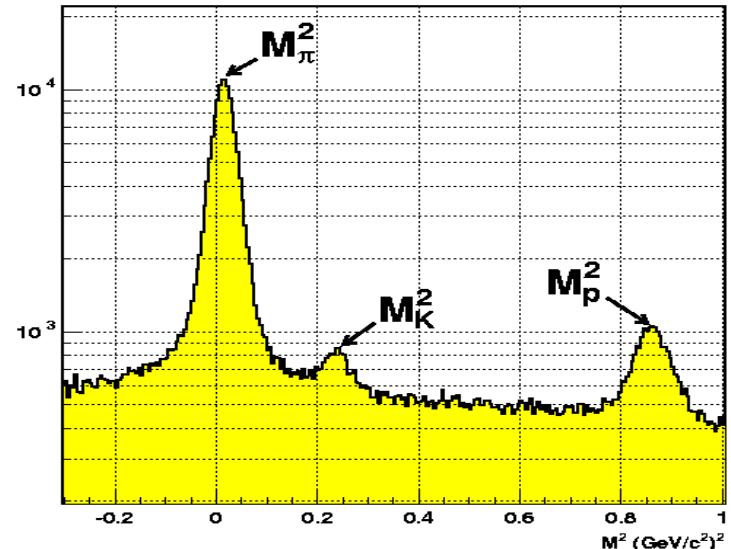
# Calibration

These results show that our set-up fulfils the needs in time and momentum resolution.

Positive arm mass spectrum,  
obtained by time difference at   
VHs, under  $\pi^-$  hypothesis in the  
negative arm.



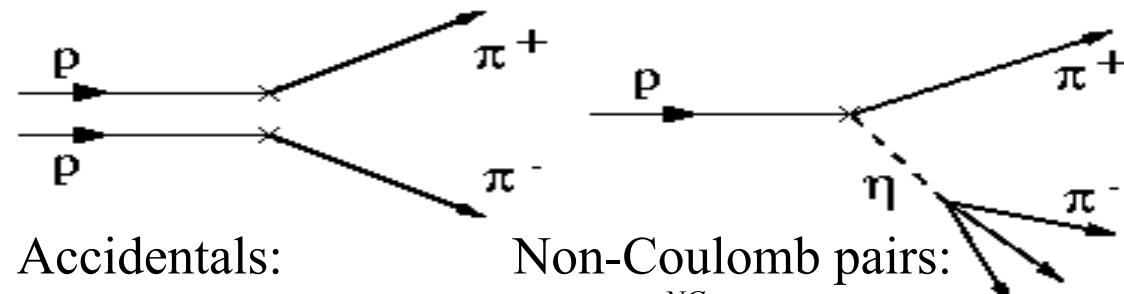
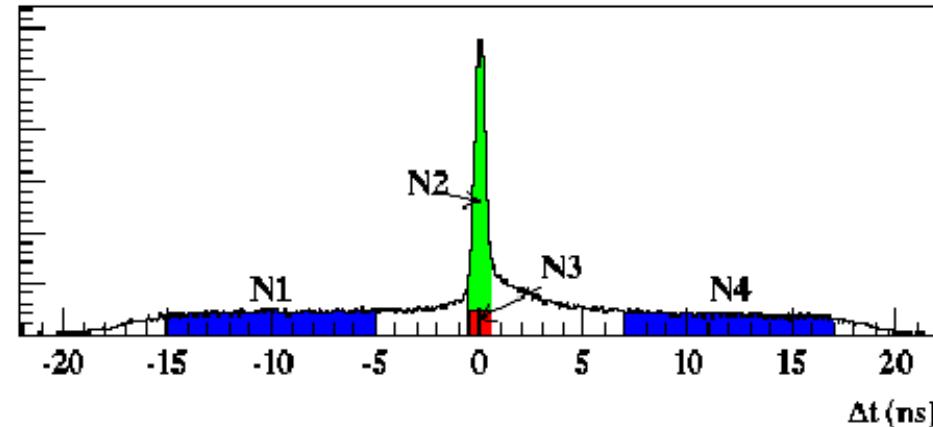
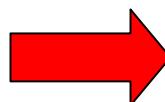
Time difference spectrum  
at VH with  $e^+e^-$  T1 trigger.



Mass distribution of  $\pi\pi^-$  pairs  
from  $\Lambda$  decay.  $\sigma_\Lambda = 0.43 \text{ MeV}/c^2$   
 $< 0.49 \text{ MeV}/c^2$  (Hartouni et al.).

# Atoms detection

The time spectrum at VH provides us the criterion to select real (time correlated) and accidental (non correlated) pairs.



Accidentals:

$$\frac{dN_{acc}}{dQ}$$

Non-Coulomb pairs:

$$\frac{dN_{corr}^{NC}}{dQ} \propto \frac{dN_{acc}}{dQ}$$

Coulomb pairs:

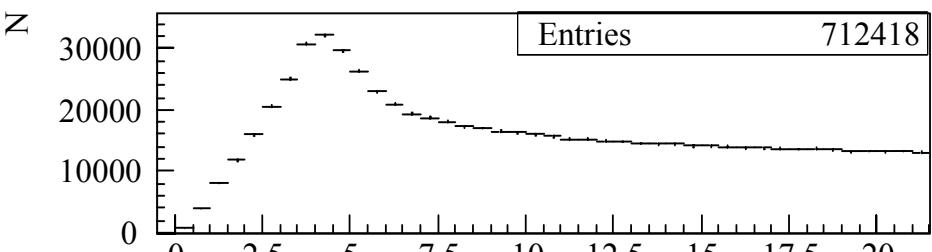
$$\frac{dN_{corr}^C}{dQ} \propto A_C(Q) \frac{dN_{acc}}{dQ}$$

$$R(Q) = \frac{\frac{dN_{corr}}{dQ}}{\frac{dN_{acc}}{dQ}} = \frac{\frac{dN_{corr}^{NC}}{dQ} + \frac{dN_{corr}^C}{dQ}}{\frac{dN_{acc}}{dQ}} = N[A_C(Q) + f]$$

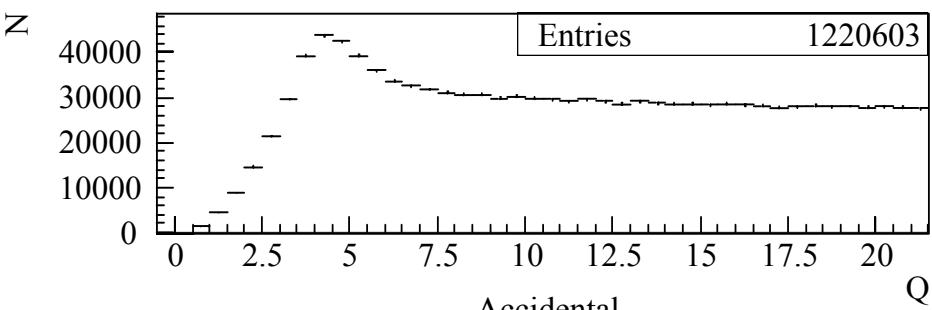
$N$  and  $f$  are obtained from a fit to the pion pairs  $Q$  spectrum in the range without atomic pairs  $Q > 3 \text{ MeV}/c$

# Atoms detection

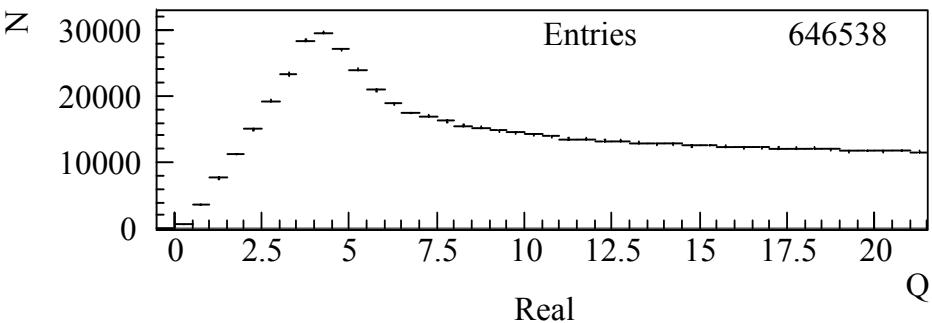
Ni 2001 data



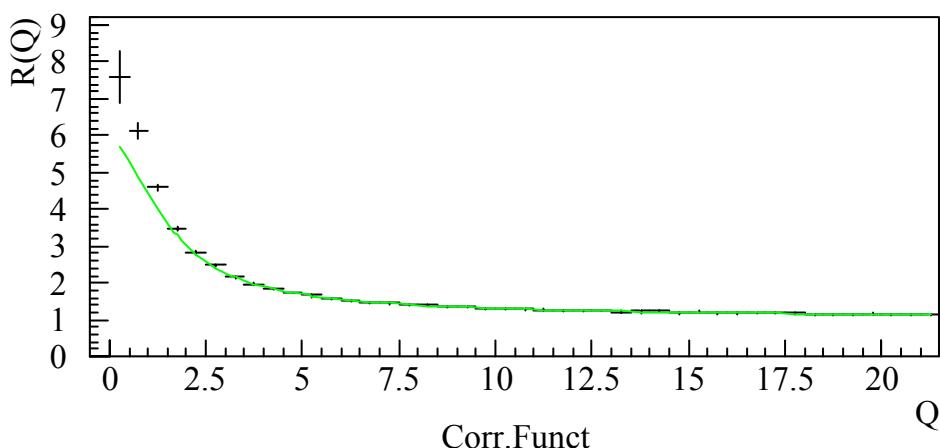
Real+Accidental



Accidental

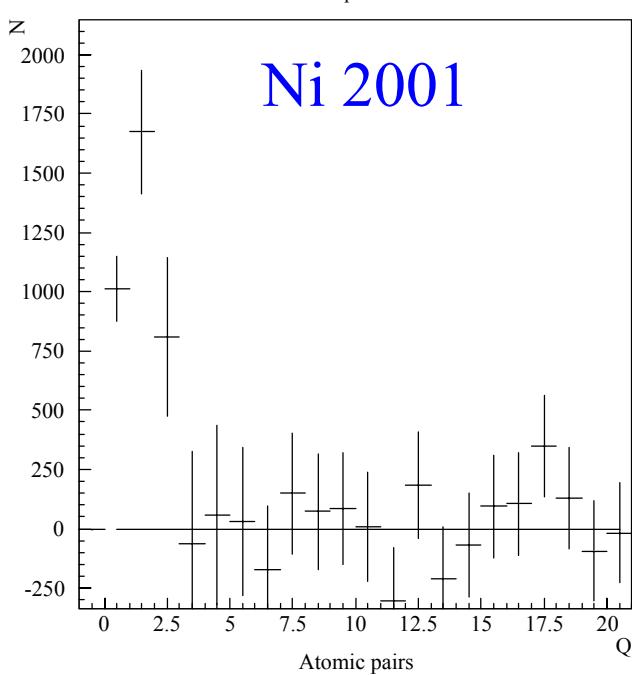
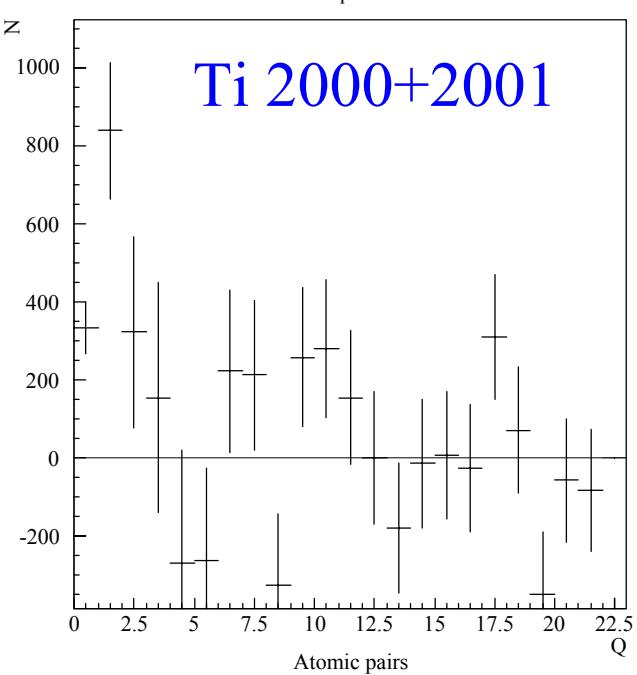
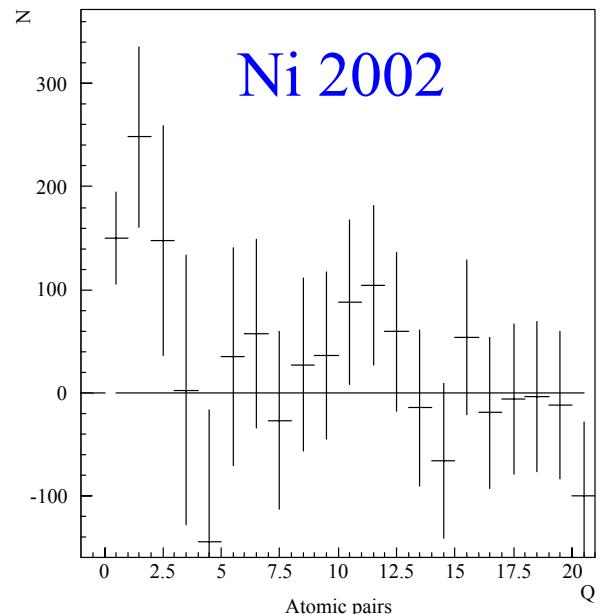
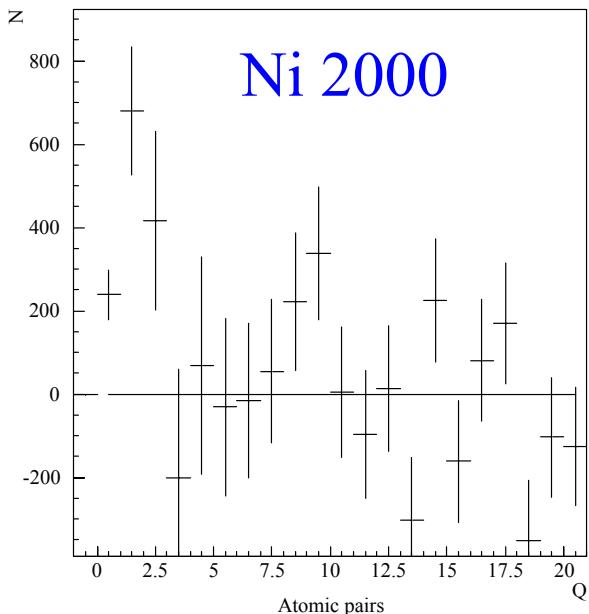
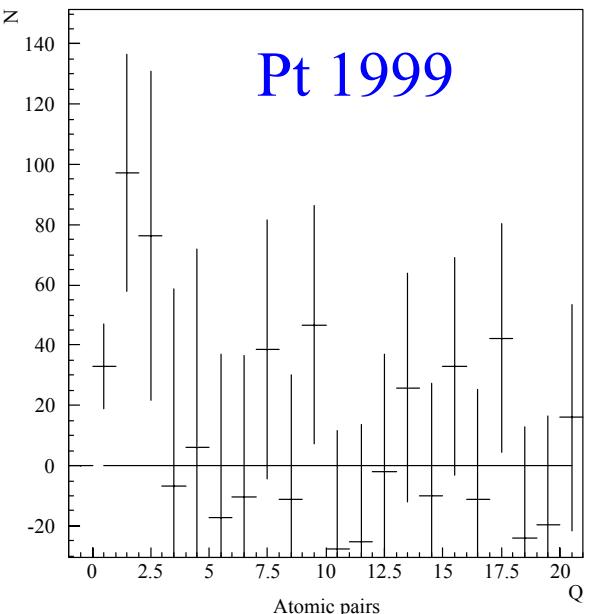


Real



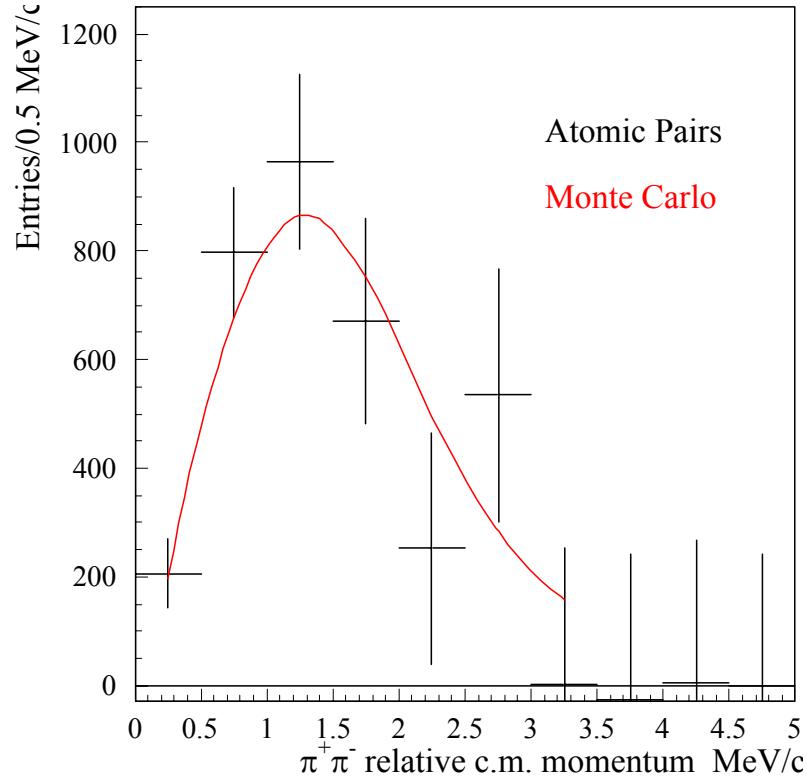
Corr.Funct

# Atomic Pairs



Target	$Z$	Thick ( $\mu m$ )
Pt	78	28
Ni 2000	28	94
Ni 2001		98
Ti	22	251

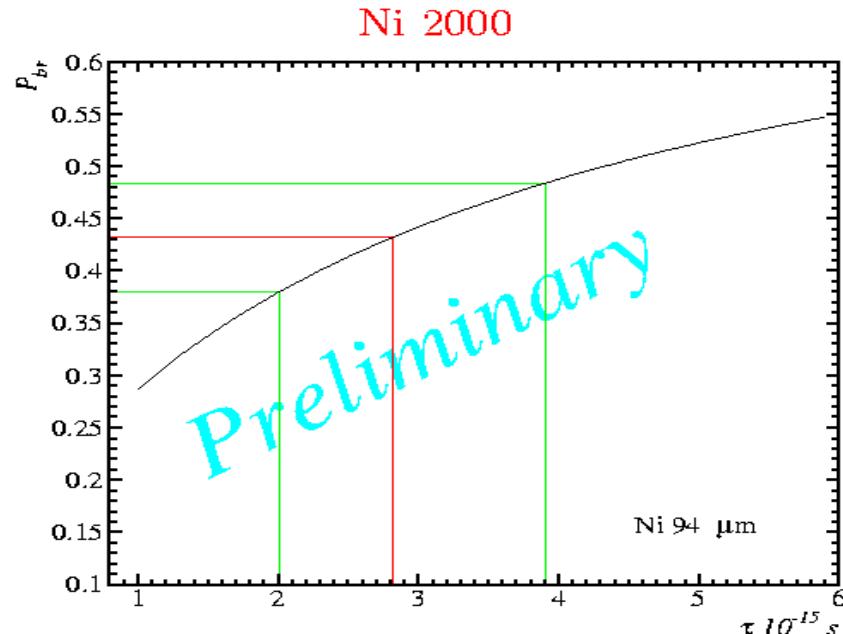
# Atomic pairs



Sample	Triggers $10^6$	$n_a$ at $Q < 2 \text{ MeV}/c$	$n_a$ at $Q < 3 \text{ MeV}/c$
Pt 1999	55.7	$130 \pm 43$ (3.σ)	$207 \pm 77$ (2.7σ)
Ni 2000	896	$920 \pm 170$ (5.4σ)	$1335 \pm 300$ (4σ)
Ti 2000+01	910	$1170 \pm 190$ (6.2σ)	$1495 \pm 340$ (4.4σ)
Ni 2001	647	$2686 \pm 310$ (8.7σ)	$3500 \pm 510$ (6.9σ)
Ni 2002 (15 day)	77	$400 \pm 100$ (4σ)	$545 \pm 170$ (3.2σ)

# Conclusions and results

Sample	Lifetime $10^{-15}$ s	Statistical error
Ni 2000	$2.8^{+1.1}_{-0.8}$	$\pm 34\%$
Ti 2000/1	$5.4^{+1.5}_{-1.3}$	$\pm 26\%$
Ni +Ti	$3.6^{+0.9}_{-0.7}$	$\pm 22\%$



- DIRAC collaboration has built up the double arm spectrometer which achieves 1 MeV/c resolution at low relative momentum ( $Q < 30$  MeV/c) of particle pairs and has successfully demonstrated its capability to detect  $\pi^+\pi^-$  atoms after 2 years of running time.
- Some preliminary lifetime results have been achieved with a 5000 atoms sample reaching an statistical accuracy of 22% in lifetime determination.
- The accurate determination of systematical errors requires a measurement of the background.
- A 10% accuracy on the atom lifetime value (goal of the experiment) will require running beyond 2002.