



Inflationary Dynamics -

a Dissipative Quantum Field Theory Process

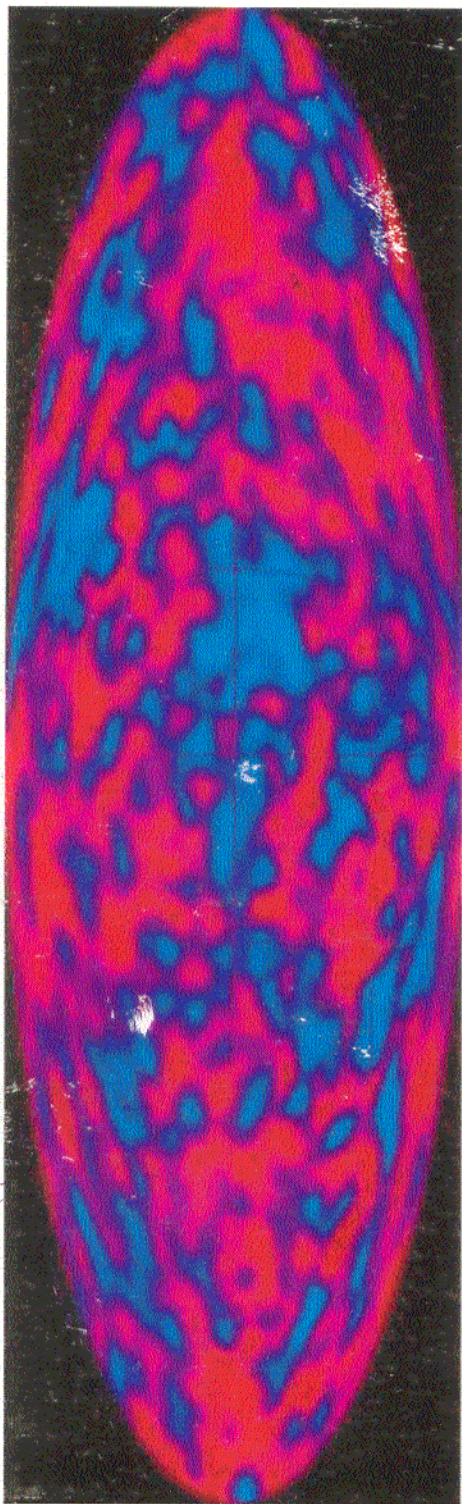
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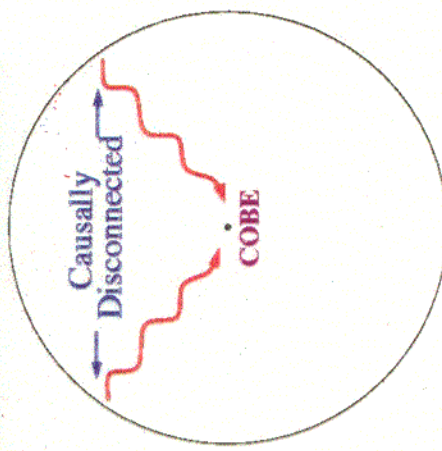
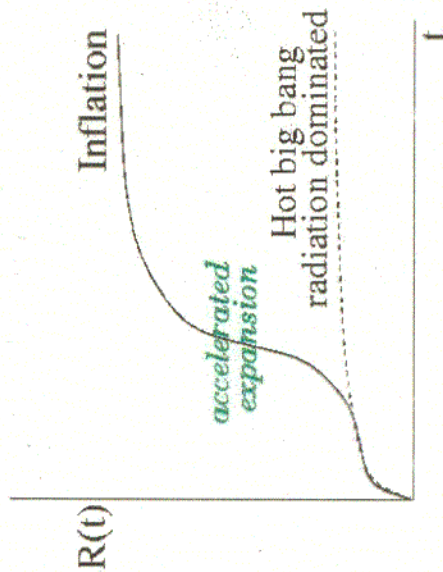
Inflation



The puzzle of cosmological initial conditions:

$$\frac{\Delta T}{T} < 10^{-5} \text{ in CMBR without causal contact}$$

The inflation solution (1981+)

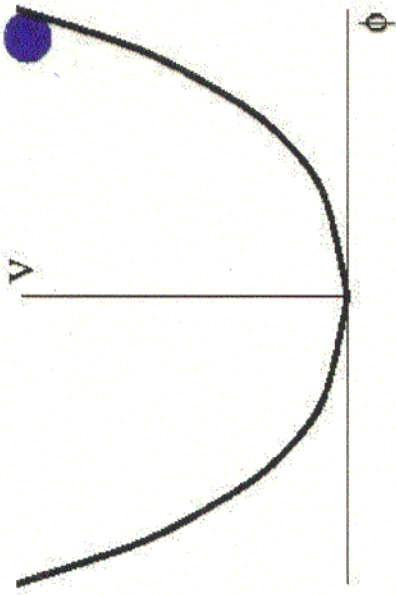


Accelerated expansion $\ddot{R}(t) > 0$

implies $\rho + 3p < 0$

How to get this from high energy physics?

Scalar field ("inflaton") dynamics



$$\rho = \dot{\phi}^2/2 + V(\phi) + (\nabla\phi)^2/2R^2$$

$$p = \dot{\phi}^2/2 - V(\phi) - (\nabla\phi)^2/6R^2$$

$$\ddot{\phi} + 3H\dot{\phi} + V'(\phi) = 0$$

= Supercooled Inflation.

Just Choose $V(\phi)$

Potential energy dominated $3H\dot{\phi} \gg \ddot{\phi}$, "slow-roll"

But what about particle creation?

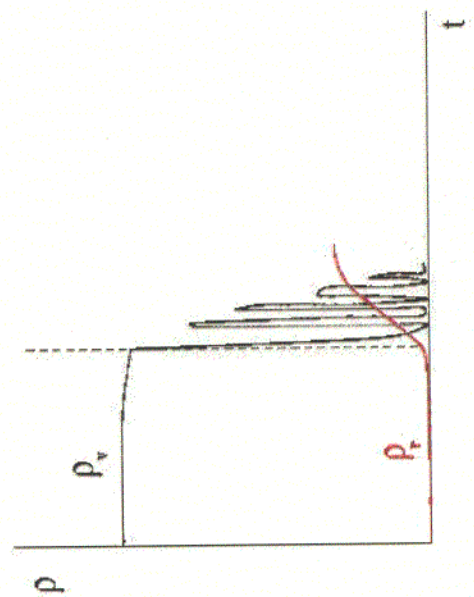
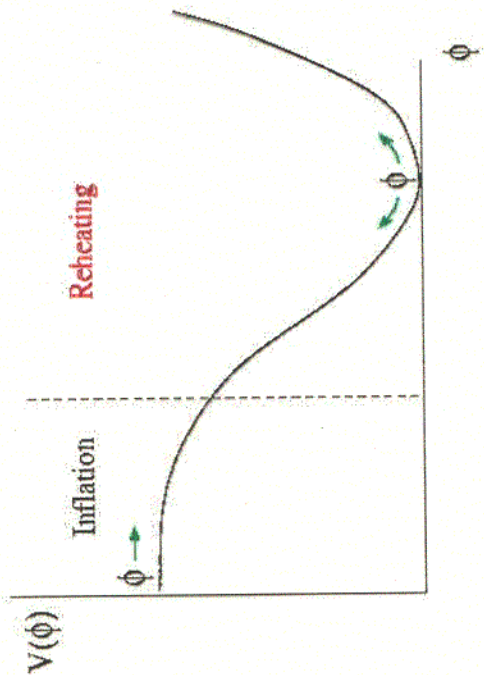
$$\ddot{\phi} + 3H\dot{\phi} + \eta\dot{\phi} + V'(\phi) = 0$$

Warm inflation: η dominates

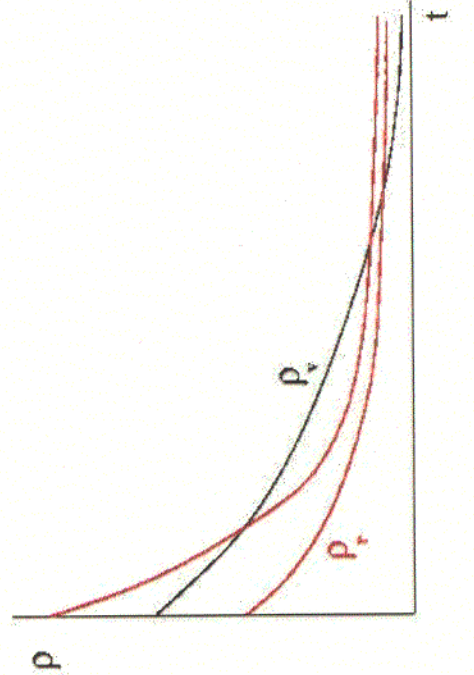
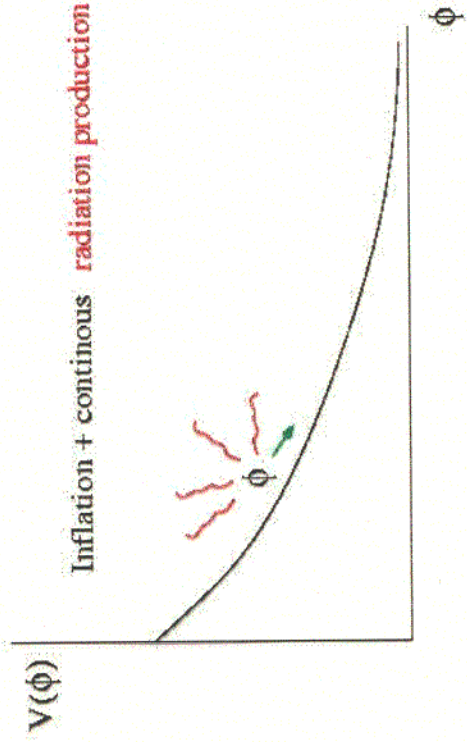
Slow-roll now means $\eta\dot{\phi} \gg 3H\dot{\phi}, \ddot{\phi}$, overdamped

The Warm Inflation Difference

Supercooled Inflation



Warm Inflation



Supercooled inflation: ϕ is isolated

– but interactions are more plausible: Warm inflation

Implies calculate

Relevant quantum mechanical process (dissipation) already studied in Condensed Matter: Caldeira–Leggett model, Fermi–Ulam–Pasta model

In Quantum Field Theory (QFT) generic couplings,
 $\phi^2 \chi^2, \phi \bar{\psi} \psi$ yield dissipation

In restrictive cases, QFT warm inflation solutions have been obtained – confirms that warm inflation works

Considerable exploration remains

Energetics

Consider GUT scale inflation: $M \sim 10^{15} \text{ GeV}$, $\rho_v \sim M^4 \sim 10^{60} \text{ GeV}^4$

$$\Rightarrow H \sim 10^{10} \text{ GeV}$$

$T > H$ requires > 1 part in $\sim 10^{20}$ of vacuum energy

→ radiation

(influences structure formation)

$T > 1 \text{ GeV}$ requires > 1 part in $\sim 10^{60}$ $\rho_v \rightarrow \rho_r$

(makes reheating unnecessary)

Supercooled inflation Basic Assumption: Scalar field isolated, will NOT dissipate the above amounts during inflation

Warm inflation: Expects above, or even more, radiation production during inflation

Equipartition Hypothesis of Statistical Mechanics: would expect the scalar field to distribute its energy evenly amongst all degrees of freedom

Dynamical Question: Will the relevant time scales during inflation prohibit the minute' radiation production given above?

Scalar Field (Φ) Dynamics

$$\mathcal{L}_\Phi = \frac{1}{2}(\partial_\mu \Phi)^2 - \frac{m_\phi^2}{2}\Phi^2 - \frac{\lambda}{4!}\Phi^4$$

$$\mathcal{L}_I = \Phi \sum_{j=1}^{N_\psi} h_j \bar{\psi}_j \psi_j, \frac{1}{2} \sum_{j=1}^{N_\chi} g_j^2 \chi_j^2 \Phi^2$$

$$\Phi = \varphi + \phi$$

Effective equation of motion (EOM) for $\varphi(t)$:

$$\begin{aligned} \ddot{\varphi}(t) + m_\phi^2 \varphi(t) + \frac{\lambda}{6} \varphi^3(t) + \frac{\lambda}{2} \varphi(t) \langle \phi^2 \rangle \\ + \frac{\lambda}{6} \langle \phi^3 \rangle + \varphi(t) \sum_{j=1}^{N_\chi} g_j^2 \langle \chi_j^2 \rangle = 0 \end{aligned}$$

$\langle \phi^2 \rangle$, $\langle \phi^3 \rangle$ and $\langle \chi_j^2 \rangle$ perturbative evaluation
2-loop order

Closed Time Path Approach - Goal

Compute

$$\langle \hat{O}(t) \rangle \equiv \frac{\text{Tr}(\hat{\rho}(t)\hat{O})}{\text{Tr}(\hat{\rho}(t))}$$

Thermal initial state at $T^<$:

$$\rho(T^<) = \exp(-\beta H) = U(T^< - i\beta, T^<)$$

($U(t, t') \equiv \exp[-iH(t - t')]$, time evolution operator)

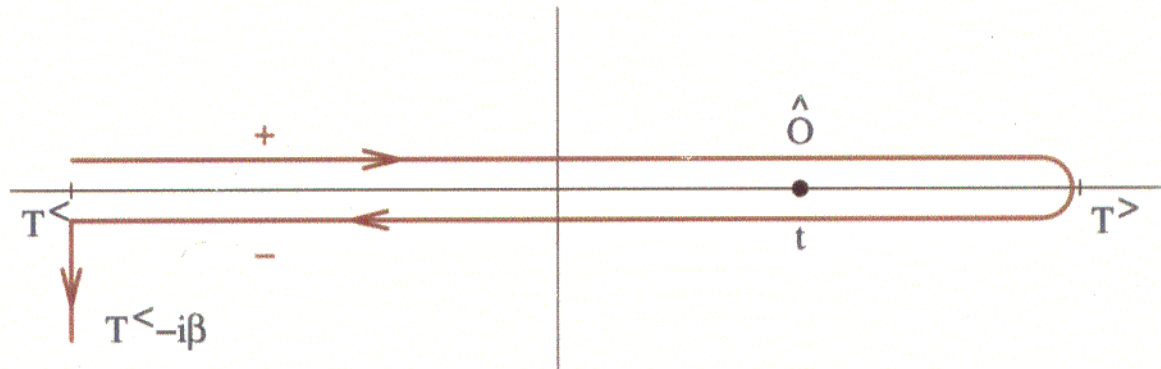
Thus

$$\langle \hat{O}(t) \rangle = \frac{\text{Tr}[U(T^< - i\beta, T^<)U(T^<, t)\hat{O}U(t, T^<)]}{\text{Tr}[U(T^< - i\beta, T^<)]}$$

Also add large positive time $T^>$

$$\langle \hat{O}(t) \rangle = \frac{\text{Tr}[U(T^< - i\beta, T^<)U(T^<, T^>)U(T^>, t)\hat{O}U(t, T^<)]}{\text{Tr}[U(T^< - i\beta, T^<)]}$$

Closed Time Path Approach - Method



Can express as a path integral

recall $U(t, t') \equiv \int \mathcal{D}\Phi \exp \left(i \int_{t'}^t d^4x \mathcal{L}[\Phi] \right)$

$$Z[J^+, J^-, J^\beta]$$

$$= \text{Tr}[U(T^< - i\beta, T^<; J^\beta) U(T^<, T^>; J^-) U(T^>, T^<; J^+)]$$

$$= \int \mathcal{D}\Phi^+ \mathcal{D}\Phi^- \mathcal{D}\Phi^\beta$$

$$\exp \left(i \int_{T^<}^{T^>} d^4x [\mathcal{L}^{J^+}[\Phi^+] - \mathcal{L}^{J^-}[\Phi^-]] + i \int_{T^<}^{T^<-i\beta} d^4x \mathcal{L}^{J^\beta}[\Phi^\beta] \right)$$

e.g. scalar field theory:

$$\mathcal{L}^J[\Phi] = \frac{1}{2} [\partial_\mu \Phi \partial^\mu \Phi - m^2 \Phi^2] - \frac{\lambda}{4!} \Phi^4 + J\Phi$$

ROBUST DISSIPATIVE MECHANISM

(Berera and Ramos, Phys. Rev. D 63, 103509 (2001))

Focus on Lagrangian:

$$\begin{aligned} \mathcal{L}[\Phi, \chi_j, \bar{\psi}_k, \psi_k] = & \frac{1}{2}(\partial_\mu \Phi)^2 - \frac{m_\phi^2}{2}\Phi^2 - \frac{\lambda}{4!}\Phi^4 \\ & + \sum_{j=1}^{N_\chi} \left\{ \frac{1}{2}(\partial_\mu \chi_j)^2 - \frac{m_{\chi_j}^2}{2}\chi_j^2 - \frac{f_j}{4!}\chi_j^4 - \frac{g_j^2}{2}\Phi^2\chi_j^2 \right\} \\ & + \sum_{i=1}^{N_\psi} \bar{\psi}_i \left[i \not{\partial} - m_{\psi_i} - \sum_{j=1}^{N_\chi} h_{ij,\chi} \chi_j \right] \psi_i, \end{aligned} \quad (1)$$

Implies reaction: $\phi \rightarrow \chi \rightarrow \psi$

Regime $m_\chi > 2m_\psi > m_\phi$: copious radiation production

e.g. GUT scale $V^{1/4}(\phi) \sim 10^{15} \text{ GeV} \implies T \sim 10^{14} \text{ GeV}$

PHYSICAL PICTURE

(Berera, Ramos, Lawrence)

-The evolution of $\varphi(t)$ changes χ -mass $\implies \chi$ -particle production from mixing $+/-$ frequency modes

(If left intact, quantum correlations of χ -field persist)

-Coupling χ to lighter ψ -field $\implies \chi$ -particles decay to ψ -particles, decohere χ -field

-Entire process backreacts on $\varphi \implies$ dissipative effects

Estimates of Dissipation from Quantum Field Theory Dynamics

R Ramos + A. B.
hep-ph/0101049
Phys. Rev. D 2001

Treat inflationary conditions: Overdamped, ultraflat potential

Direct Decay Models $\phi \rightarrow \bar{\psi}\psi, \chi\chi$ ($m_\phi > 2m_{\psi,\chi}$)

$$T \sim (\rho_r/g^*)^{1/4} \sim \lambda^{1/2} m_\phi / 10$$

$$\rho_v^{1/4} \sim 10^{15-16} \text{ GeV (GUT scale)}$$

$$\lambda \sim 10^{-(10-16)}$$

$$m_\phi \sim 10^{(10-13)} \text{ GeV}$$

$$\Rightarrow T \sim 10 - 10^7 \text{ GeV}$$

Sets lower bound on radiation production from generic QFT models consistent with inflation

\Rightarrow Reheating redundant

No gravitino overproduction in SUSY versions

Indirect Decay Models $\phi \rightarrow \chi \rightarrow \bar{\psi}\psi$ ($m_\phi < 2m_\psi < m_\chi$)

For same parameter regime, T as large as 10^{14} GeV

- Copious radiation production

Very interesting regime, needs more study

The warm inflationary universe on a computer

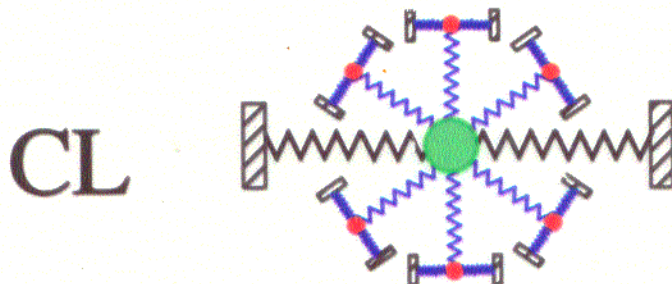
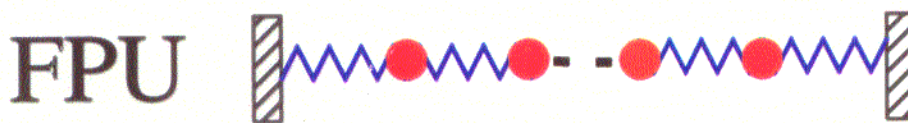
A.B. with

G.Lacagnina (*lattice gauge theory*), C.Verdozzi (*condensed matter theory*)

- study of **overdamped motion** and its universal features;
- study of how **equipartition** is achieved

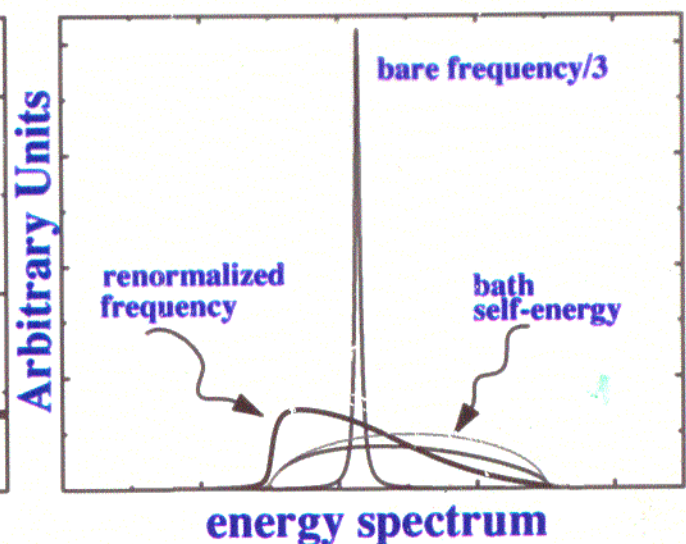
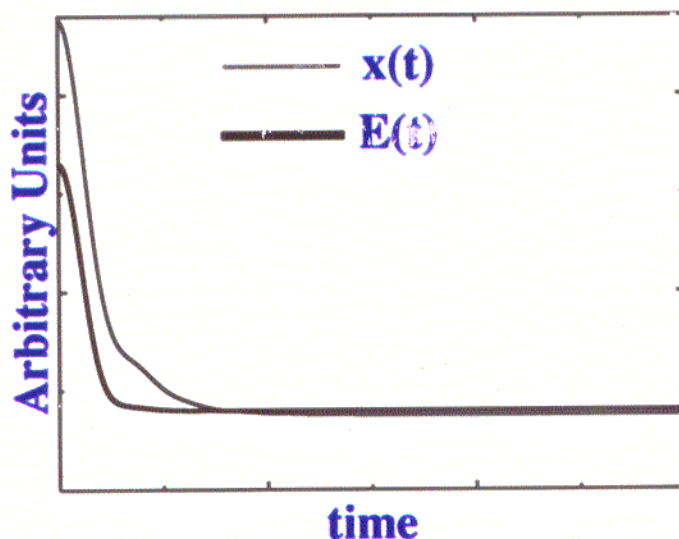
Conceptually / practically important and FEASIBLE Goals:

- 1) Numerical simulations of **quantum/classical** models from condensed matter: **Fermi-Pasta-Ulam, Caldeira-Leggett**



- 2) Simulations of lattice quantum field theory models: **Caldeira-Leggett, ϕ^4**

An example of overdamping in the classical regime

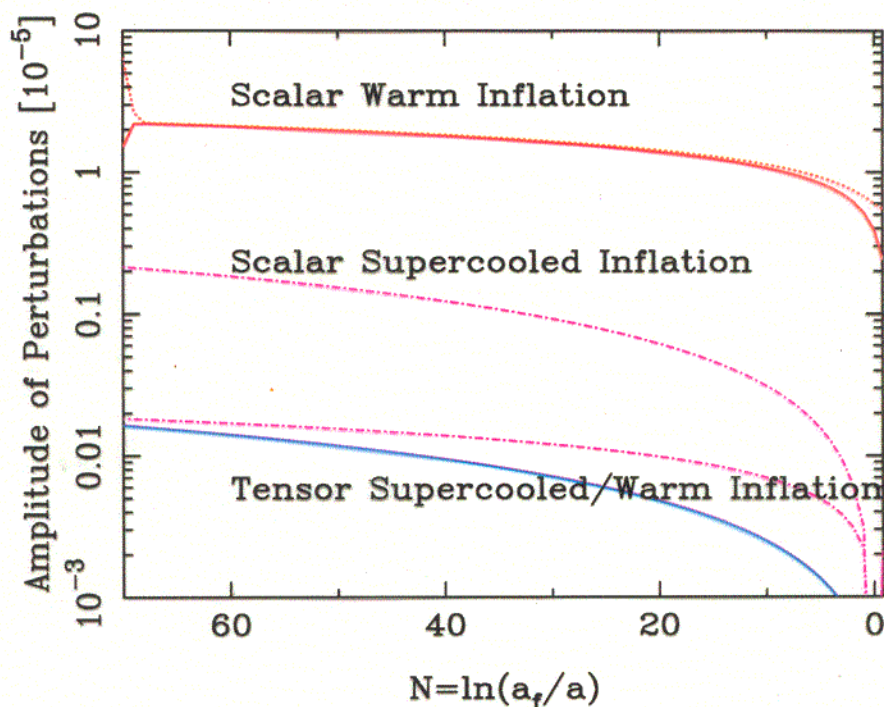


Signatures of Warm Inflation

(Taylor & Berera, 2000, Phys Rev D)

- Standard inflation has no interactions so universe is **supercooled**.
- Warm inflation includes interactions

Amplitude of perturbations: $V = \frac{1}{2}m^2\phi^2$



- Warm inflation predicts **different tensor-to-scalar ratio** than supercooled inflation.
- **No consistency relation** in warm inflation
- Mechanism for **isocurvature modes** - which may be detectable by Planck.

Non-Gaussianity in the CMB from Warm Inflation

(astro-ph/0205152, in press Phys. Rev. D)

A Gaussian distribution of gravitational field perturbations will have bispectrum

$$B \sim \langle \Phi(\mathbf{k}_1)\Phi(\mathbf{k}_2)\Phi(\mathbf{k}_3) \rangle \quad \text{equal to zero.}$$

Expanding the scalar field fluctuations to second order leads to the expression

$$\langle \Phi(\mathbf{k}_1)\Phi(\mathbf{k}_2)\Phi(\mathbf{k}_3) \rangle = A_{\text{inf}} (2\pi)^3 \delta^3(\mathbf{k}_1 + \mathbf{k}_2 + \mathbf{k}_3) [P_{\Phi}(\mathbf{k}_1)P_{\Phi}(\mathbf{k}_2) + \text{perms}],$$

where A_{inf} is not zero due to the self-interaction of the scalar field.

We find for warm inflation

$$A_{\text{inf}}^{\text{warm}} = 7 \times 10^{-2} \quad \text{compares to} \quad A_{\text{inf}}^{\text{supercooled}} = 5 \times 10^{-2} .$$

These contributions to the bispectrum are over-ridden by other physical effects, and will be undetectable in the CMB for the MAP and Planck Surveyor satellites.

Conclusion

Inflationary cosmology lacks thorough treatment of interaction dynamics - could solve the problems it confronts

- Inflation in general can occur concurrent with radiation production, warm inflation (PRL 75, 3218 (1995))

- Observational tests for radiation during inflation
 - tensor/scalar ratio (PRD 62, 083517 (2000))
 - nongaussian
 - isocurvature

- Quantum field theory robust mechanism for warm inflation (PRD 63, 103509 (2001))