

# STRUCTURE FUNCTIONS ARE NOT PARTON PROBABILITIES

Paul Hoyer

ICHEP-02 Amsterdam

25.7.2002

What do parton distributions

- extracted from DIS -

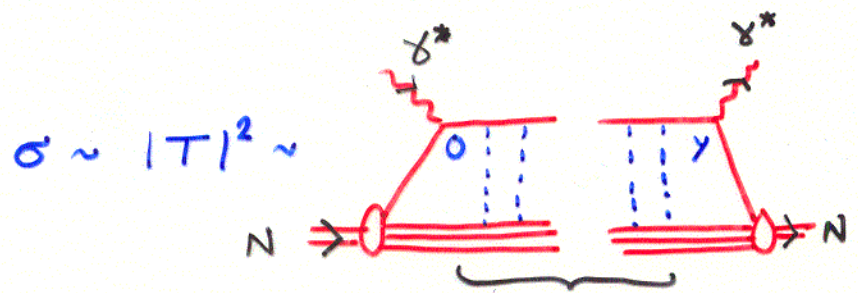
tell us about target structure?

Common belief:  $q(x, Q^2)$  is the probability to find a quark carrying momentum fraction  $x$  at resolution  $1/Q$

Turns out to be wrong! Brodsky, PH, Marchal, Peigné, Sannino  
hep-ph/0104291 = PR D65 (2002) 114025

- Misses interference effects  $\Rightarrow$  shadowing, Diffraction, Polarization
- Corrections may be large at small  $x$

DYNAMICS OF DIS: View from  $q^z \simeq -\nu$  frame



Space-time separation of  $\gamma^*$  vertices in  $T, T^*$ :

$$y = (y^+, y^-, \vec{y}_\perp)$$

$$y^+ = (y^0 + y^3) \sim \frac{1}{q^-} \sim \frac{1}{\nu} \rightarrow 0$$

$$|\vec{y}_\perp| \sim \frac{1}{Q} \rightarrow 0$$

Effect missed in probability interpretation

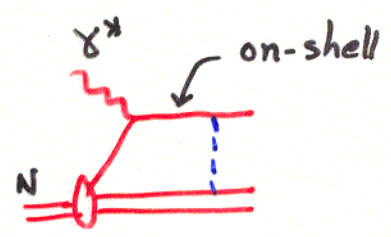
Struck quark Coulomb scatters in target

$$y^2 = y^+ y^- - y_\perp^2 \rightarrow 0 \text{ Light like separation}$$

$\gamma^*$  coherence length/along light-cone:  $y^- \sim \frac{1}{q^+} \sim \frac{\nu}{Q^2} \sim \frac{1}{2m_N x}$  Large at small  $x$

- Coulomb rescattering within  $\frac{1}{2m_N x}$  affects  $\sigma_{DIS}$

- On-shell intermediate states give DIS amplitudes complex, dynamic phases



$\Rightarrow$  Interference phenomena

Why did we believe that rescattering is irrelevant?

QCD factorization proofs give, in a general gauge:

$$q(x, Q^2) = \frac{1}{8\pi} \int dy^- \exp(-\frac{i}{2} x P^+ y^-)$$

$$* \langle N(p) | \bar{q}(y^-) \gamma^+ \underbrace{\mathbb{P} \exp\left[ig \int_0^{y^-} dw^- A^+(w^-)\right]}_{\text{Path-ordered exponential}} q(0) | N(p) \rangle_{y^+=0, y_\perp \sim 1/Q}$$

Path-ordered exponential describes Coulomb scattering

- All fields are at  $y^+ = 0$ : Equal LC time
- Expression is gauge invariant due to  $\mathbb{P} \exp[ ]$ , and valid at leading order in Bj limit:  $q^- A^+ \sim 2v A^+ \gg \vec{q}_\perp \cdot \vec{A}_\perp, \dots$  assumed
- In  $A^+ = 0$  gauge:  $\mathbb{P} \exp[ ] = 1$  and matrix element reduces to a sum of probabilities for finding a quark in  $|N\rangle$

BUT:  $A^+ = 0$  gauge is not allowed!  
Resulting expression for  $q(x, Q^2)$  is incorrect

Reason:  $q^- A^+ = 0$  is not large, derivation fails

i.e: Bj limit ( $v, Q^2 \rightarrow \infty$ ) and LC gauge limit ( $A^+ \rightarrow 0$ ) do not commute

cf.  $e\mu \rightarrow e\mu$  at Born level:  $\left\{ \begin{array}{l} s \rightarrow \infty \\ vs \\ A^+ \rightarrow 0 \end{array} \right.$  Limits do not commute

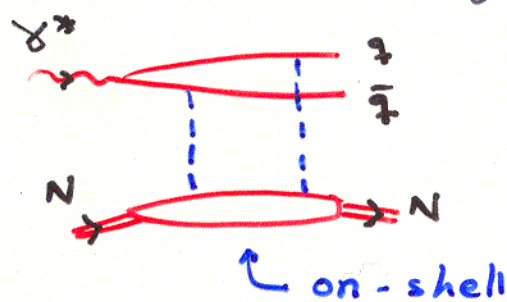
# REMARKS

- \* Correct expression for  $g(x, Q^2)$  in  $A^+ = 0$  gauge is not yet known, cf. X. Ji & F. Yuan, hep-ph/0206057
- \* Phase due to Coulomb scattering causes single spin asymmetry in semi-inclusive DIS:  $\gamma^* N_{\uparrow} \rightarrow \pi(\vec{k}_{\perp}) + X$   
 Brodsky, Hwang & Schmidt, hep-ph/0201296  
 Collins, hep-ph/0204004

This 'Sivers Effect' is unrelated to a transverse polarization of the struck quark in  $|N\rangle$

- \* Diffractive DIS is due to Coulomb rescattering

Imaginary phase of Pomeron  $\sim$  two-gluon exchange arises due to on-shell intermediate state, i.e., via rescattering



$\Rightarrow$  No "Pomeron" in target wave function!

- \* Are the rescattering effects the same in all processes i.e., is  $g(x, Q^2)$  universal?

Spin asymmetry is reversed in Drell-Yan

Collins, hep-ph/0204004

Brodsky, Hwang & Schmidt, hep-ph/0206259

Is shadowing the same in DY as in DIS?

Peigné hep-ph/0206138

$\Rightarrow$  Novel questions on 'classic' parton distributions